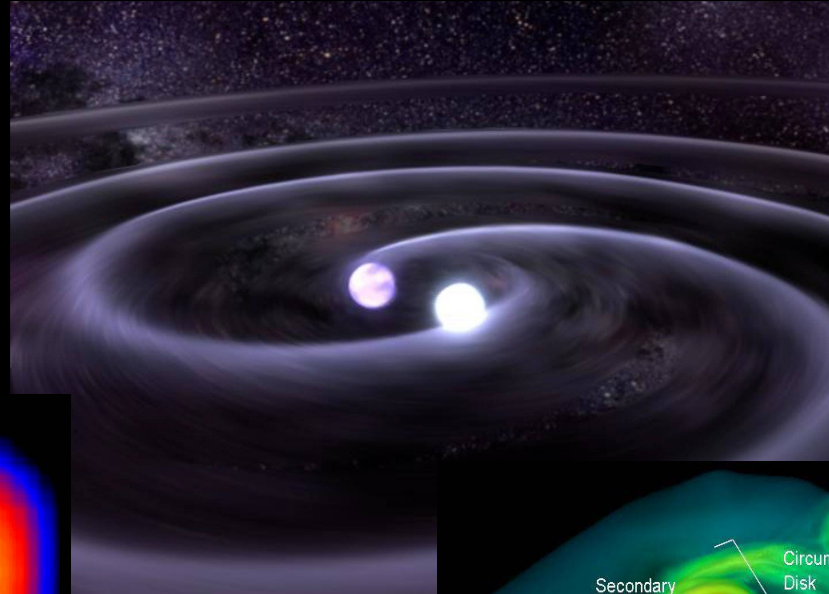
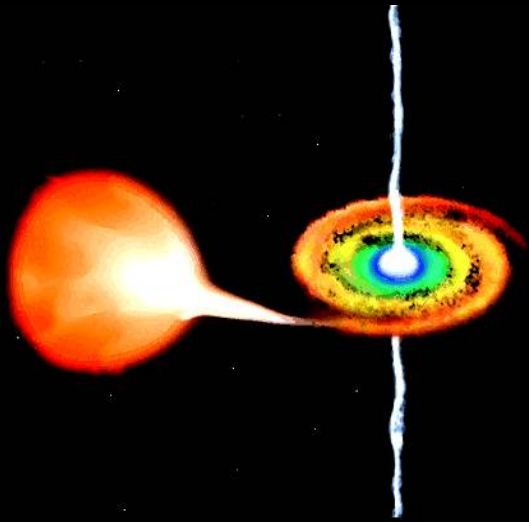
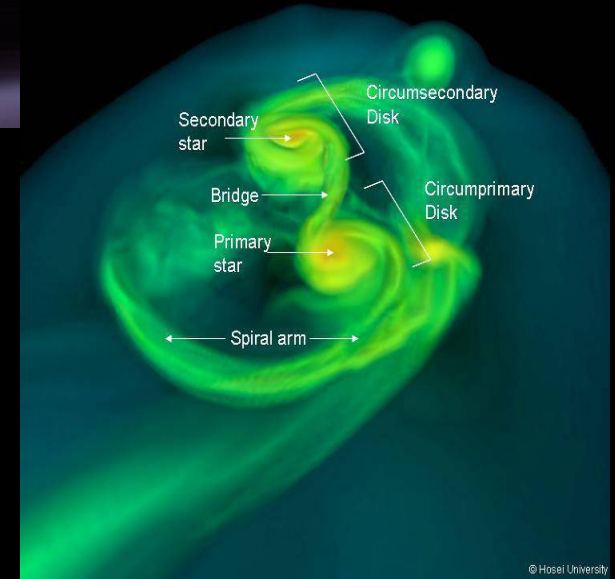
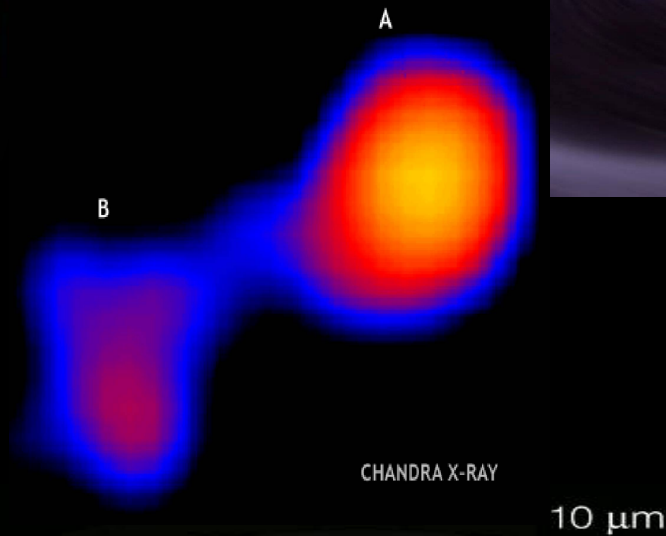


# Binary Stars – Final Lecture!



Astro 8501  
6944

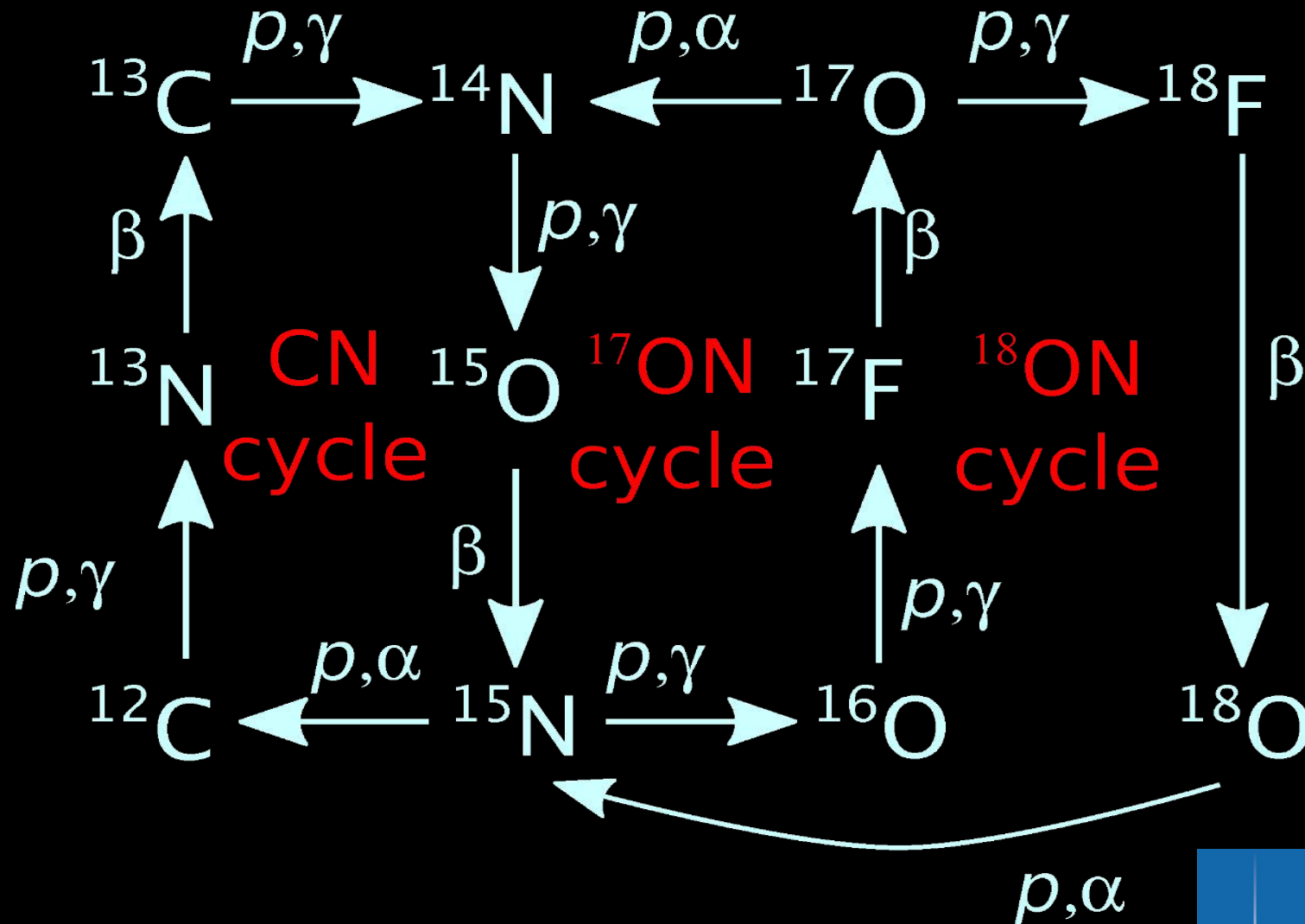


# Binary–star Nucleosynthesis

- Many types of stars are only or mostly found in binaries
- The physics we have learned about in this course will help us to understand them
- Chemically peculiar binaries:
  - Algols
  - Massive stars (WR stars etc)
  - Ba/CH/CEMP stars
  - Thermohaline mixing
  - Galactic chemical evolution

# Nuclear Burning In Stars

- All stars burn H to He, e.g. CNO cycle



# CN cycle

$$\frac{d}{dt} \begin{bmatrix} {}^{12}\text{C} \\ {}^{13}\text{C} \\ {}^{14}\text{N} \end{bmatrix} = \begin{bmatrix} -1/\tau_{12} & 0 & 1/\tau_{14} \\ 1/\tau_{12} & -1/\tau_{13} & 0 \\ 0 & 1/\tau_{13} & -1/\tau_{14} \end{bmatrix} \begin{bmatrix} {}^{12}\text{C} \\ {}^{13}\text{C} \\ {}^{14}\text{N} \end{bmatrix}$$

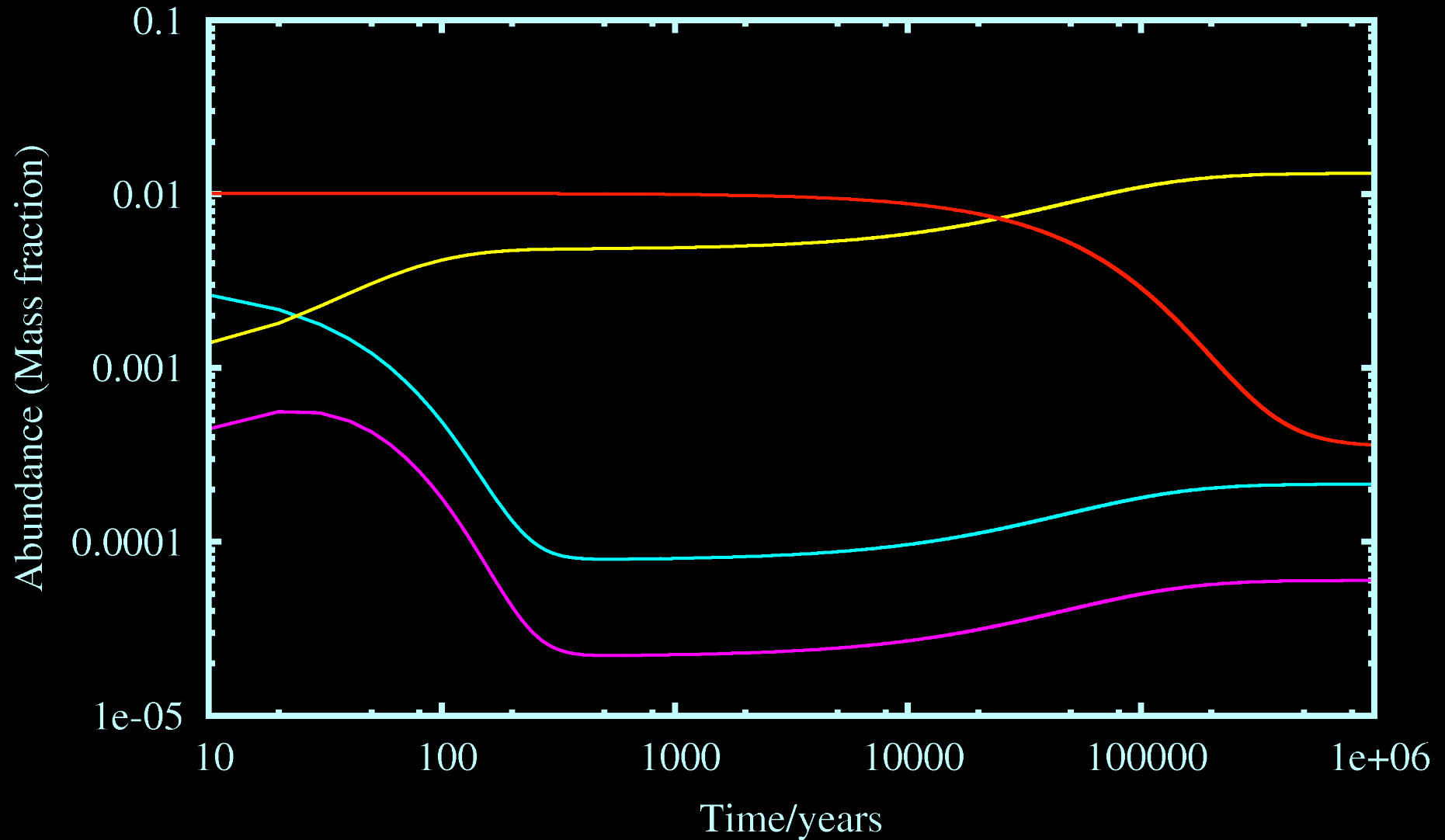
$$\frac{d}{dt} \mathbf{U} = \Lambda \mathbf{U}$$

$$\mathbf{U}(t) = A e^{\lambda_1 t} \mathbf{U}_1 + B e^{\lambda_2 t} \mathbf{U}_2 + C e^{\lambda_3 t} \mathbf{U}_3$$

And similarly for the other cycles  
See e.g. Clayton's book

# CNO cycle

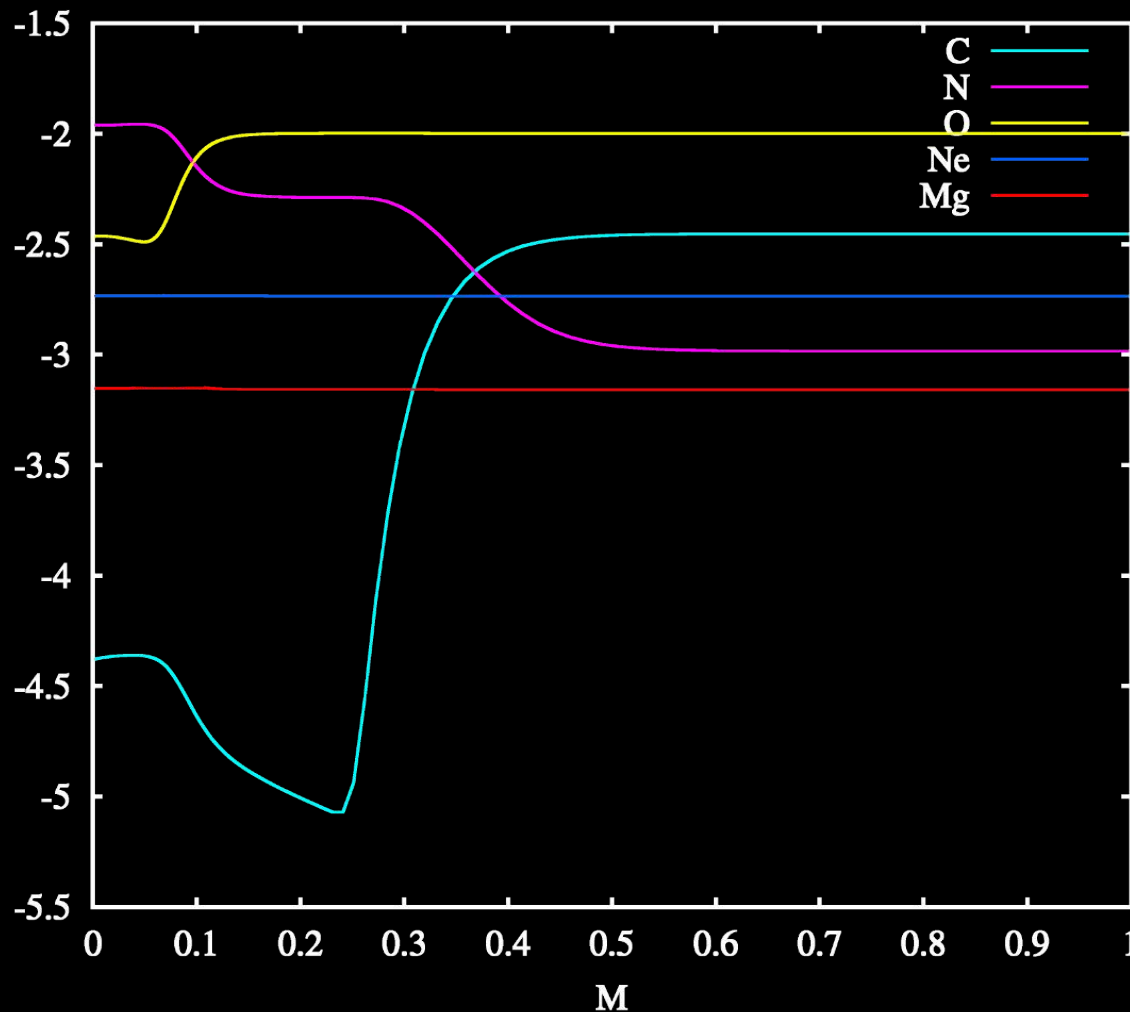
CNO cycle at  $T=4 \times 10^7$  K,  $\rho=1.0$  g/cm<sup>3</sup>



C12 — C13 — N14 — O16 —

# Internal stellar evolution

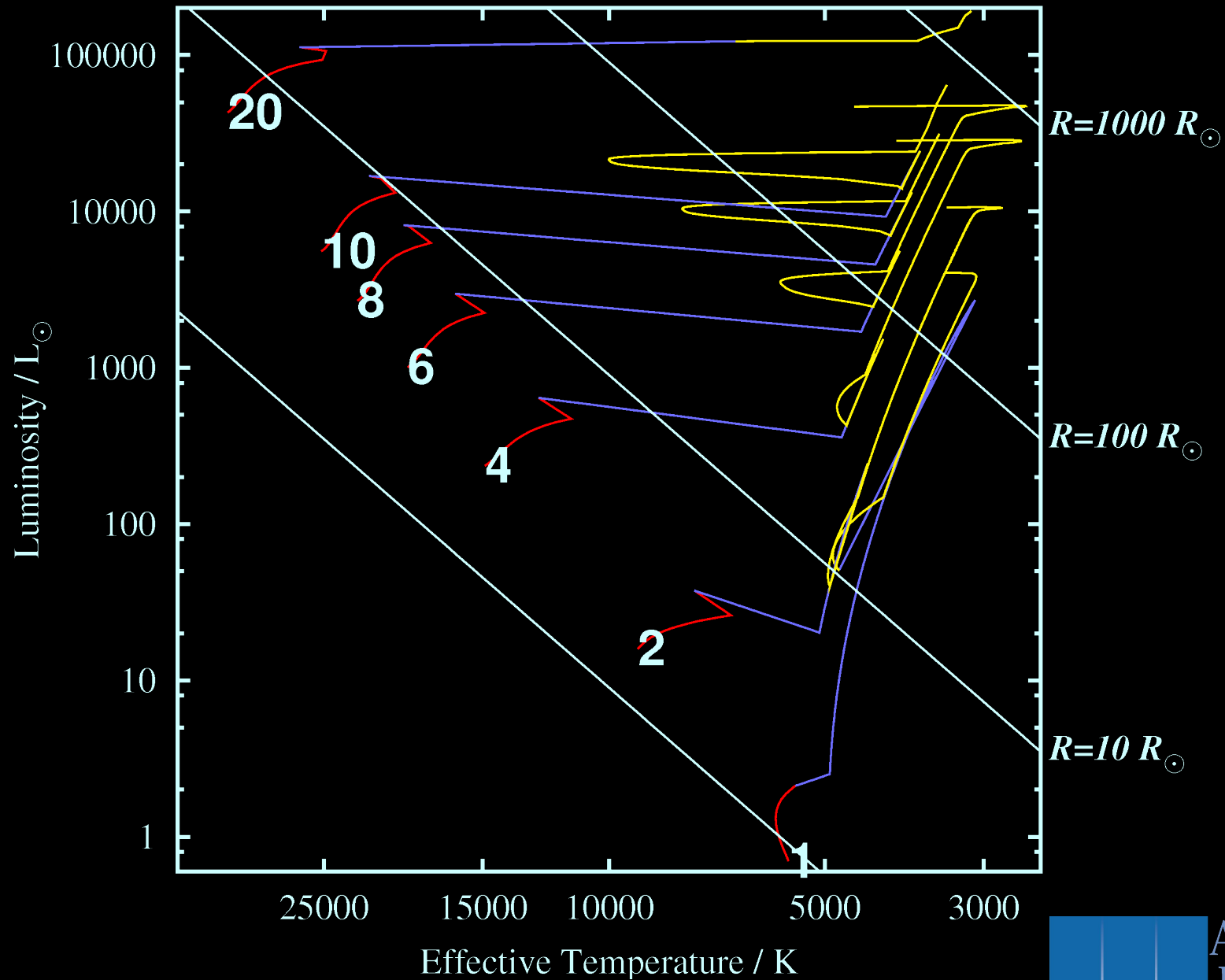
- Composition changes inside a star



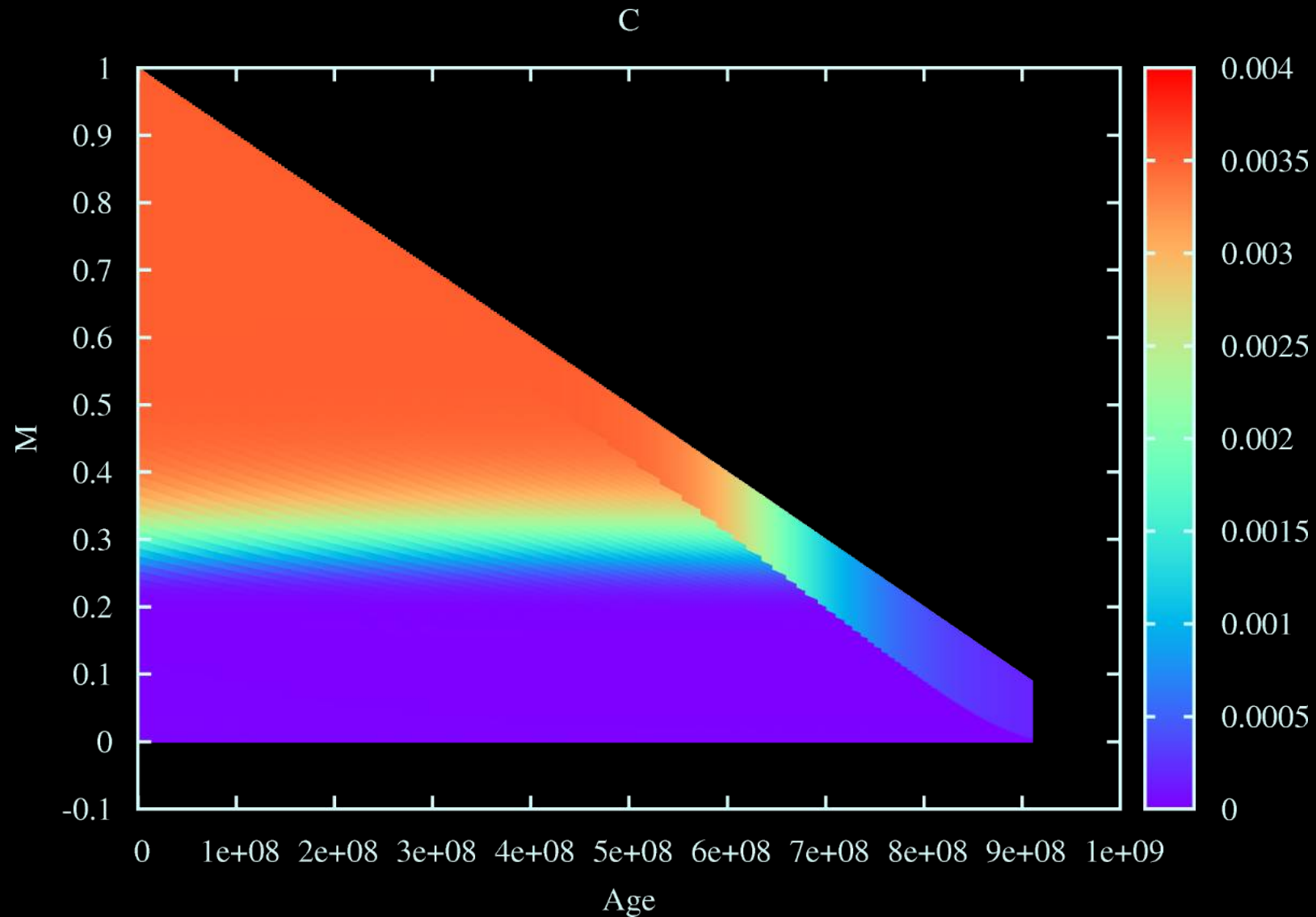
1  $M_{\odot}$

TAMS

# Mass transfer



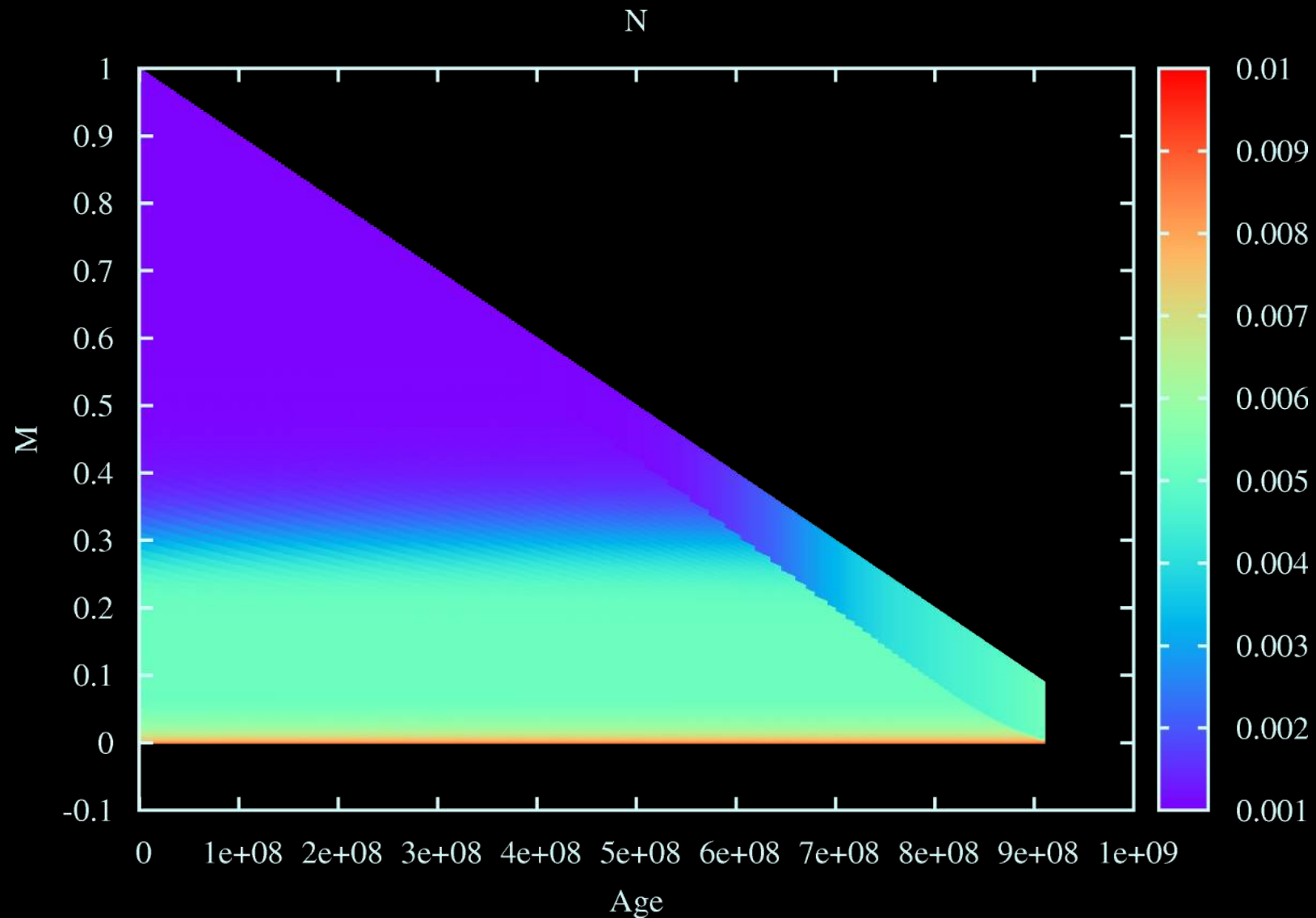
# Stripping a solar-mass star



Models made with *Window To The Stars*  
<http://www.astro.uni-bonn.de/~izzard/window.html>

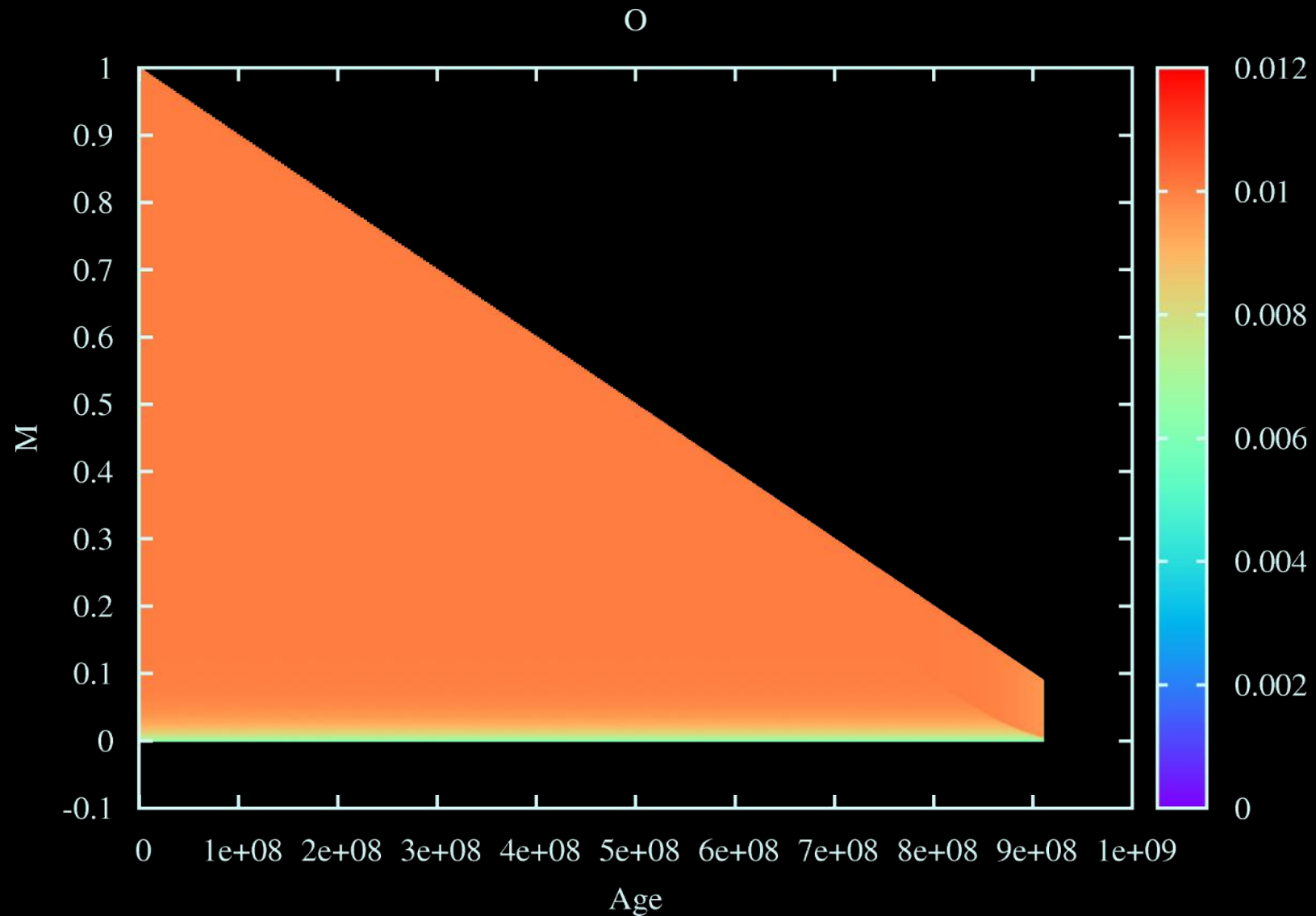


# Stripping a solar-mass star



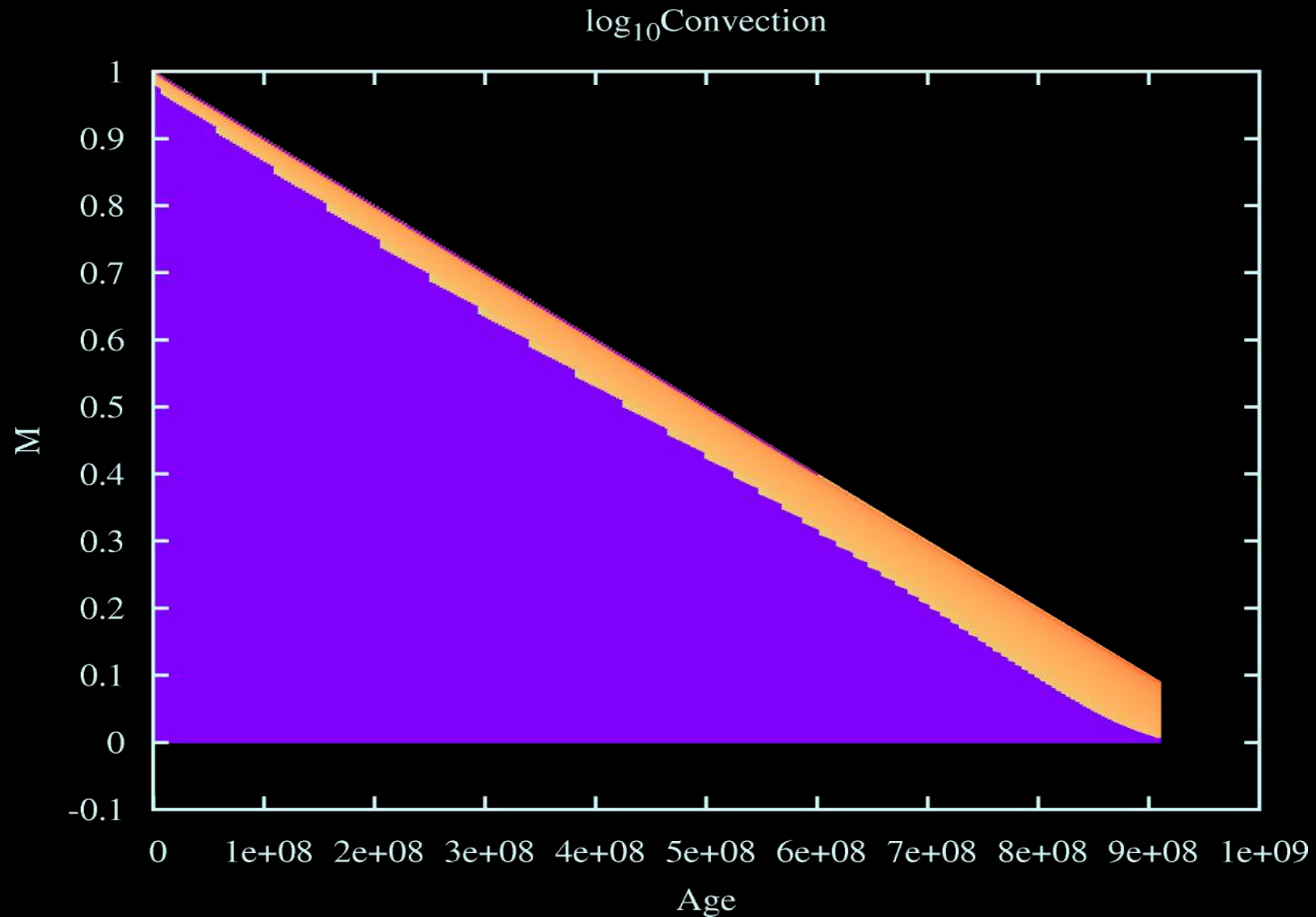
Models made with *Window To The Stars*  
<http://www.astro.uni-bonn.de/~izzard/window.html>

# Stripping a solar-mass star



Models made with *Window To The Stars*  
<http://www.astro.uni-bonn.de/~izzard/window.html>

# Stripping a solar-mass star



Models made with *Window To The Stars*  
<http://www.astro.uni-bonn.de/~izzard/window.html>

# Algol observations

- Algols have N-enriched mass donors
- Stripping leads to exposed layers

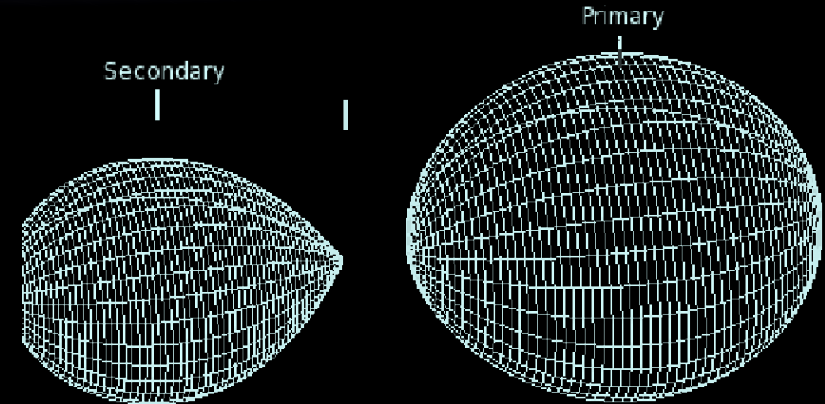
# Observed e.g. LZ Cep

Mahy et al 2011  
ArXiv 1106.6162

**Table 2.** Orbital solution and stellar parameters.

	Primary	Secondary
$P$ [d]	3.070507 (fixed)	
$e$	0.0 (fixed)	
$T_0$ [HJD - 2450000]	5032.019±0.002	
$q(M_1/M_2)$	2.53±0.05	
$\gamma$ [km s <sup>-1</sup> ]	-11.81±0.91	-11.40±1.20
$K$ [km s <sup>-1</sup> ]	88.72±1.02	224.48±2.58
$a \sin i$ [ $R_\odot$ ]	5.38±0.06	13.61±0.16
$M \sin^3 i$ [ $M_\odot$ ]	7.00±0.18	2.77±0.05
rms [km s <sup>-1</sup> ]	2.9198	
$T_{\text{eff}}$ [K]	32000±1000	28000±1000
$\log \frac{L}{L_\odot}$	5.11 <sup>+0.19</sup> <sub>-0.16</sub>	4.69 <sup>+0.19</sup> <sub>-0.16</sub>
$\log g$	3.5±0.1	3.1±0.1
$M_{\text{spec}}$ [ $M_\odot$ ]	15.9 <sup>+0.8</sup> <sub>-1.4</sub>	4.1 <sup>+2.4</sup> <sub>-2.1</sub>
$M_{\text{ev}}$ [ $M_\odot$ ]	25.3 <sup>+1.2</sup> <sub>-1.9</sub>	18.0 <sup>+2.1</sup> <sub>-2.5</sub>
radius [ $R_\odot$ ]	11.7 <sup>+1.3</sup> <sub>-2.7</sub>	9.4 <sup>+2.8</sup> <sub>-2.2</sub>
He/H	0.1±0.02	0.4±0.1
C/H [ $\times 10^{-4}$ ]	1.0±0.5	0.3±0.2
N/H [ $\times 10^{-4}$ ]	0.85±0.2	12.0±2.0
O/H [ $\times 10^{-4}$ ]	3.0±0.5	0.5±0.3
$V \sin i$ [km s <sup>-1</sup> ]	130±10	80±10
$v_{\text{mac}}$ [km s <sup>-1</sup> ]	40±5	44±5
$\dot{M}$ [ $10^{-8} M_\odot \text{ yr}^{-1}$ ]	1.0±0.3	-
$v_\infty$ [km s <sup>-1</sup> ]	1800±100	-

**Notes.** The given errors correspond to 1- $\sigma$ . The solar abundances for the chemical elements quoted here are He/H = 0.1, C/H =  $2.45 \times 10^{-4}$ , N/H =  $0.60 \times 10^{-4}$ , O/H =  $4.57 \times 10^{-4}$ , respectively.



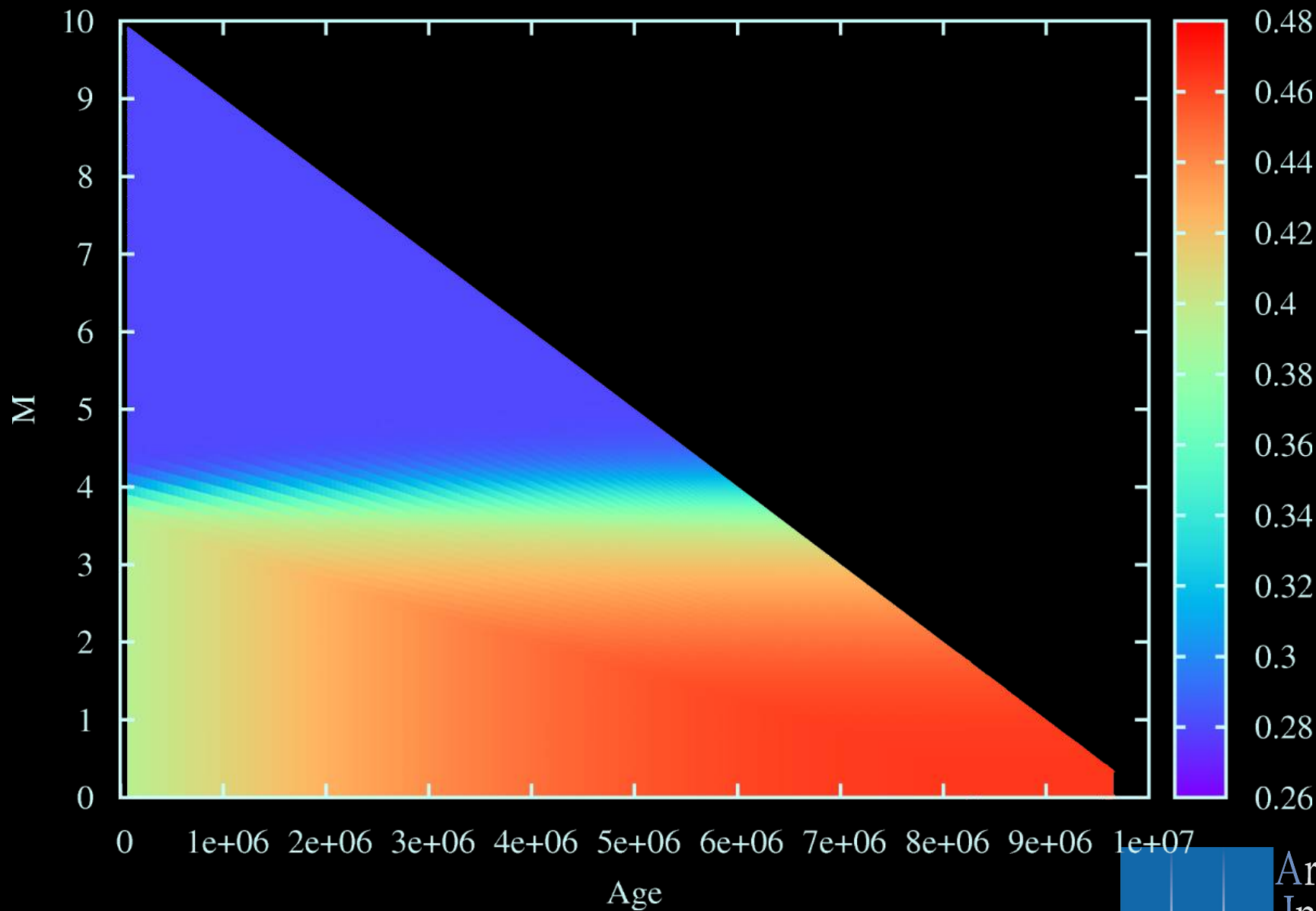
**Table 3.** Parameters fitted from the Hipparcos light curve.

Parameters	Sol 1	Sol 2
$i$ [°]	50.1 <sup>+2.1</sup> <sub>-1.5</sub>	48.1 <sup>+2.0</sup> <sub>-0.7</sub>
$q$ [ $M_1/M_2$ ]	2.53 (fixed)	2.53 (fixed)
Filling factor primary [%]	98.0 <sup>+1.2</sup> <sub>-1.0</sub>	94.8 <sup>+2.0</sup> <sub>-3.0</sub>
Filling factor secondary [%]	87.0 <sup>+3.0</sup> <sub>-5.0</sub>	98.6 <sup>+0.3</sup> <sub>-1.5</sub>
$T_{\text{eff,p}}$ [K]	32000 (fixed)	32000 (fixed)
$T_{\text{eff,s}}$ [K]	28000 (fixed)	28000 (fixed)
$M_p$ [ $M_\odot$ ]	15.5 <sup>+1.0</sup> <sub>-1.0</sub>	16.9 <sup>+1.0</sup> <sub>-1.0</sub>
$M_s$ [ $M_\odot$ ]	6.1 <sup>+1.0</sup> <sub>-1.0</sub>	6.7 <sup>+1.0</sup> <sub>-1.0</sub>
$R_{\text{pole,p}}$ [ $R_\odot$ ]	10.5 <sup>+1.2</sup> <sub>-1.2</sub>	10.5 <sup>+1.2</sup> <sub>-1.2</sub>
$R_{\text{pole,s}}$ [ $R_\odot$ ]	6.1 <sup>+1.2</sup> <sub>-1.2</sub>	7.1 <sup>+1.2</sup> <sub>-1.2</sub>
$R_{\text{equ,p}}$ [ $R_\odot$ ]	13.1 <sup>+1.2</sup> <sub>-1.2</sub>	12.4 <sup>+1.2</sup> <sub>-1.2</sub>
$R_{\text{equ,s}}$ [ $R_\odot$ ]	6.9 <sup>+1.2</sup> <sub>-1.2</sub>	9.3 <sup>+1.2</sup> <sub>-1.2</sub>

**Notes.** The index 'p' ('s') refers to the primary (secondary).  $R_{\text{pole}}$  is the polar radius, and  $R_{\text{equ}}$  the equatorial radius.

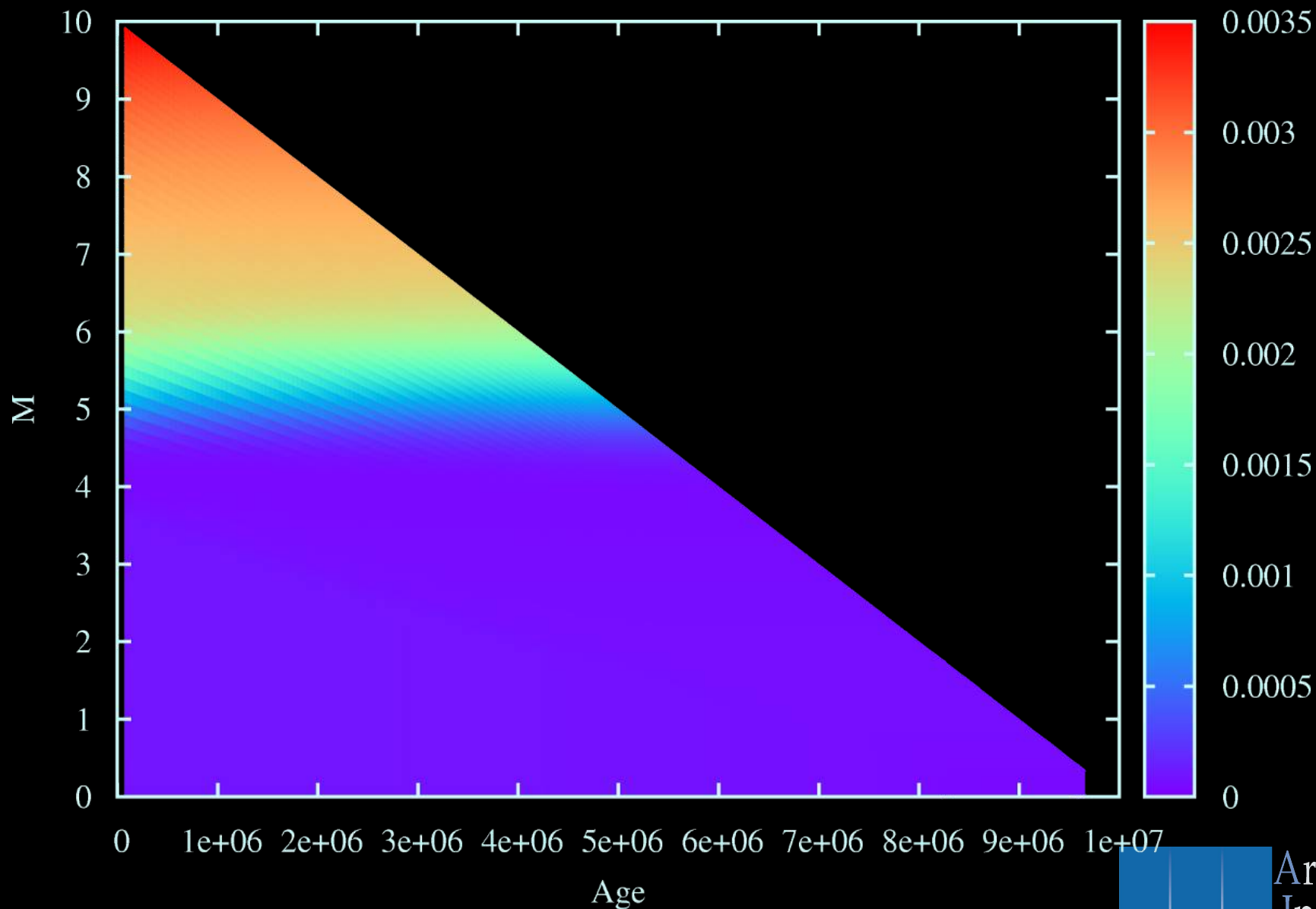
# 10Msun stripped

He

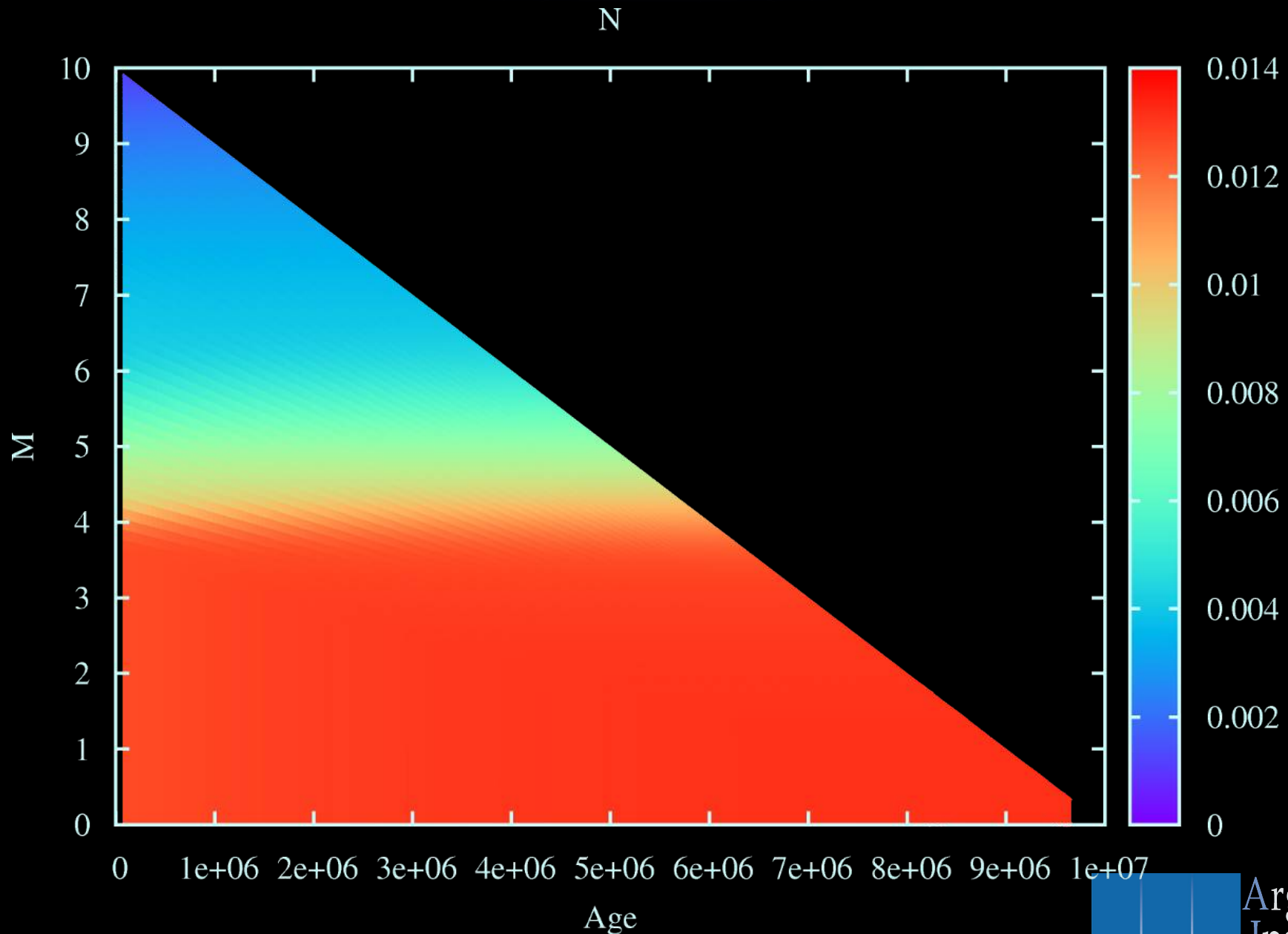


# 10Msun stripped

c



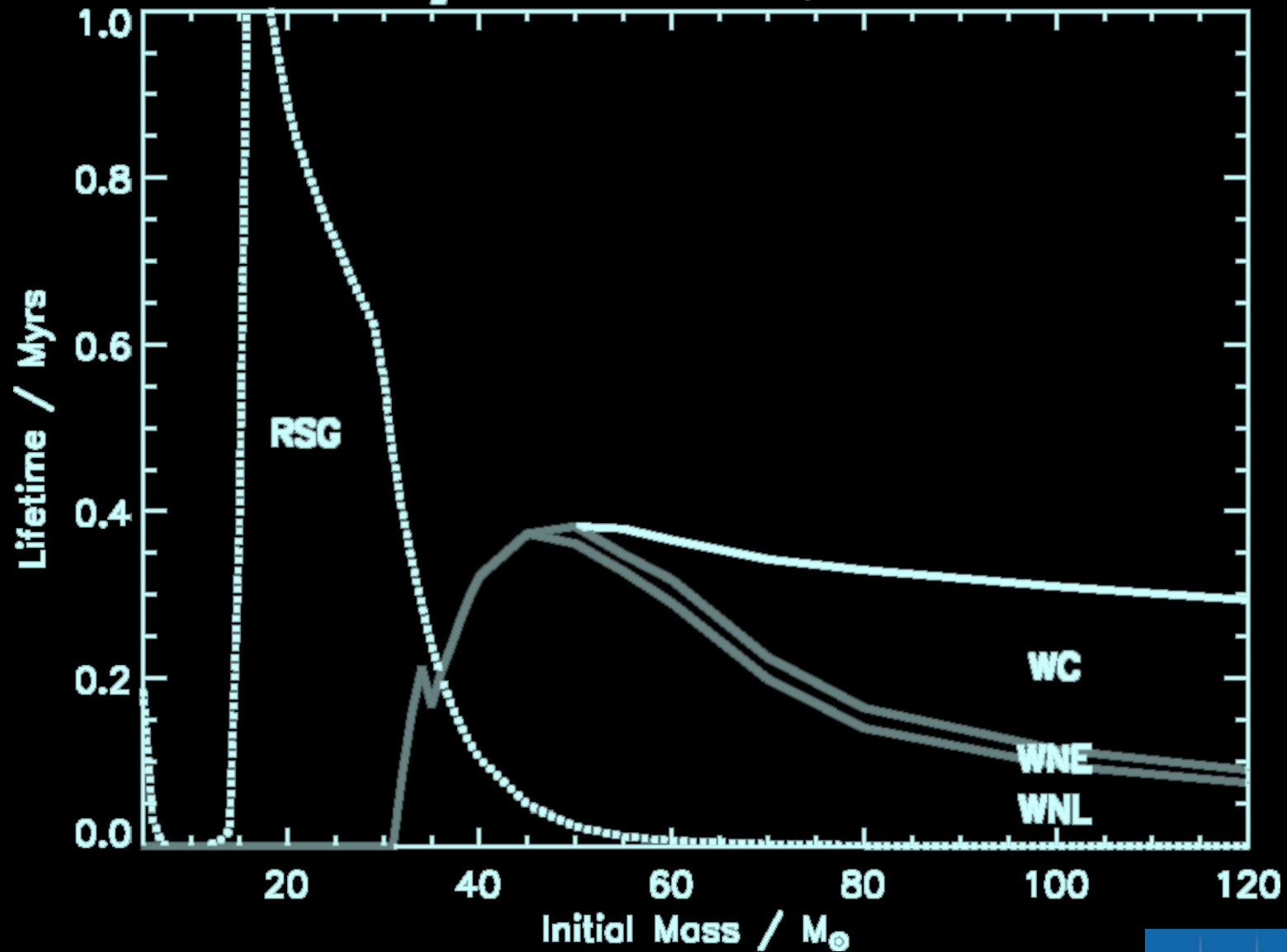
# 10Msun stripped





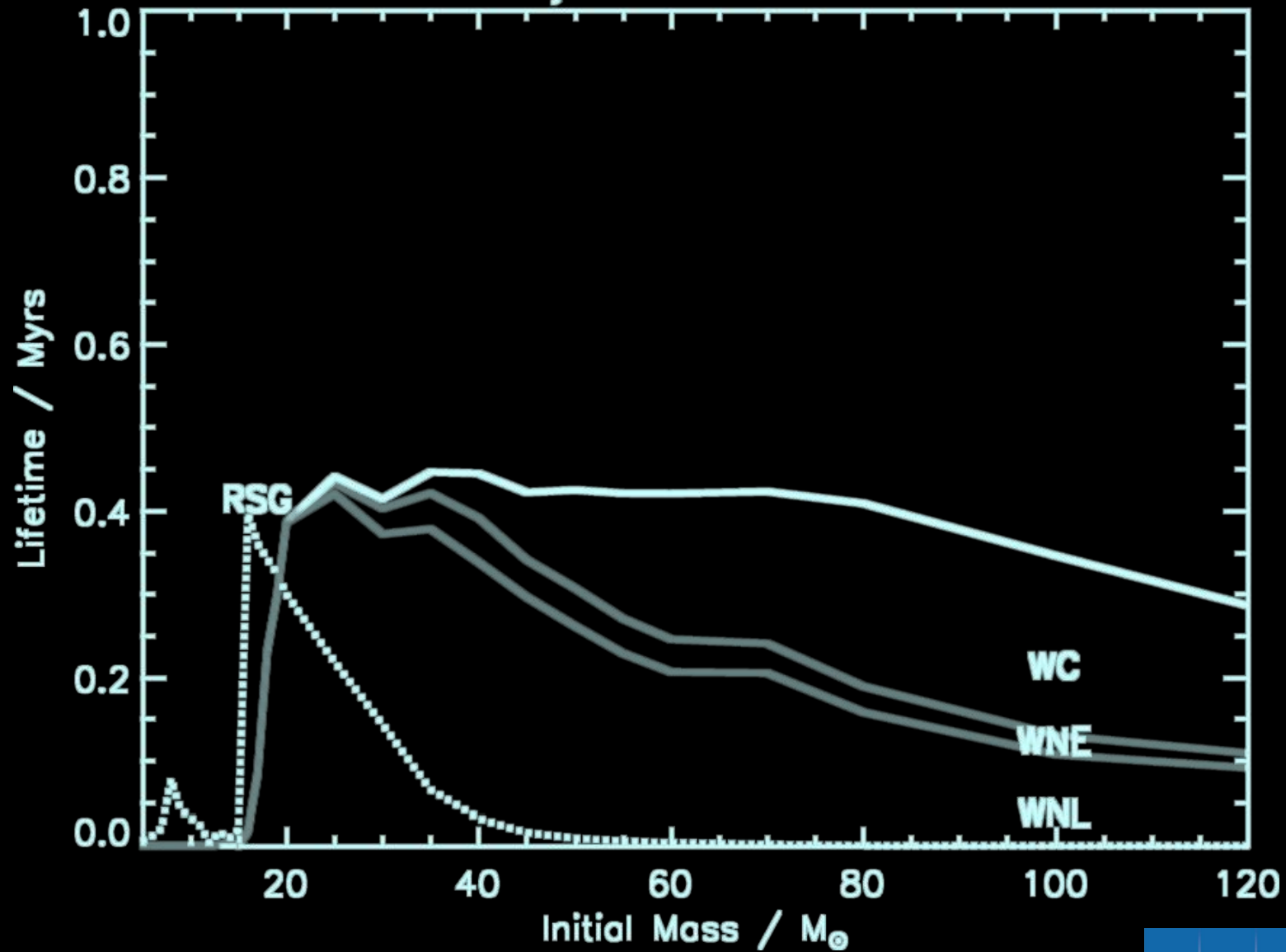
# Red Supergiants

Single stars models,  $Z=0.004$

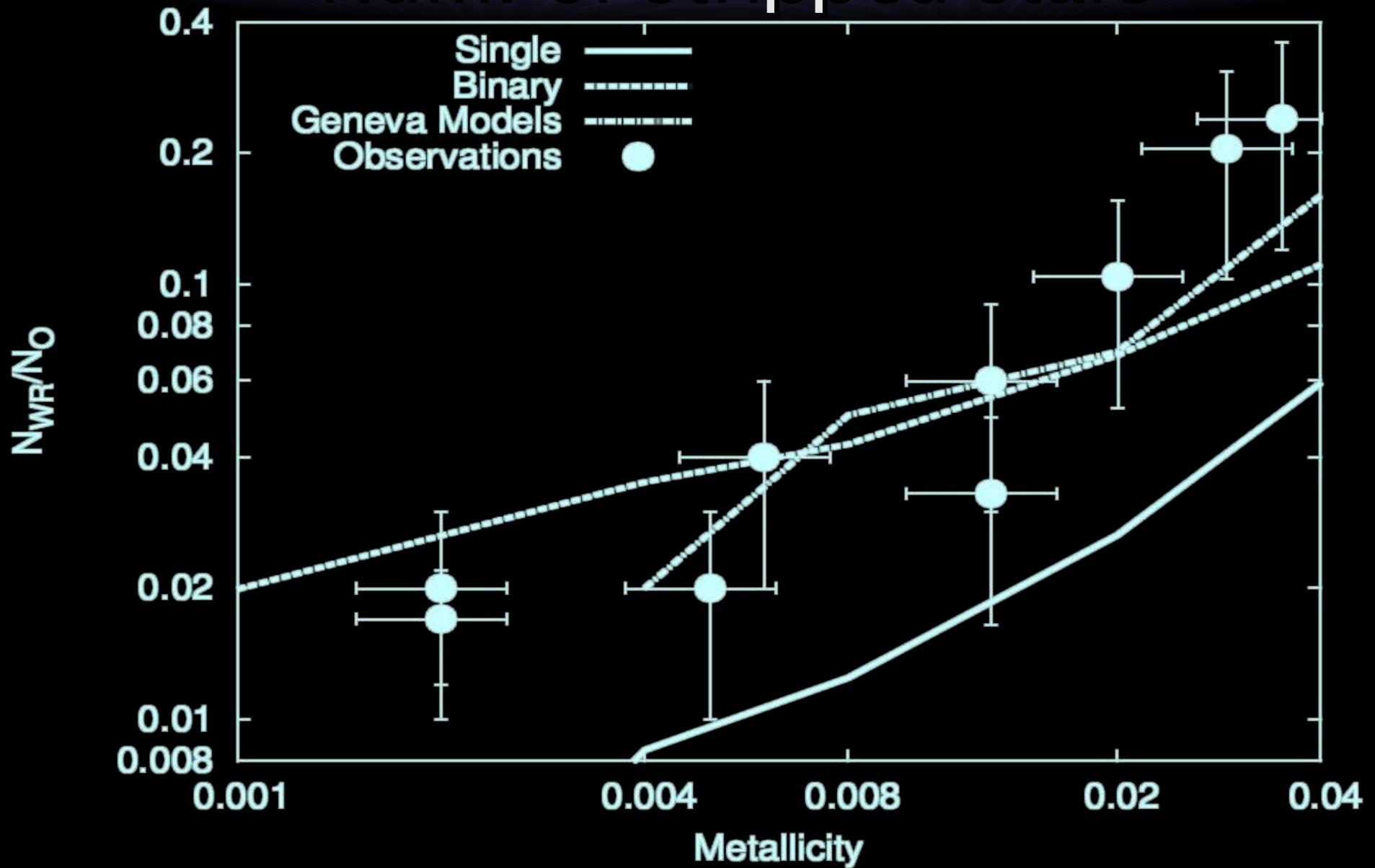


# Red Supergiants

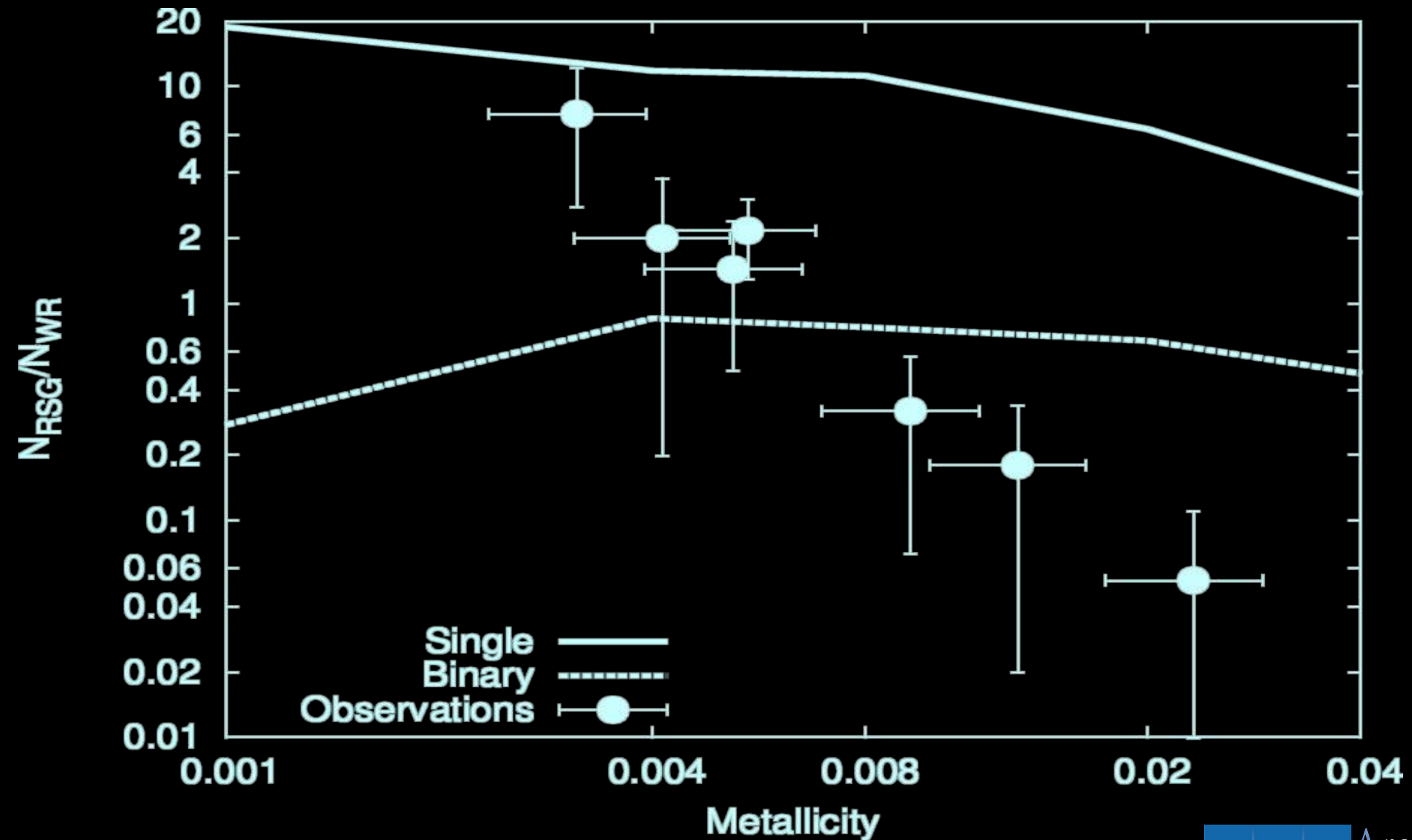
Primary models,  $Z=0.004$



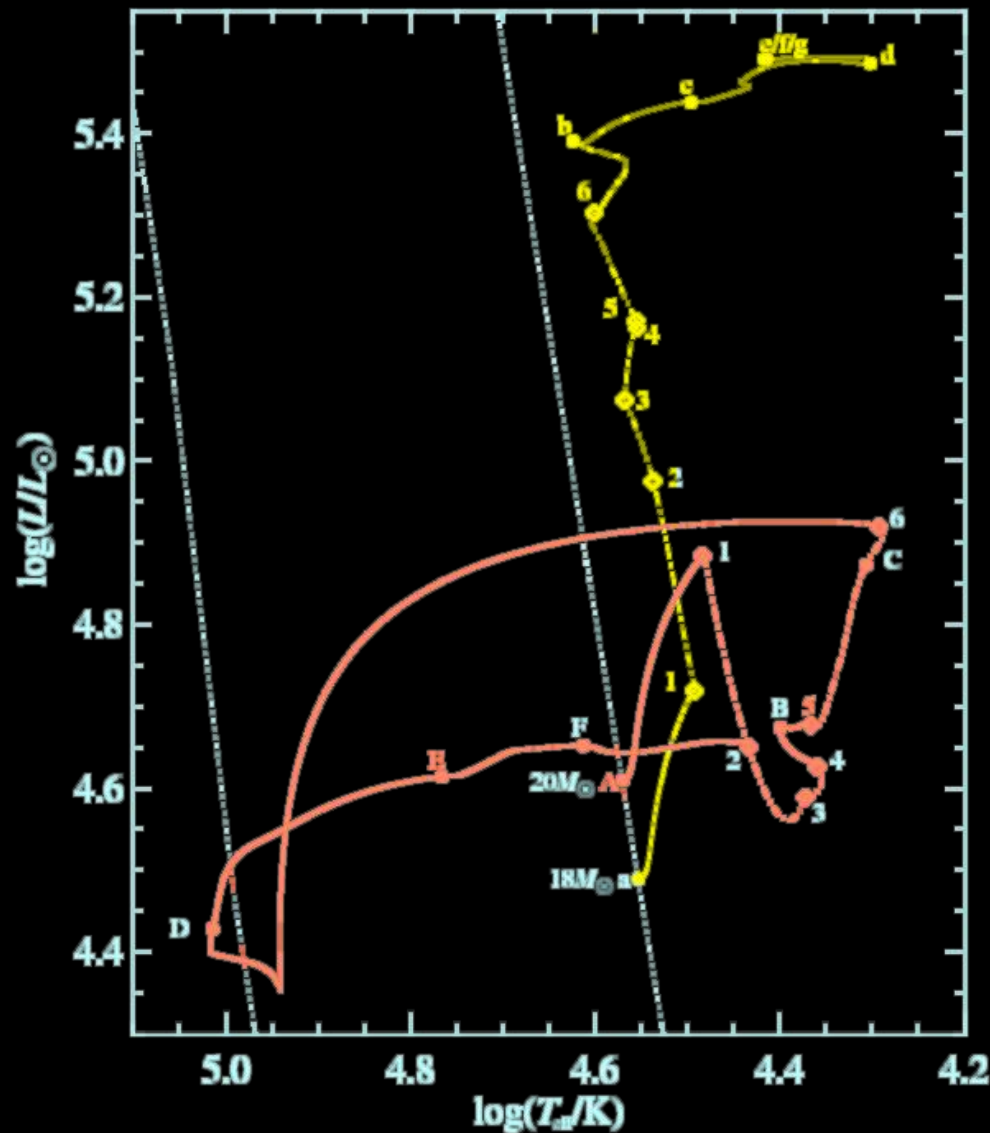
# Num. of stripped stars



# Num. of stripped stars



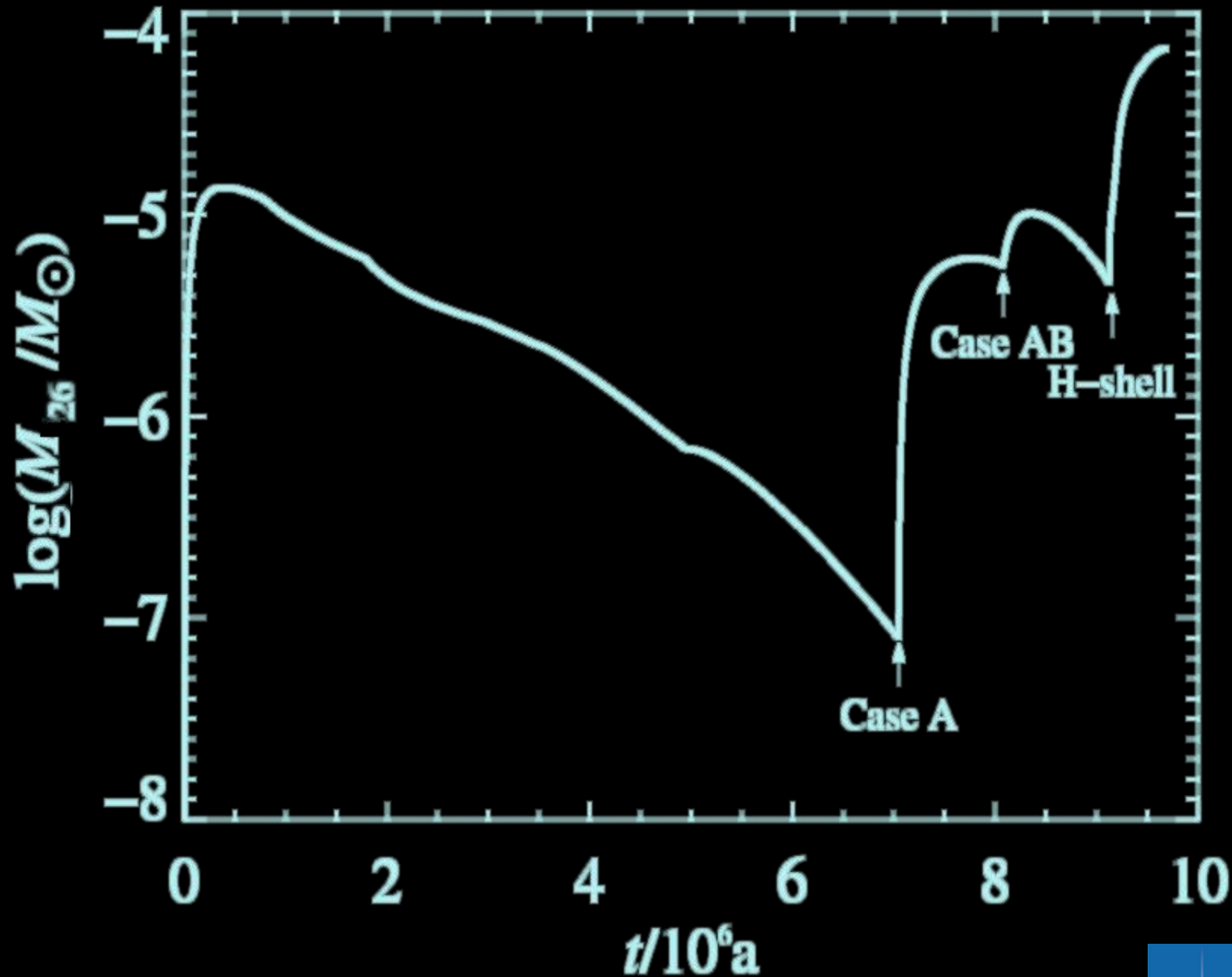
# Effects of Accretion: A126



Langer, Braun,  
Wellstein 1998

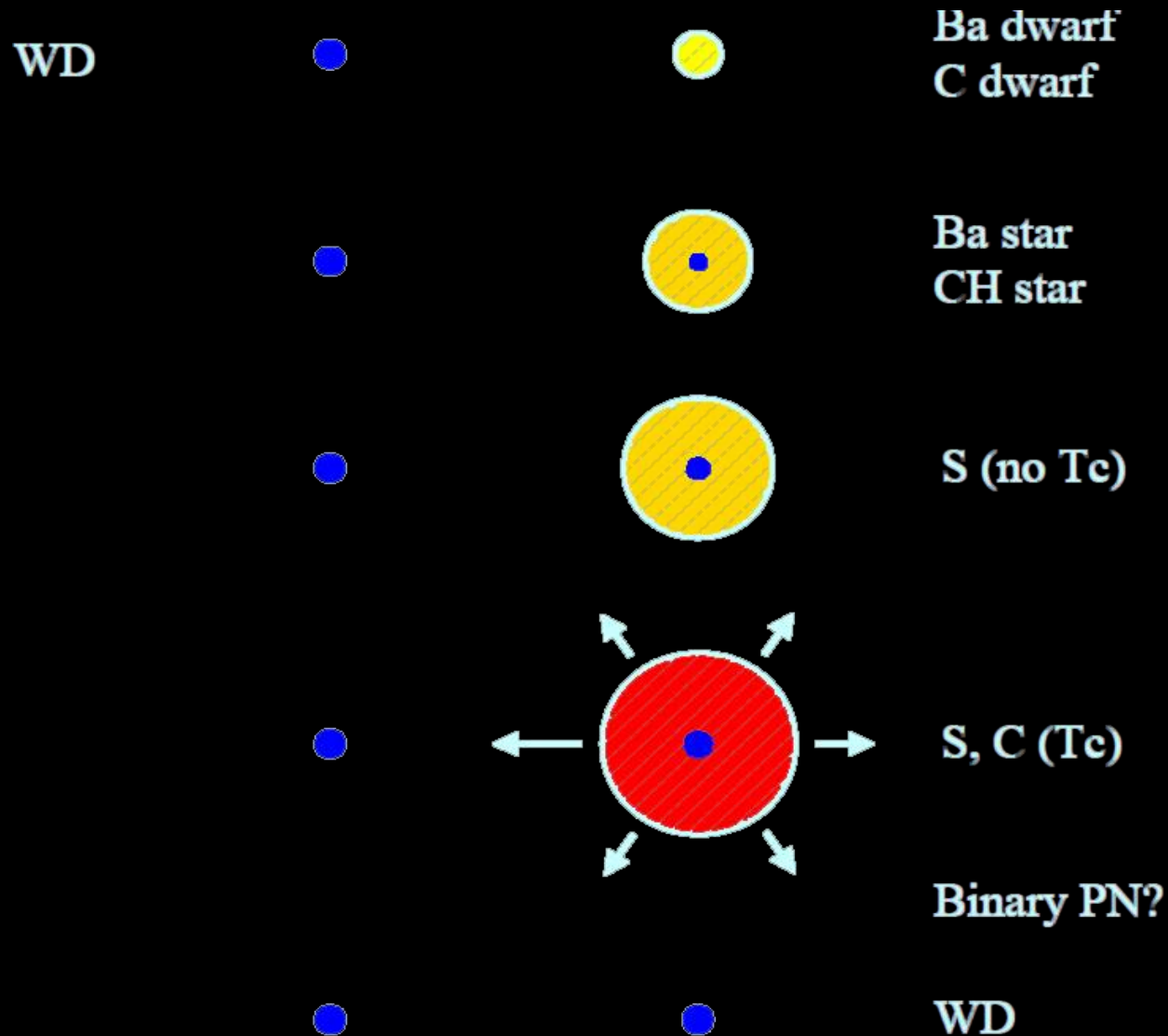
**Figure 1: Evolutionary tracks in the HR diagram of the components of a  $20+18 M_{\odot}$  case A close binary system with a metallicity of  $Z_{\odot}/4$  and an initial period of 2.5 days.**

# Effects of Accretion: Al26





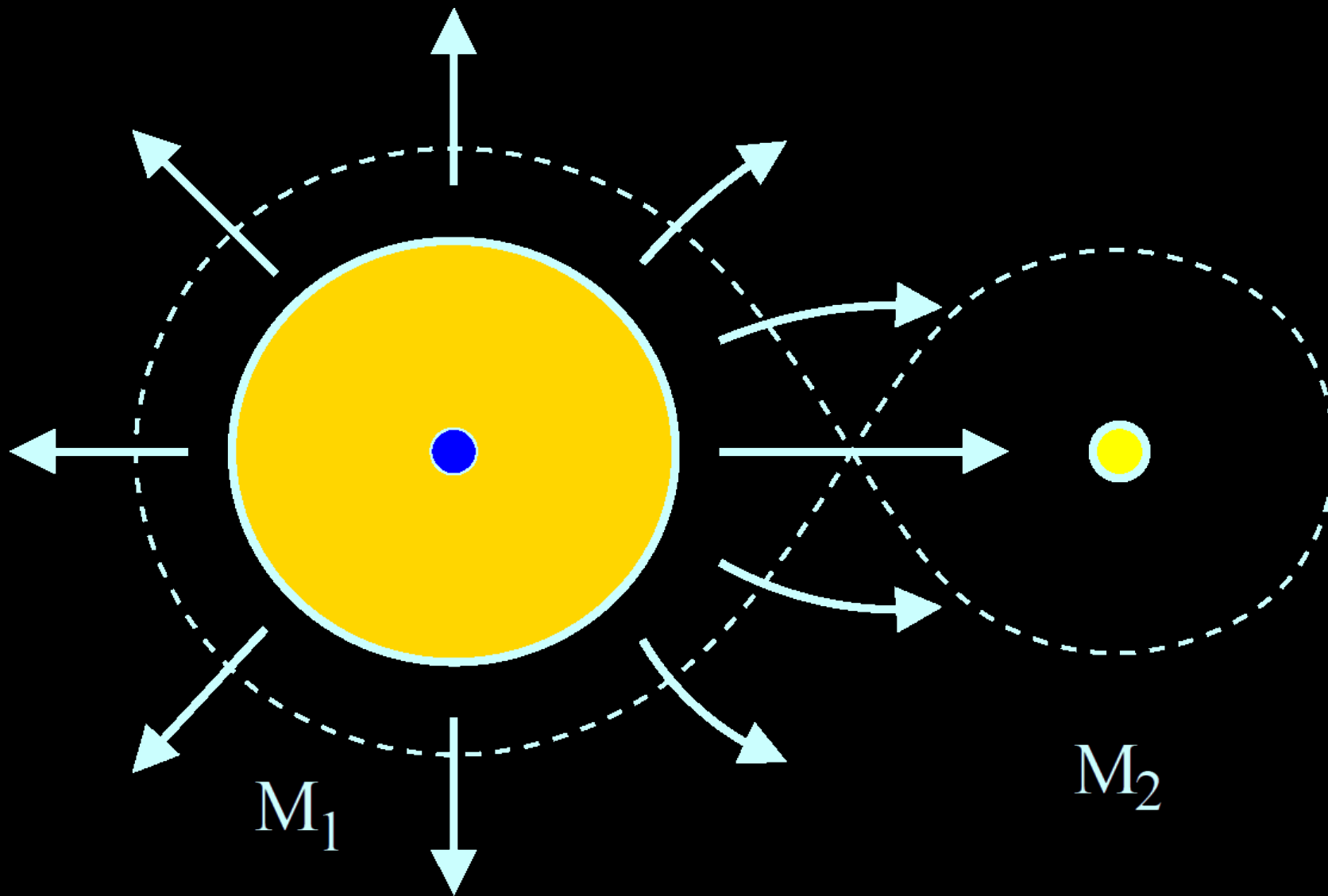
# Wind mass transfer



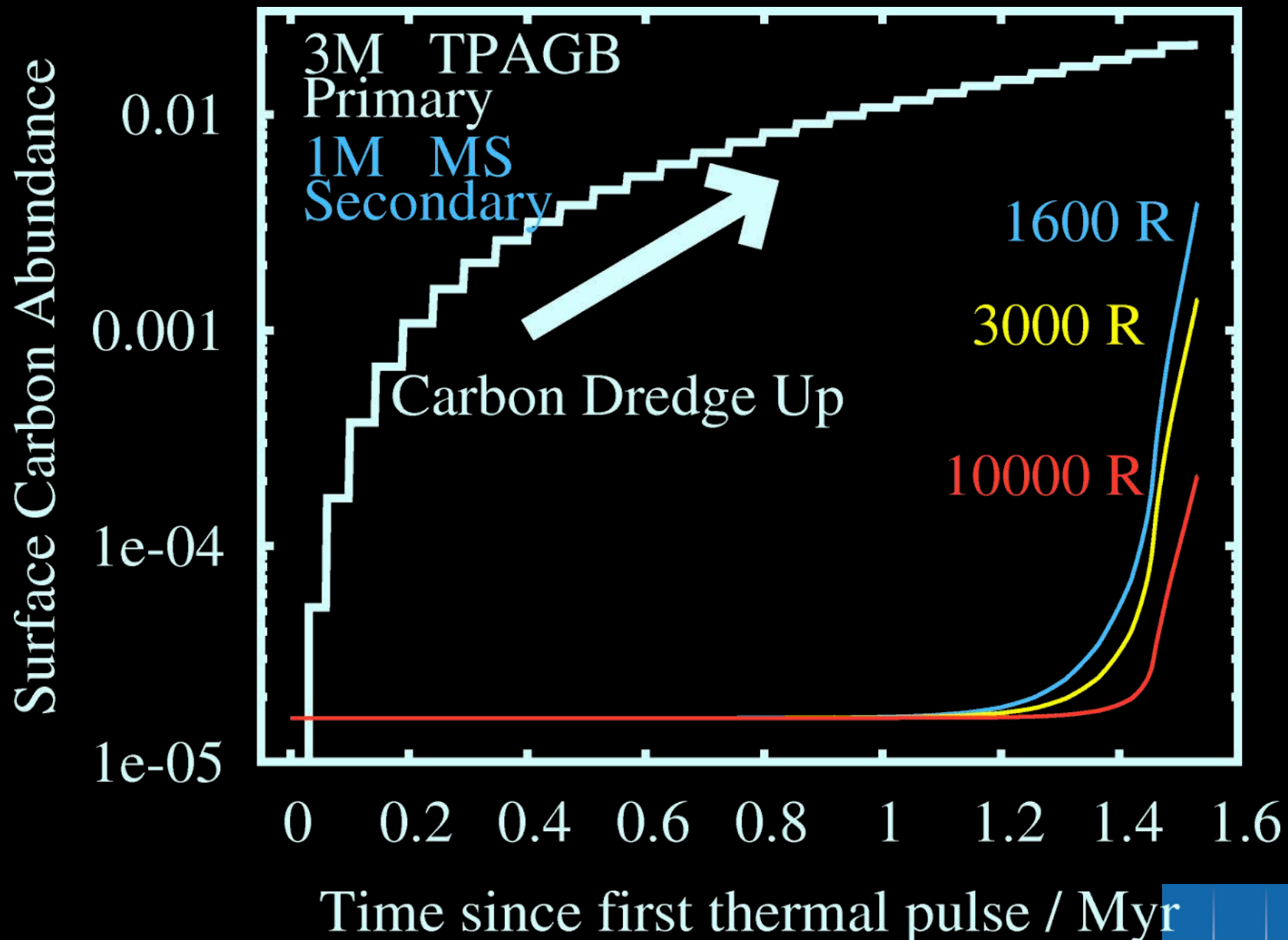
Jorissen 1999 IAUS 191,437



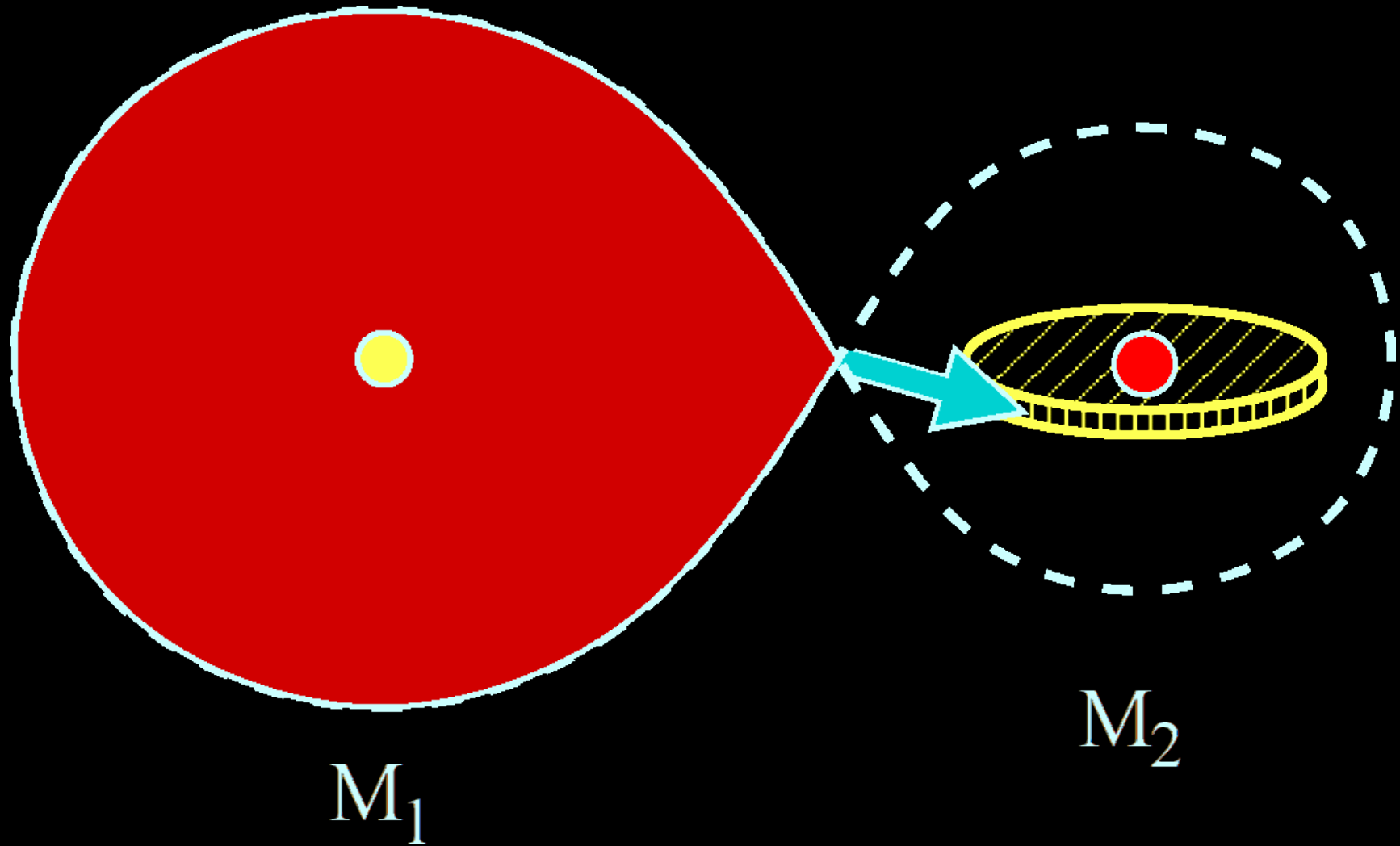
# Wind Accretion



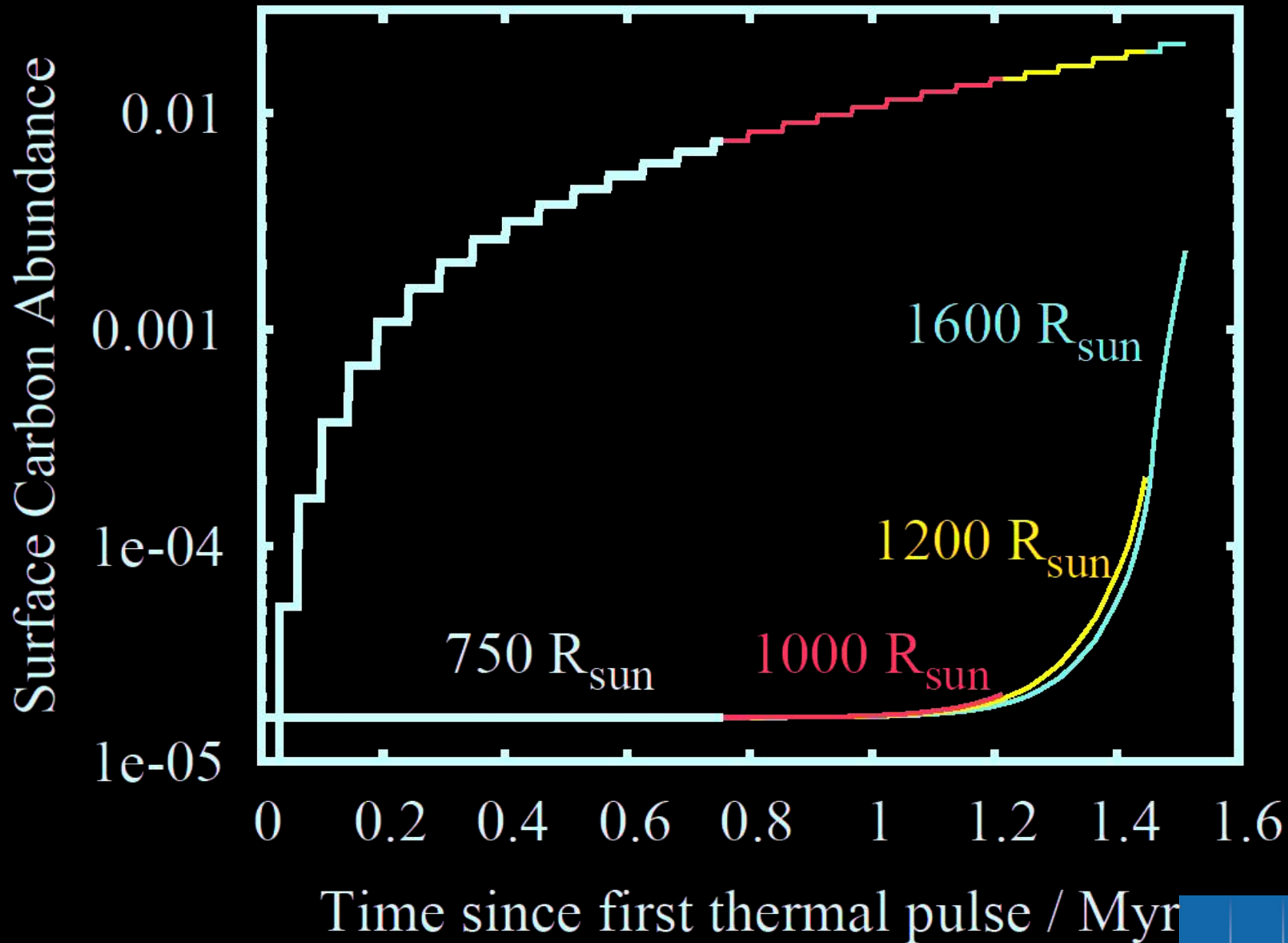
# Wider systems: barium/CH stars



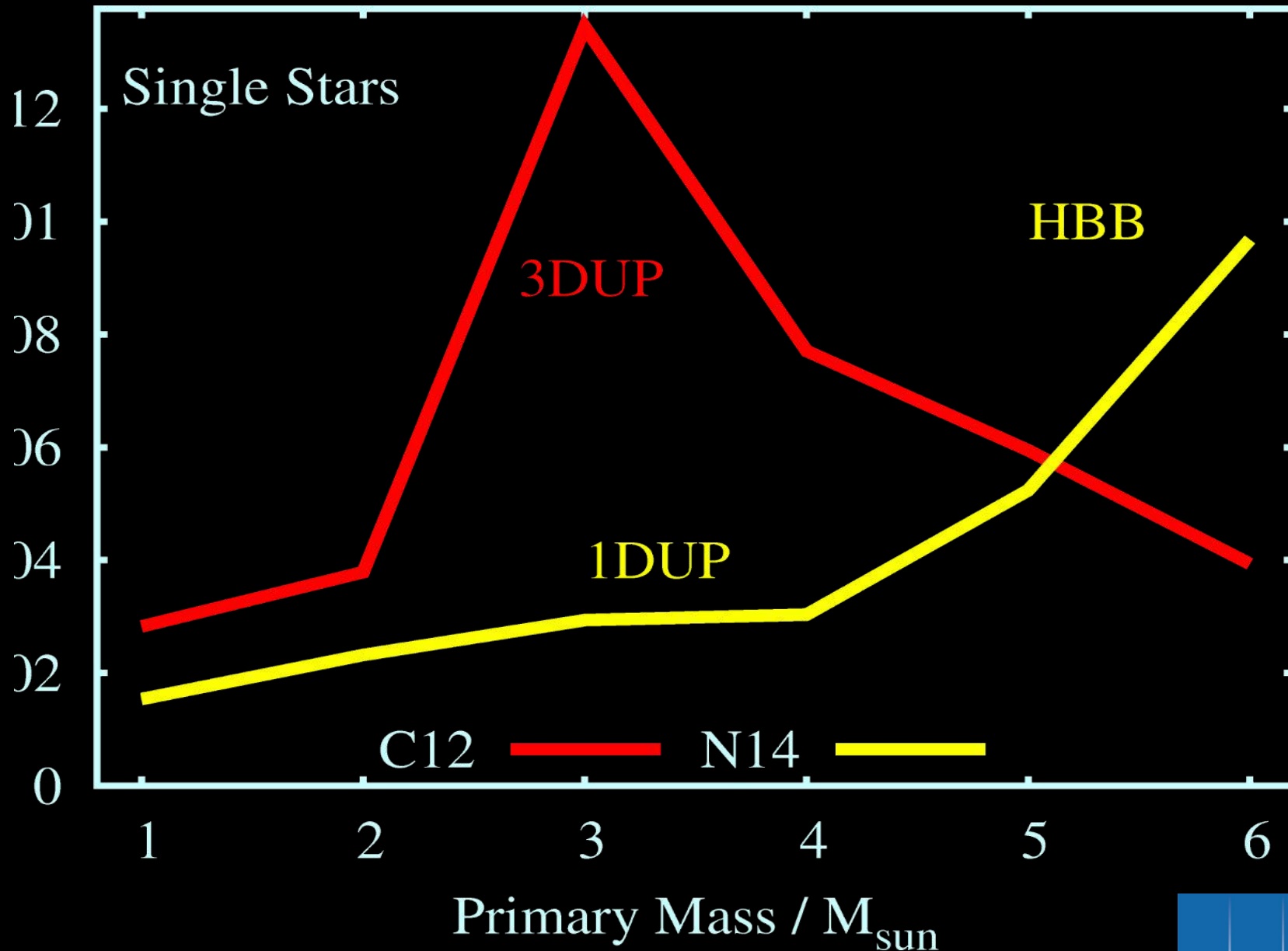
# Also RLOF if close enough



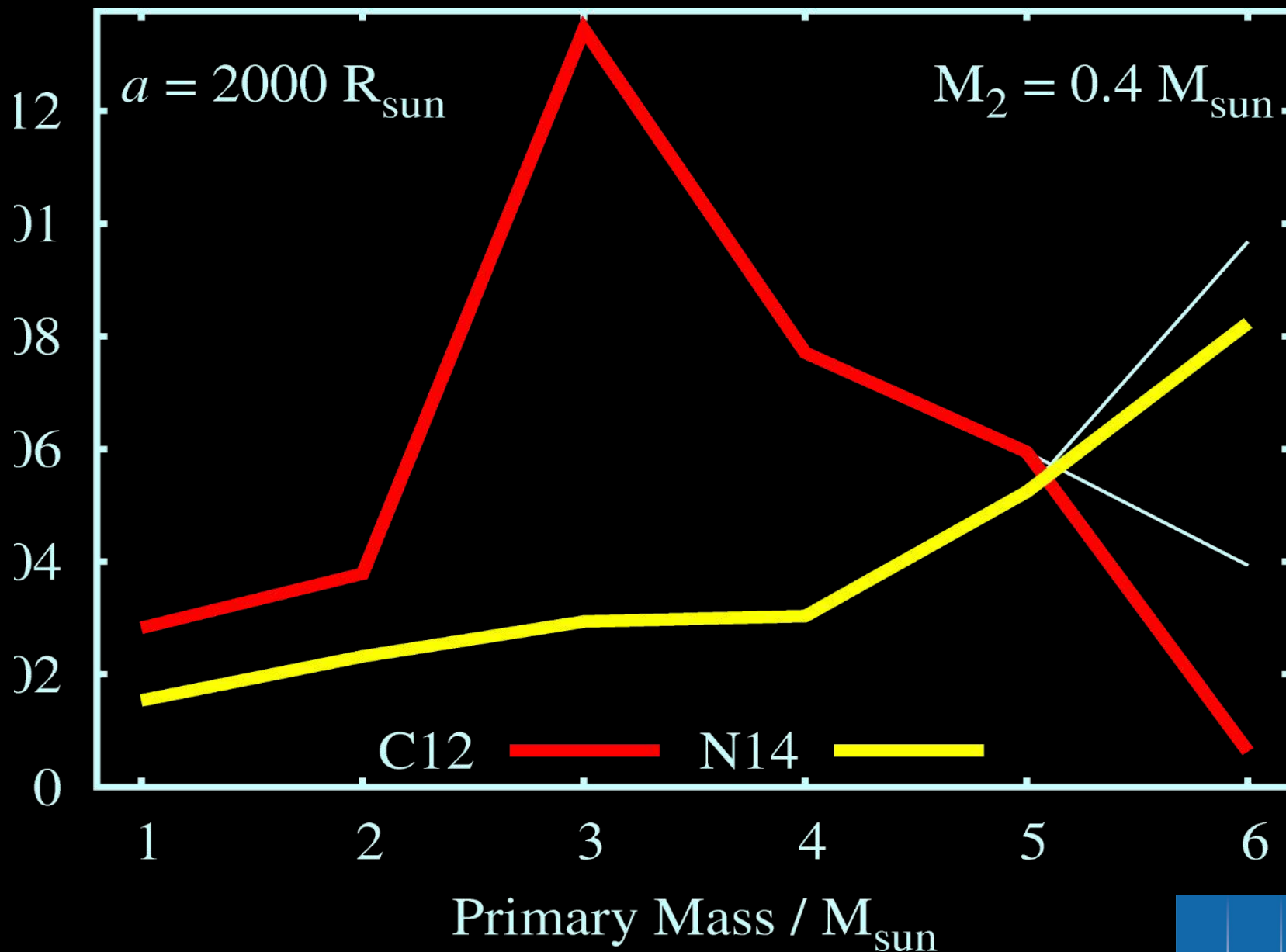
# Also RLOF if close enough



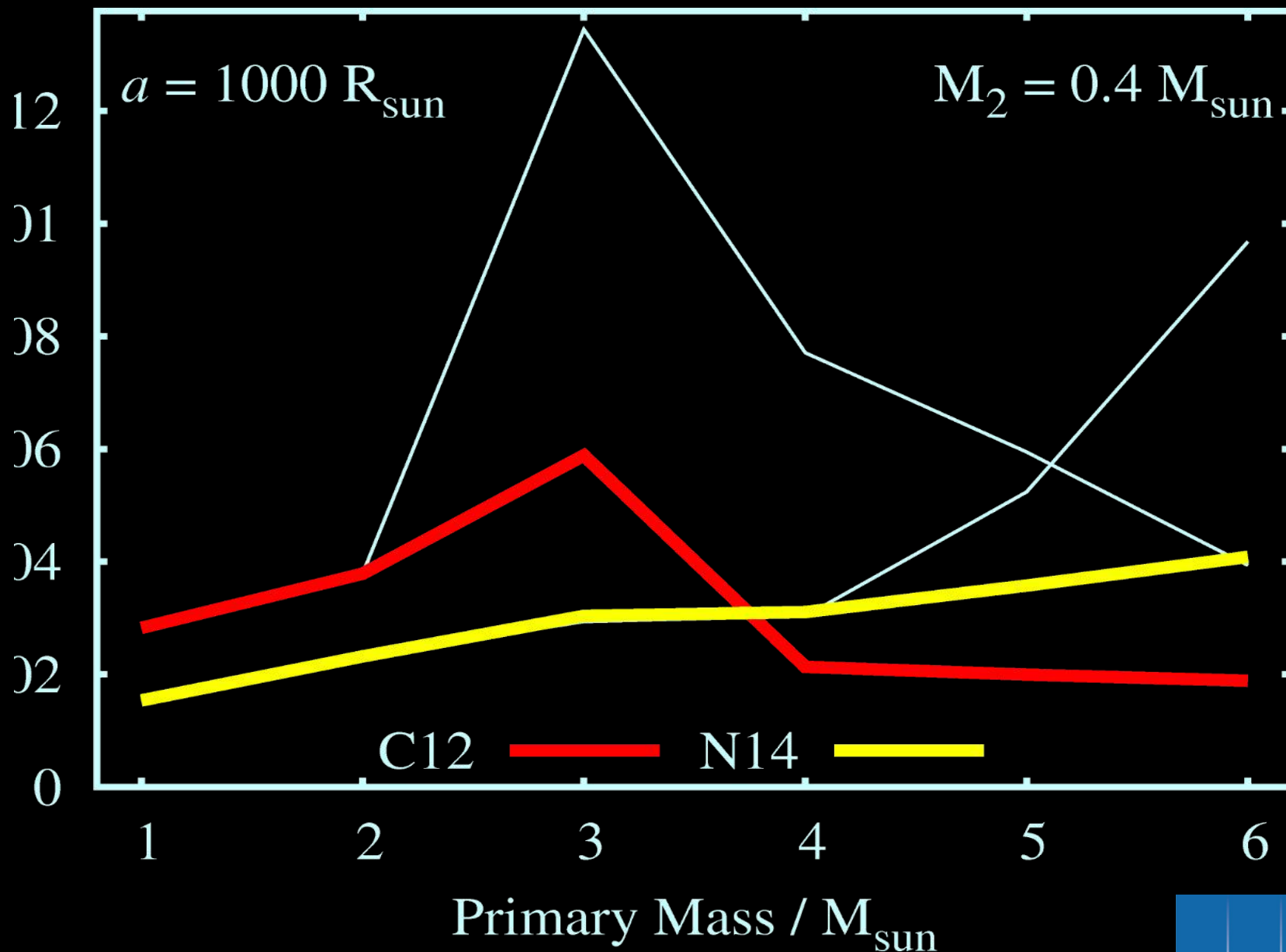
# Wider systems: barium/CH stars



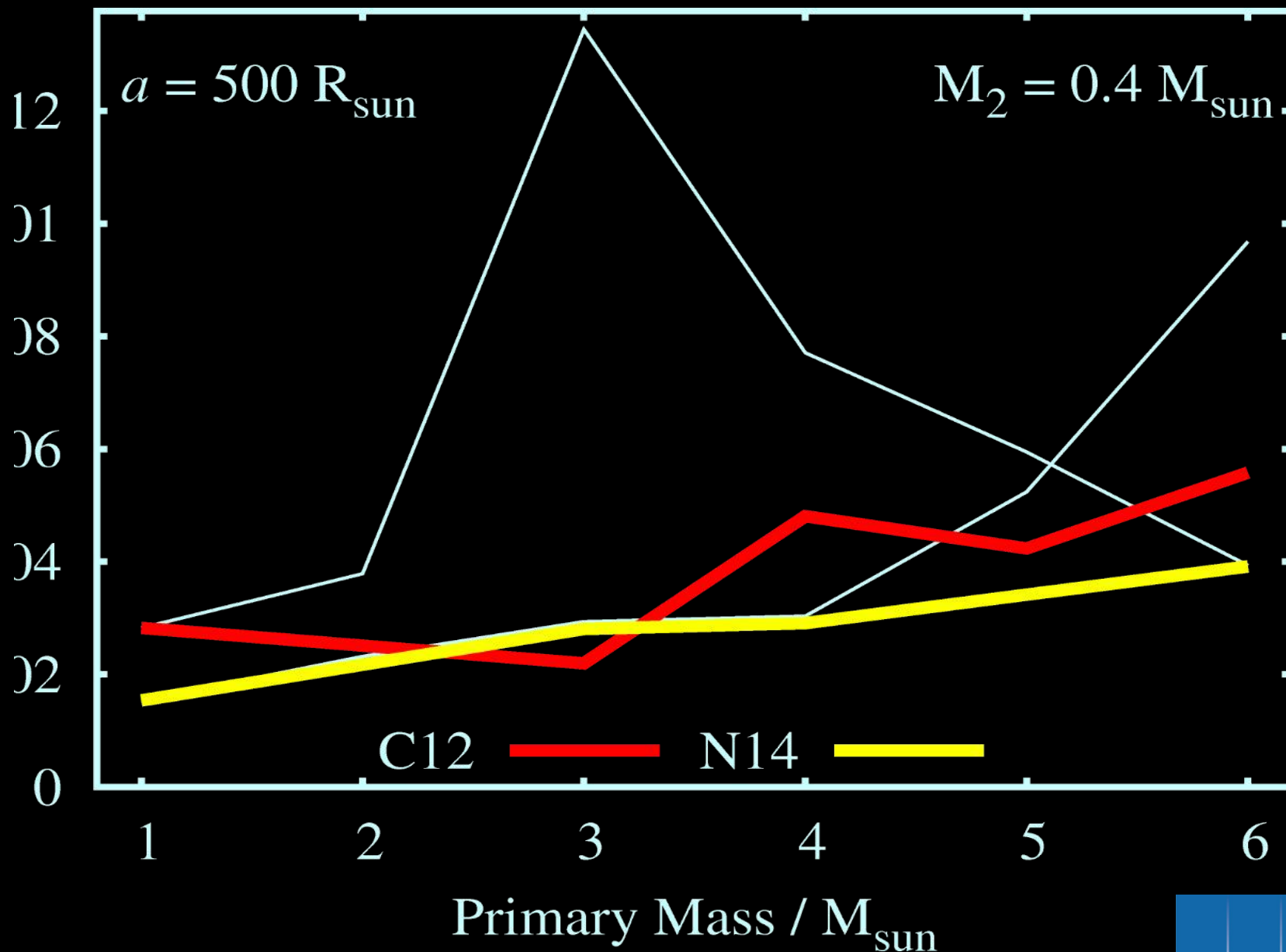
# Wider systems: barium/CH stars



# Wider systems: barium/CH stars

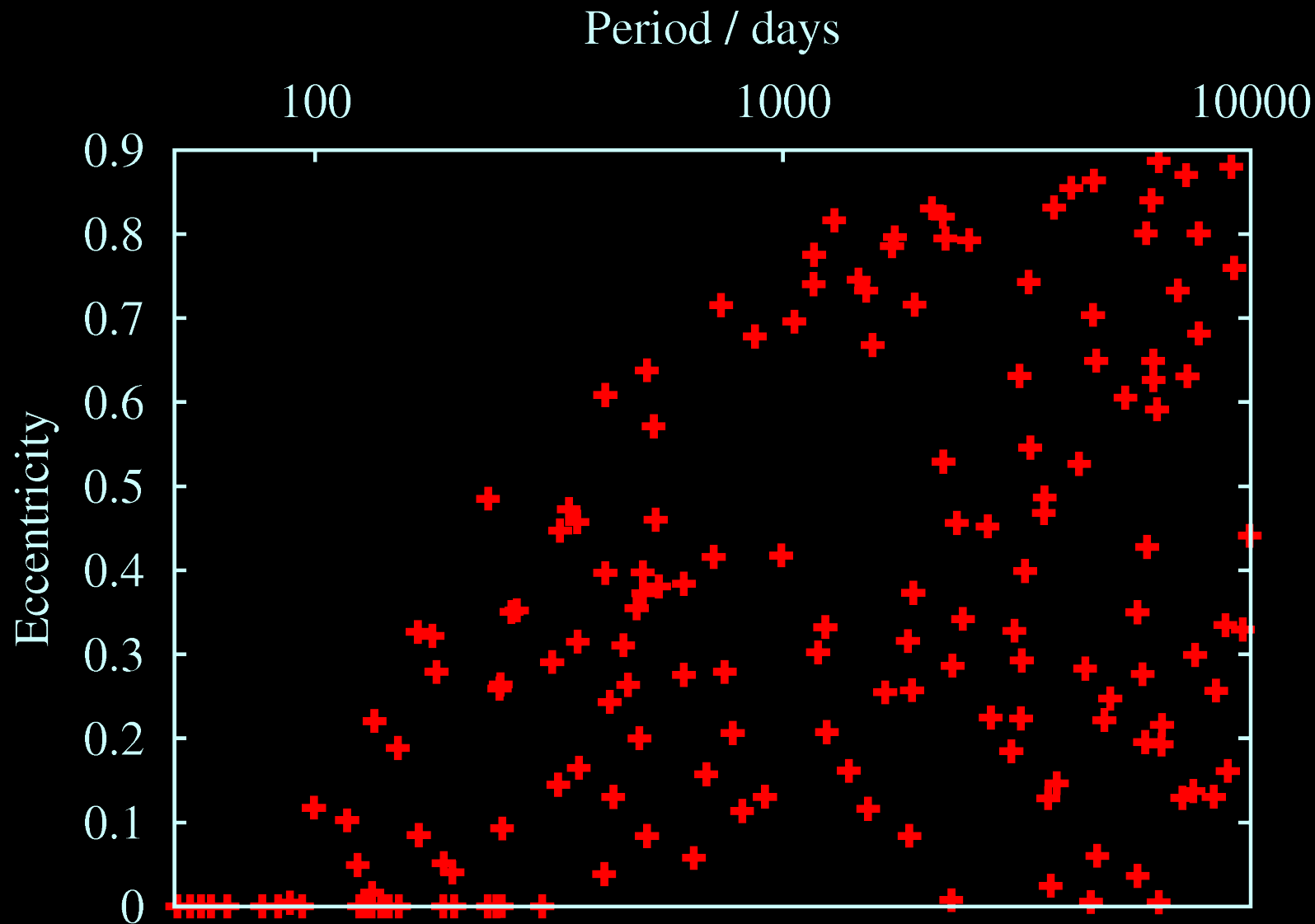


# Wider systems: barium/CH stars

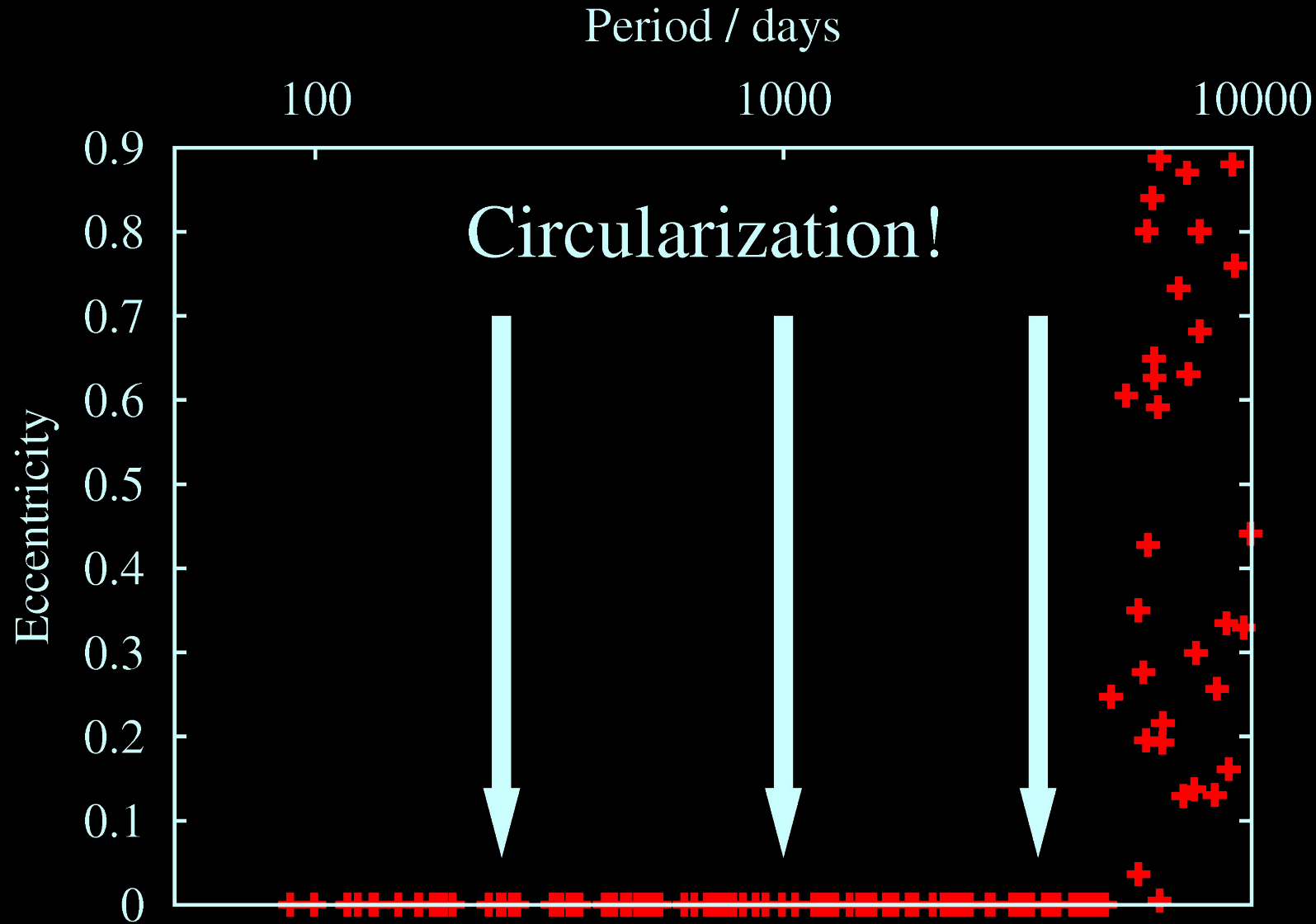




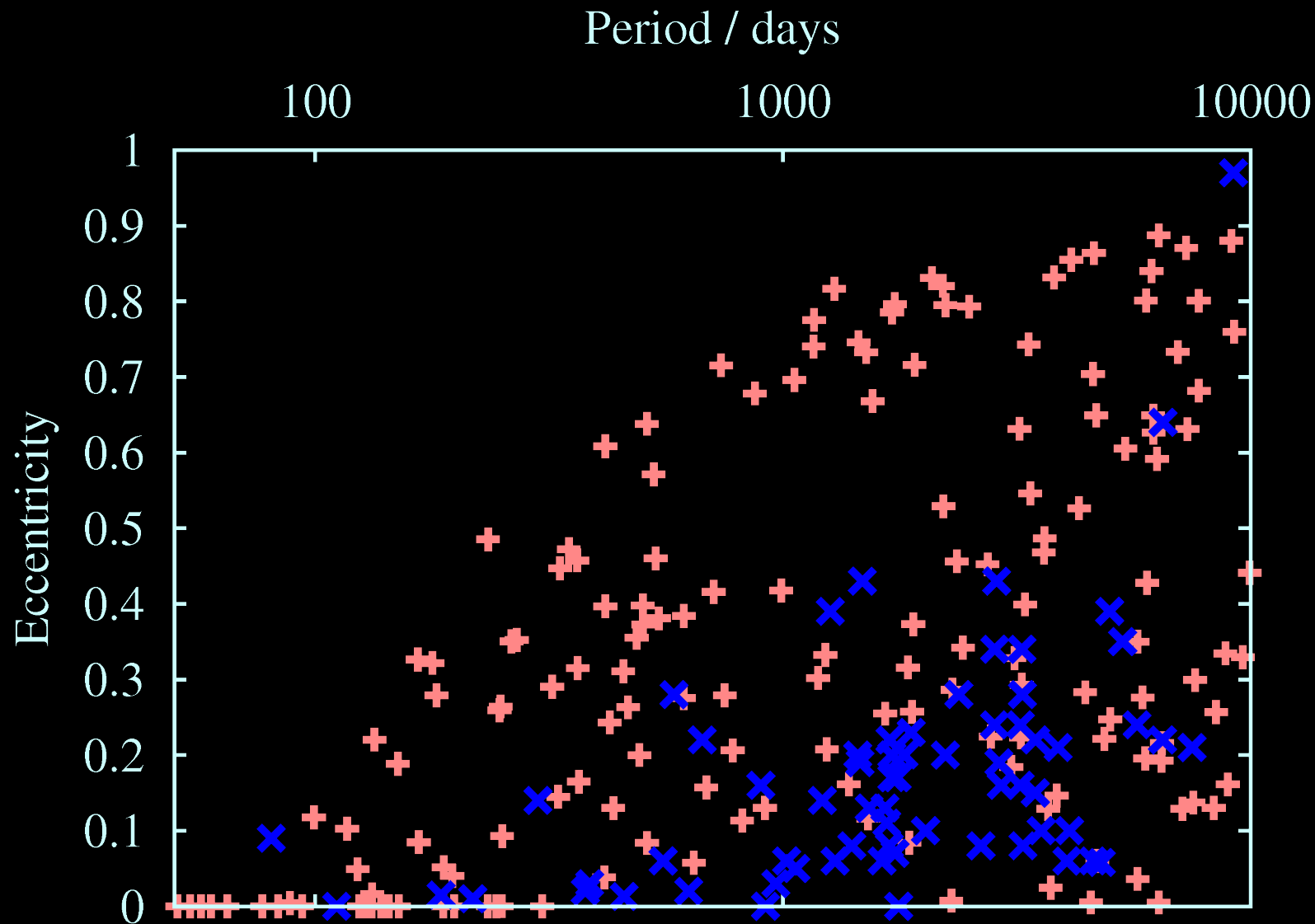
# Barium Stars and eccentricity



# Barium Stars and eccentricity



# Barium Stars and eccentricity



# Thermohaline mixing

- *What happens to material that accretes?*
- *In general it comes from an evolved star i.e. one in which  $\text{H} \rightarrow \text{He}$ ,  $\text{C, N, O} \rightarrow \sim 98\% \text{N}$  etc.*

- *i.e. the molecular weight is larger*

$$\rho = n \times m_{\text{H}} \times \mu$$

$$\mu = \frac{4}{6X + Y + 2}$$

- *Unstable to thermohaline instability*
- *See e.g. <https://secure.wikimedia.org/wikipedia/en/wiki/Thermohaline>*

# Thermohaline in ink

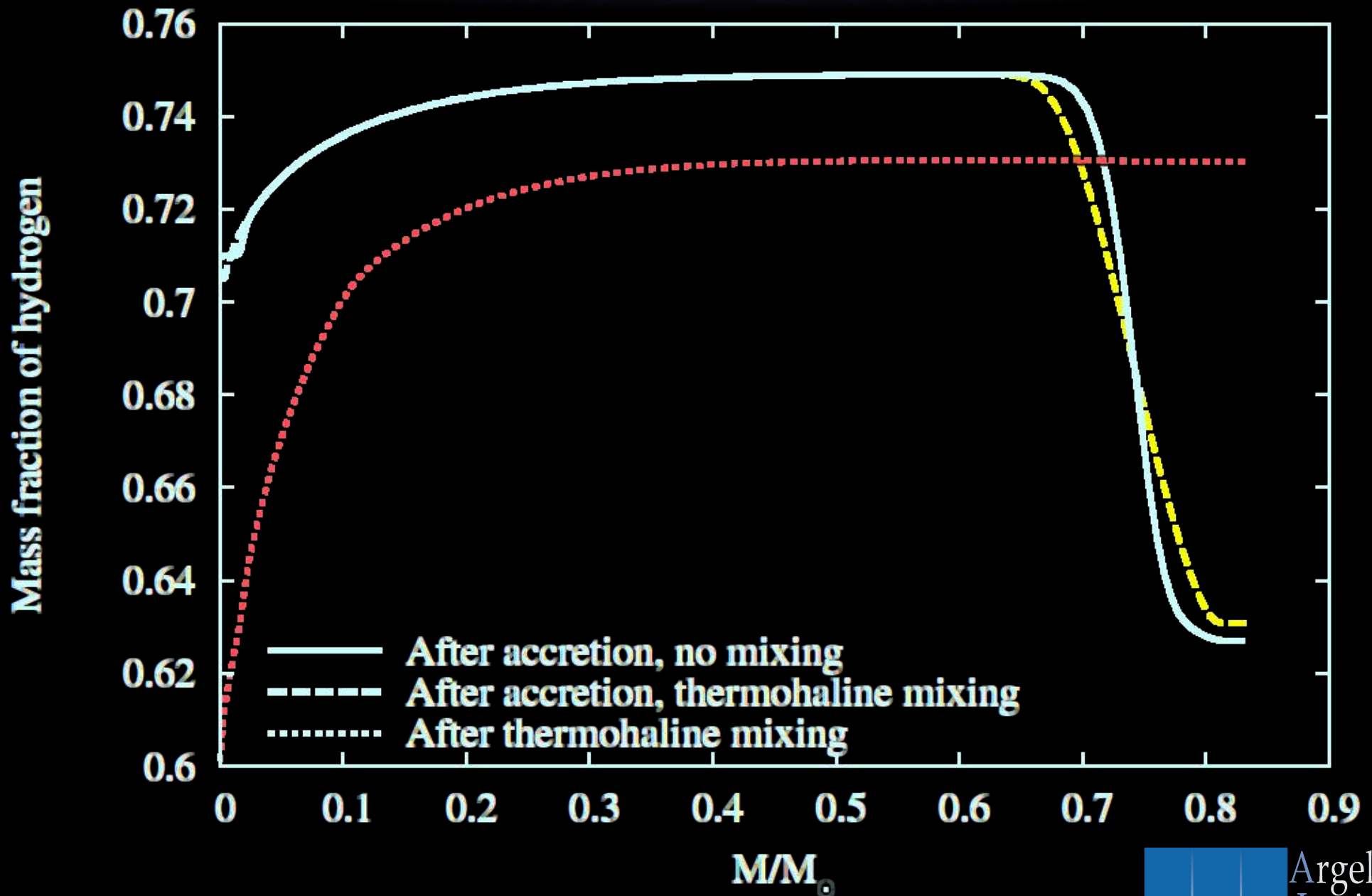


# Thermohaline in stars

- Relies on thermal transport so instability occurs on thermal timescales (i.e. fast c.f.  $\tau_{\text{th}}$ )
- Kippenhahn et al. 1998: diffusion model

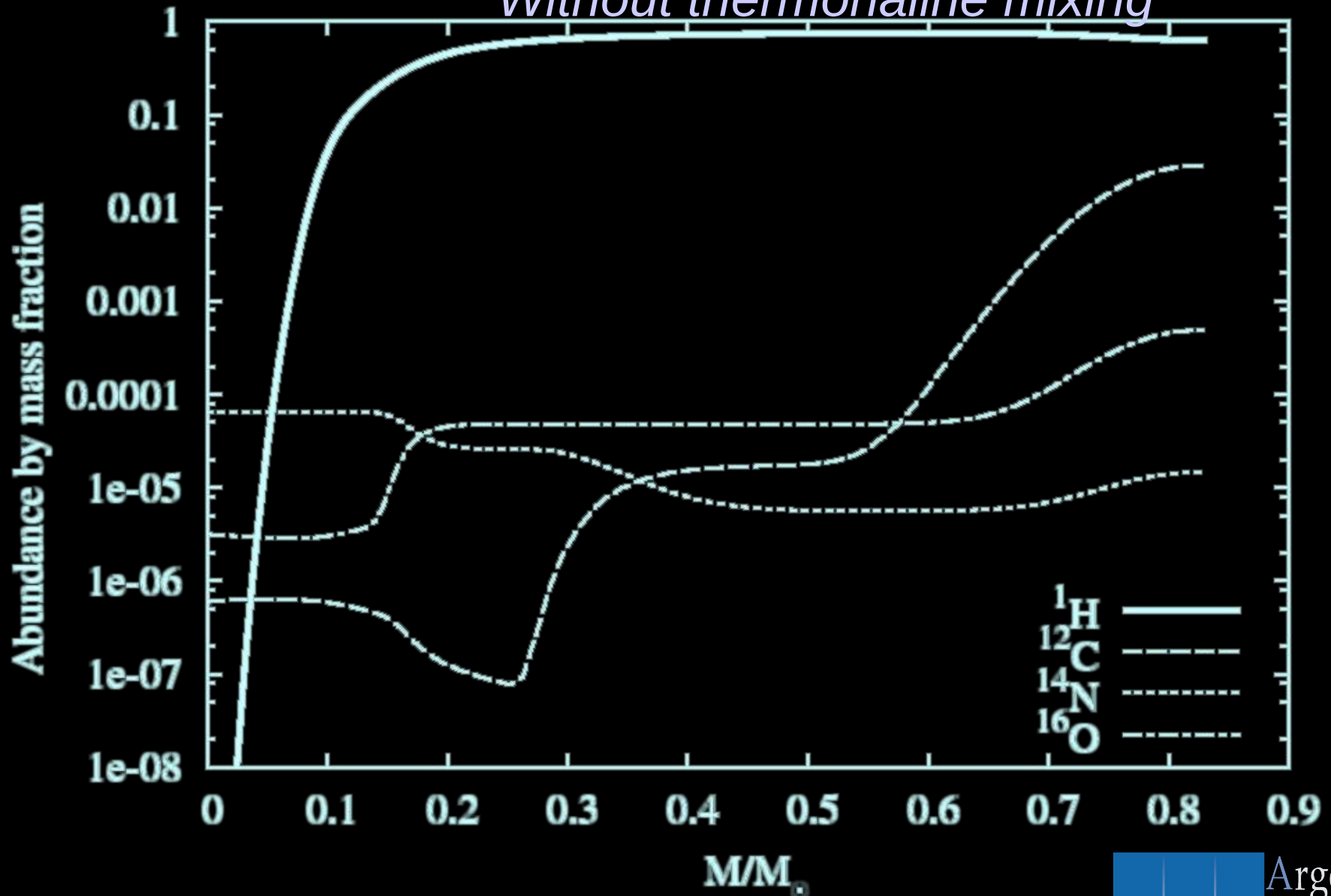
$$D_{\text{th}} = \frac{16acT^3 H_{\text{P}}}{(\nabla_{\text{ad}} - \nabla) c_{\text{P}} \rho \kappa} \left| \frac{d\mu}{dr} \right| \frac{1}{\mu}$$

# Thermohaline example



# CEMP star: $[C/Fe]=3.25$

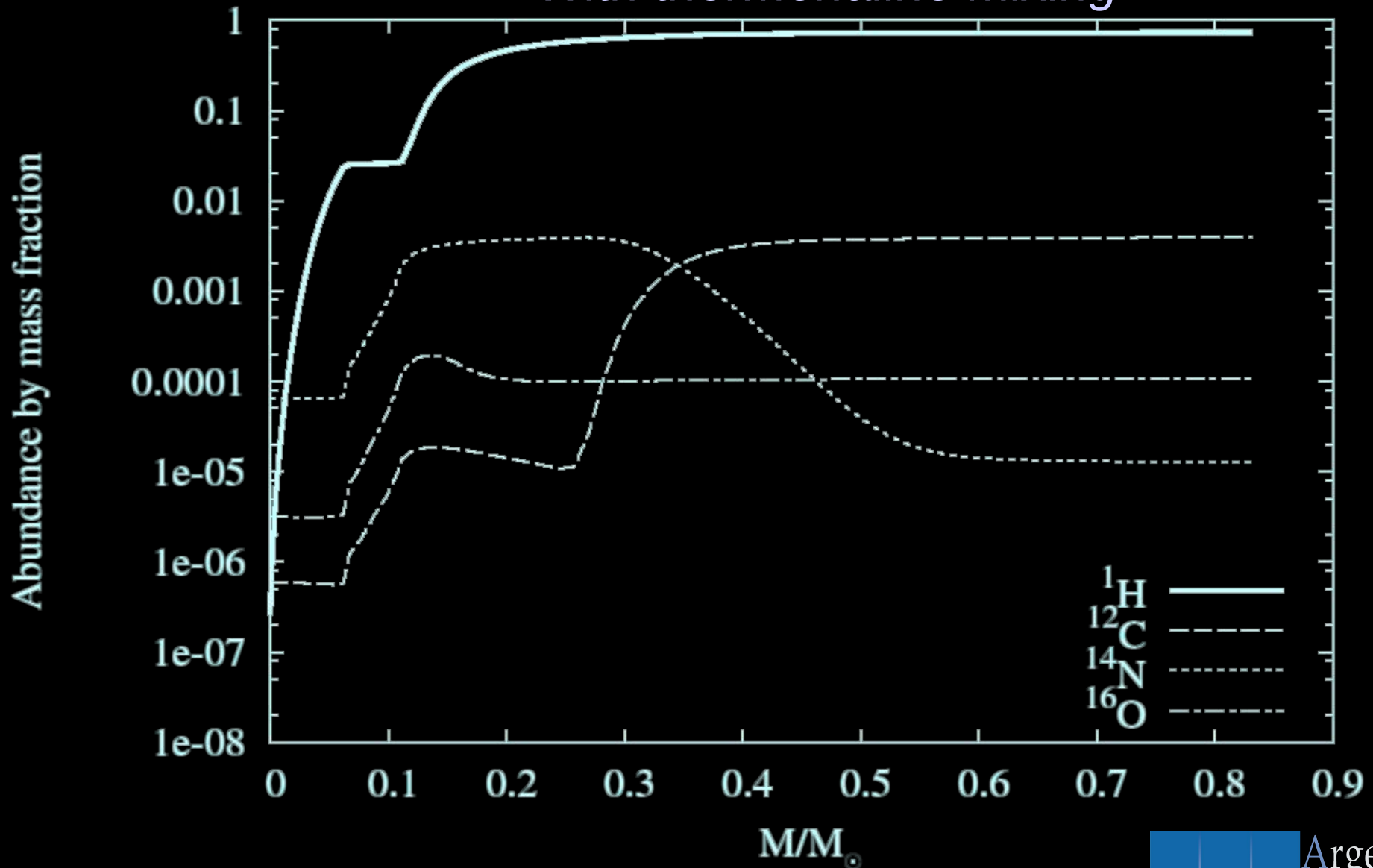
*Without thermohaline mixing*



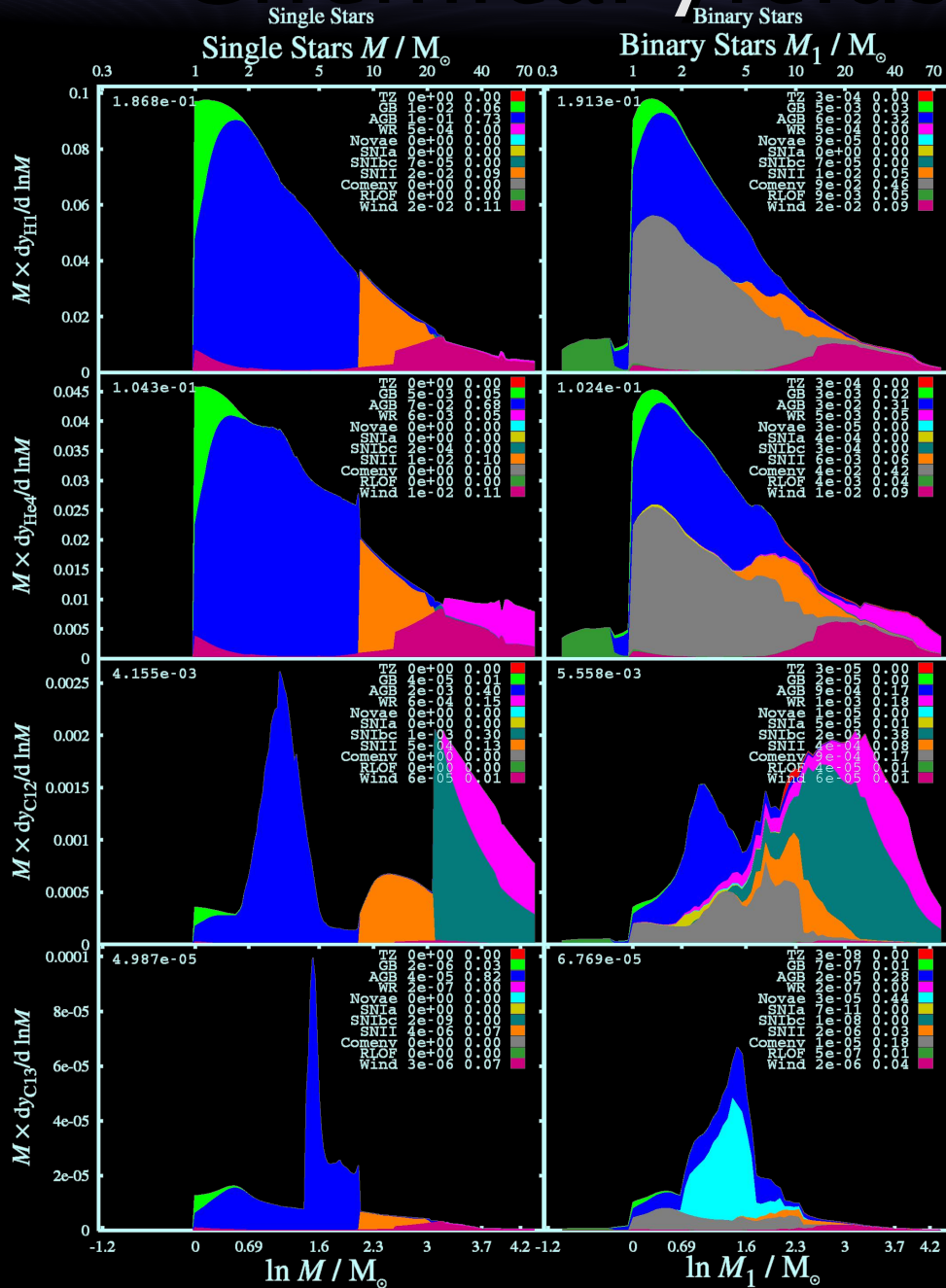


# CEMP star: $[C/Fe]=2.41$

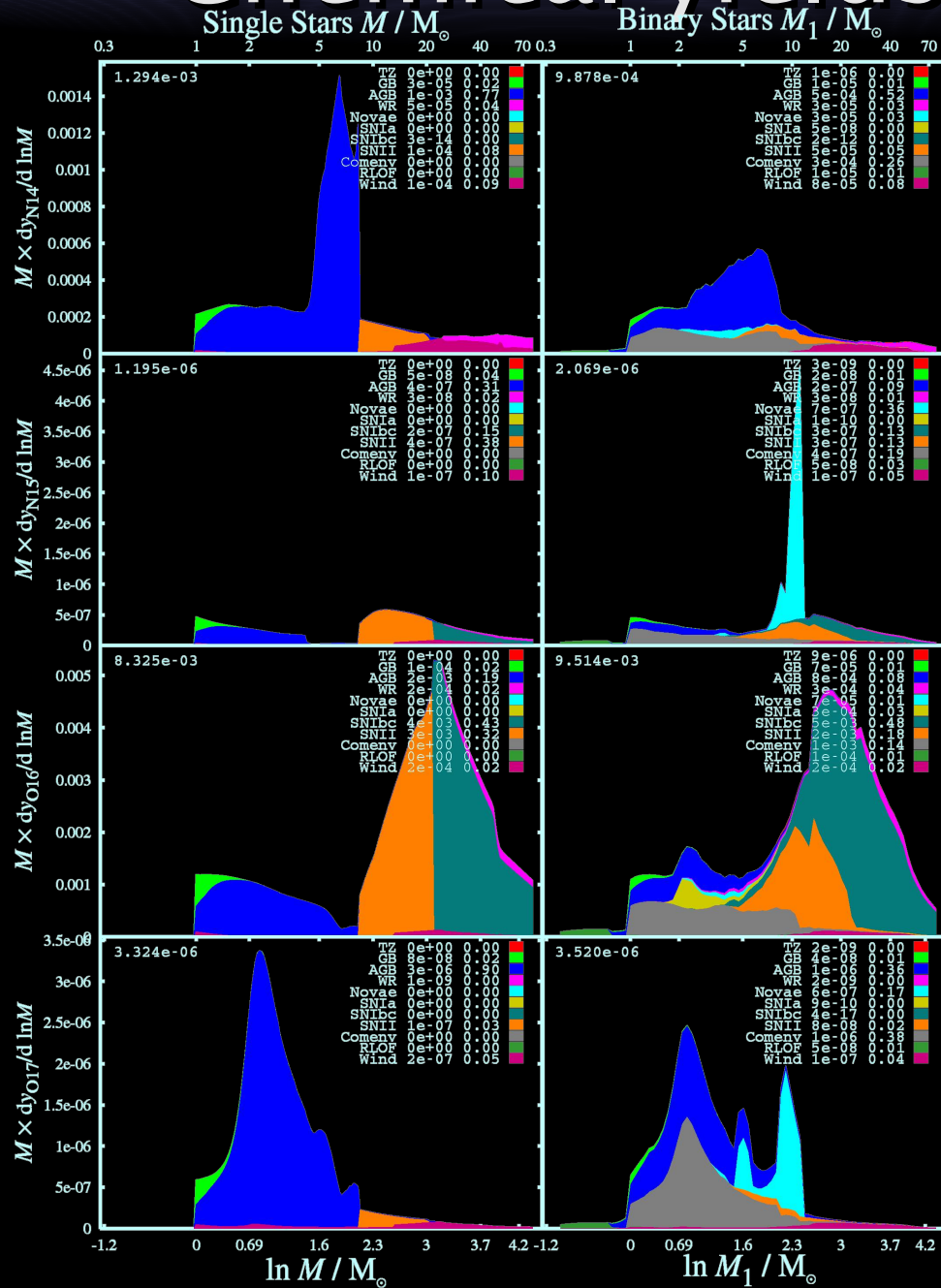
*With thermohaline mixing*



# Chemical yields



# Chemical yields



# Part 2: Modelling Binary Stars

- Traditional stellar models
- Rapid stellar codes
- Population synthesis
- Parameter space and initial distributions
- Stellar accountancy
- Examples of the power of population synthesis



# Traditional stellar modelling

- Stellar structure equations

$$\frac{dP}{dm} = -\frac{Gm}{4\pi r^4} \quad \frac{dL}{dm} = \epsilon$$

$$\frac{dr}{dm} = \frac{1}{4\pi r^2 \rho} \quad \frac{dT}{dm} = -\frac{3}{4ac} \frac{\kappa}{T^3} \frac{F}{(4\pi r^2)^2}$$

- Stiff equations
- Solving them is CPU expensive

# Discretisation

- Simplest case: mass conservation

$$dm = 4\pi\rho r^2 \times dr$$

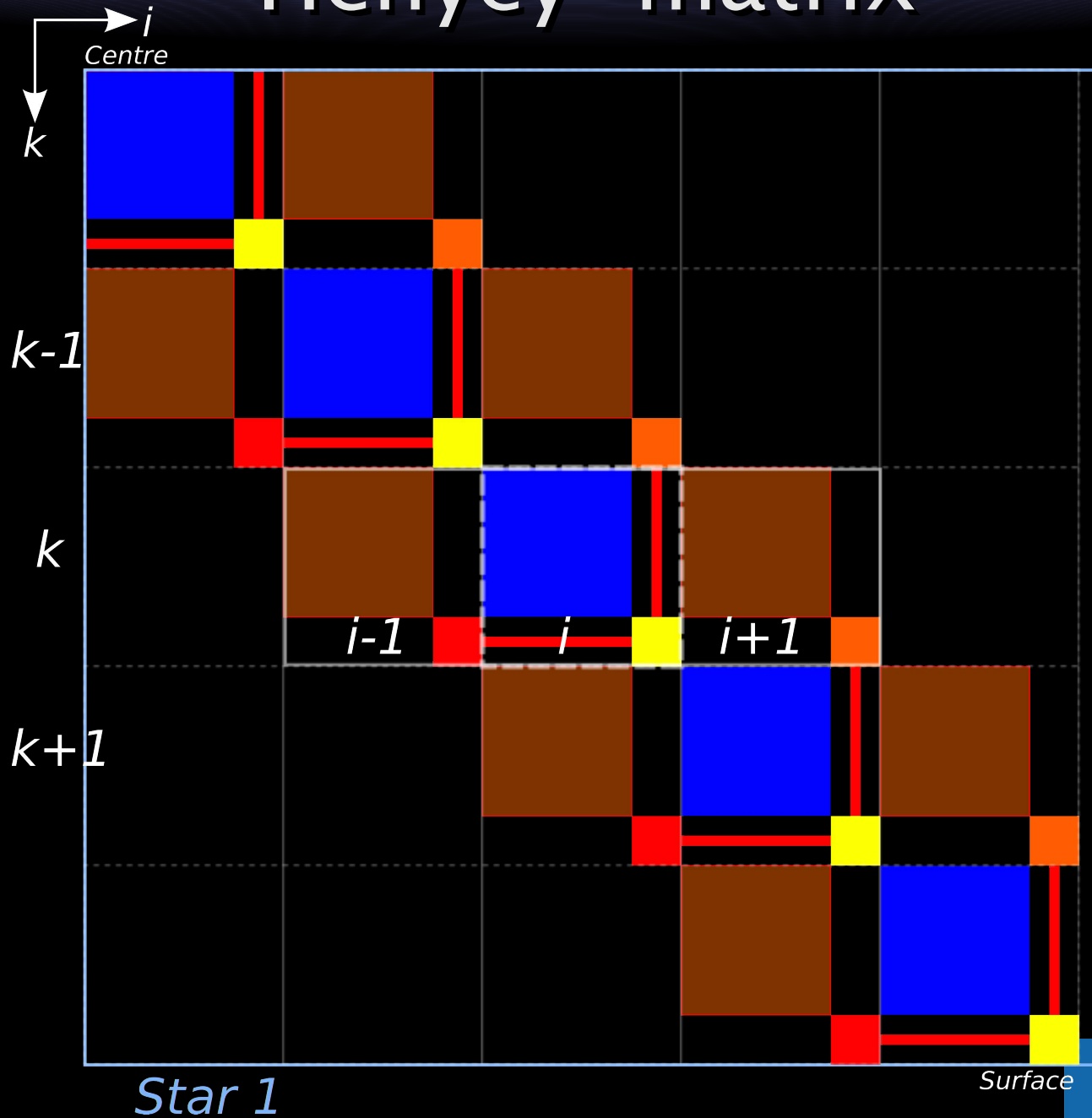
- A possible discretisation:

$$M_{i+1} - M_i = \frac{4\pi}{3} \rho_{i+\frac{1}{2}} [r_{i+1}^3 - r_i^3]$$

- Repeat for other equations/variables

$$T, P, r \text{ and } \ln f \text{ (degeneracy)}$$

# "Henyey" matrix



# Detailed code runtimes

- Say we want  $N$  timesteps
- These take  $\Delta t$  per timestep
- Total runtime per star

- $t_{\text{CPU}} \sim N \Delta t$
- $\frac{\tau}{\delta t} \Delta t$

- Typically (for an AGB star):

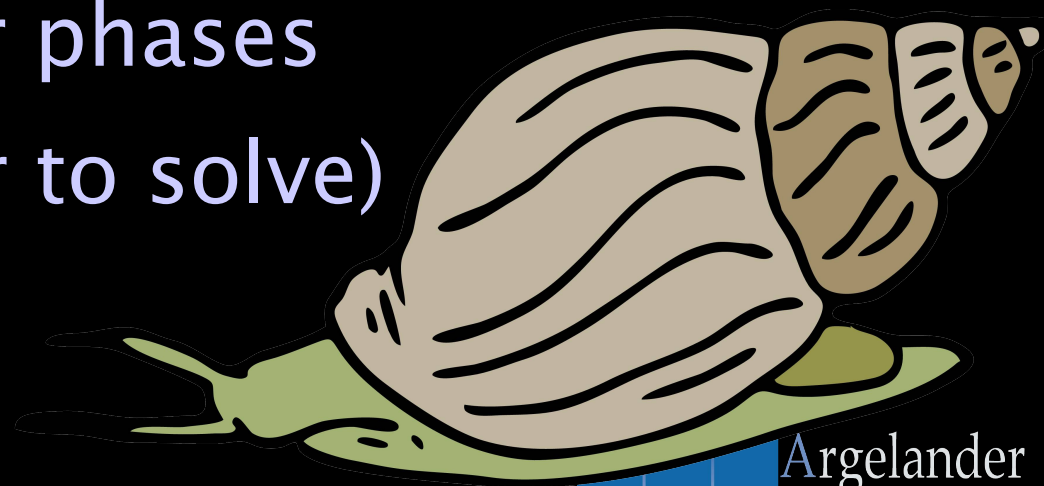
$$\tau \sim 1 \text{ Myr} \quad \delta t \sim 1 \text{ year} \quad \Delta t \sim 10 \text{ s}$$

$$t_{\text{CPU}} \sim 10^7 \text{ s}$$

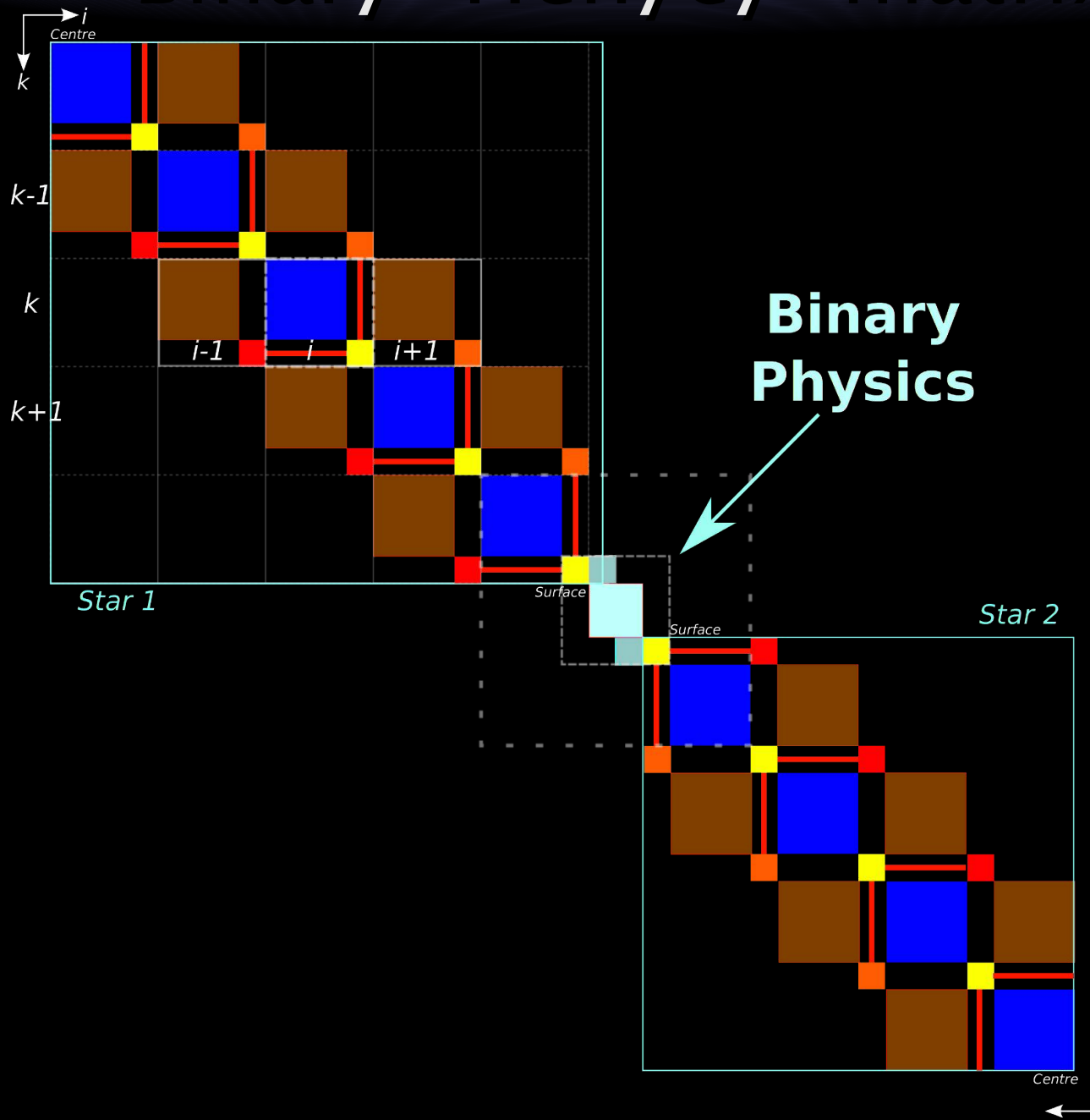


# Binary Star Equations

- Twice everything in a single star model
- Binary interaction equations (2, 3, more?)
- Runtime *at least*
- $t_{\text{CPU}}(\text{binary}) \gtrsim 2 \times t_{\text{CPU}}(\text{single})$
- Will be even more in complicated mass-transfer phases
- Bigger matrix (slower to solve)

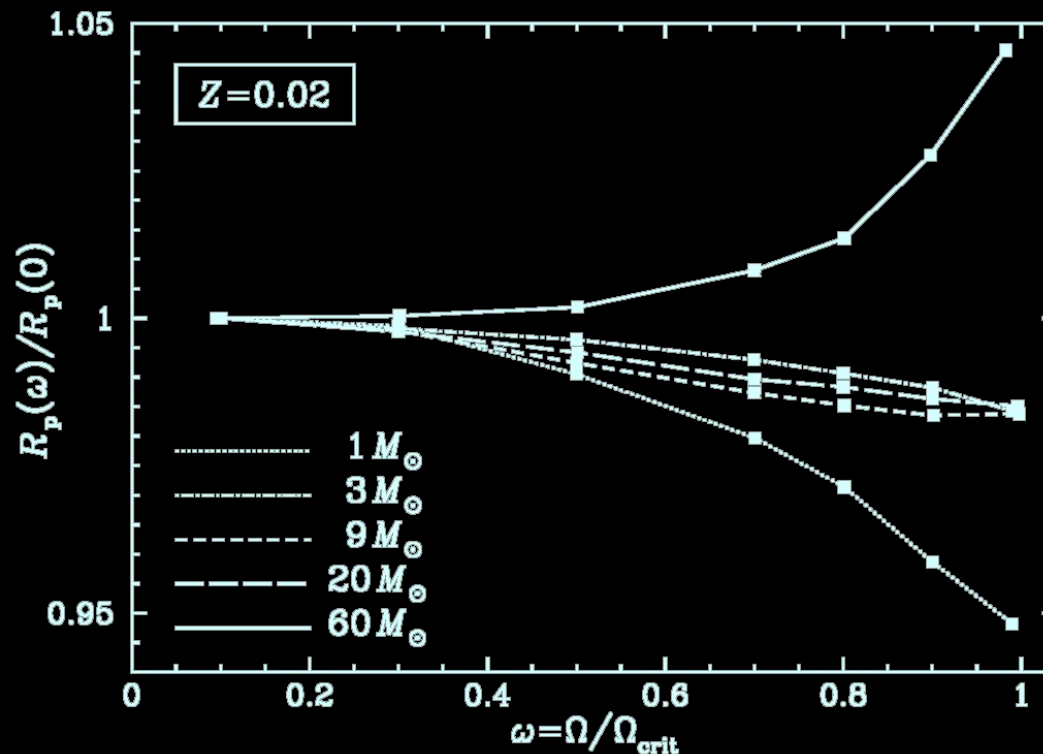


# Binary "Henye" matrix



## An aside: dimensions of rotating stars

- Can we treat stars as essentially *single stars*?
- Polar radius is approx const.



Ekstrom et al  
2008 A&A  
478, 467

Variations in the polar radius as a function of the ratio  $\omega = \Omega/\Omega_{\text{crit}}$ , normalized to the non-rotating value, for various masses at standard metallicity.

# Rapid Stellar Models

- Creating *detailed* stellar models is slow and difficult
- Rapid or synthetic stellar models are faster
- Replace details solver with pre-solved model set:
  - Fitting formulae
  - Or lookup tables
- Sacrifice (usually unwanted) details for speed: up to 10,000,000 times faster.



# Fitting Formulae

- Eggleton, Fitchett, Tout 1989, Hurley et al 2000,2002
- Zero-age main sequence:

$$L_0 = \begin{cases} \frac{1.107M^3 + 240.7M^9}{1 + 281.9M^4} & M \leq 1.093 \\ \frac{13990M^5}{M^4 + 2151M^2 + 3908M + 9536} & M \geq 1.093 \end{cases}$$

$$R_0 = \begin{cases} \frac{0.1148M^{1.25} + 0.8604M^{3.25}}{0.04651 + M^2} & M \leq 1.334 \\ \frac{1.968M^{2.887} - 0.7388M^{1.679}}{1.821M^{2.337} - 1} & M \geq 1.334 \end{cases}$$

# Fitting Formulae

- Time evolution function of  $\tau = t/t_{\text{MS}}$

$$t_{\text{MS}} = \frac{2550 + 669M^{2.5} + M^{4.5}}{0.0327M^{1.5} + 0.346M^{4.5}} .$$

- Then

$$\log_{10} L = \log_{10} L_0 + \alpha\tau_{\text{MS}} + \beta\tau_{\text{MS}}^2$$

$$\log_{10} R = \log_{10} R_0 + \alpha'\tau_{\text{MS}} + \beta'\tau_{\text{MS}} + \gamma'\tau_{\text{MS}}^3$$

# Fitting formulae

$$\alpha = \begin{cases} 0.2594 + 0.1348 \log_{10} M & M \leq 1.334 \\ 0.09209 + 0.05934 \log_{10} M & M > 1.334 \end{cases}$$

$$\beta = \begin{cases} 0.144 - 0.833 \log_{10} M & M \leq 1.334 \\ 0.3756 \log_{10} M - 0.1744 (\log_{10} M)^2 & M > 1.334 \end{cases}$$

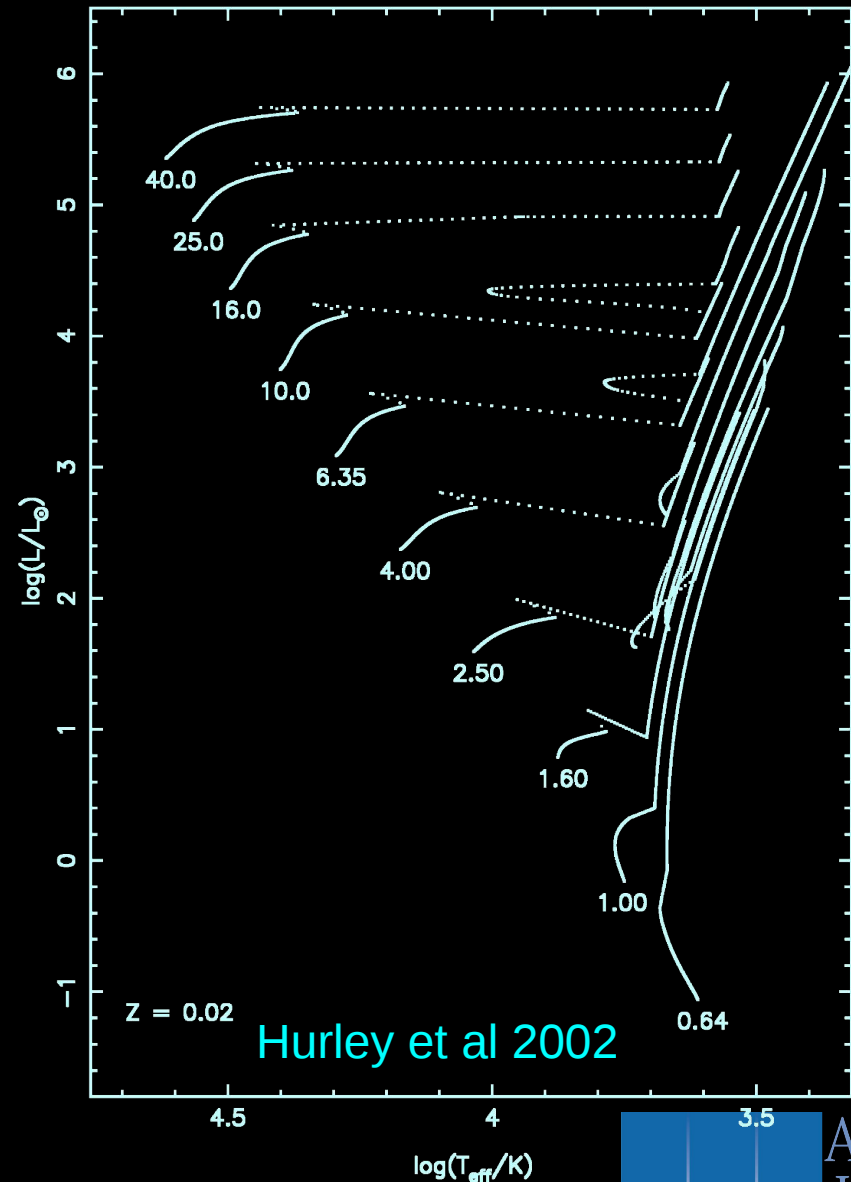
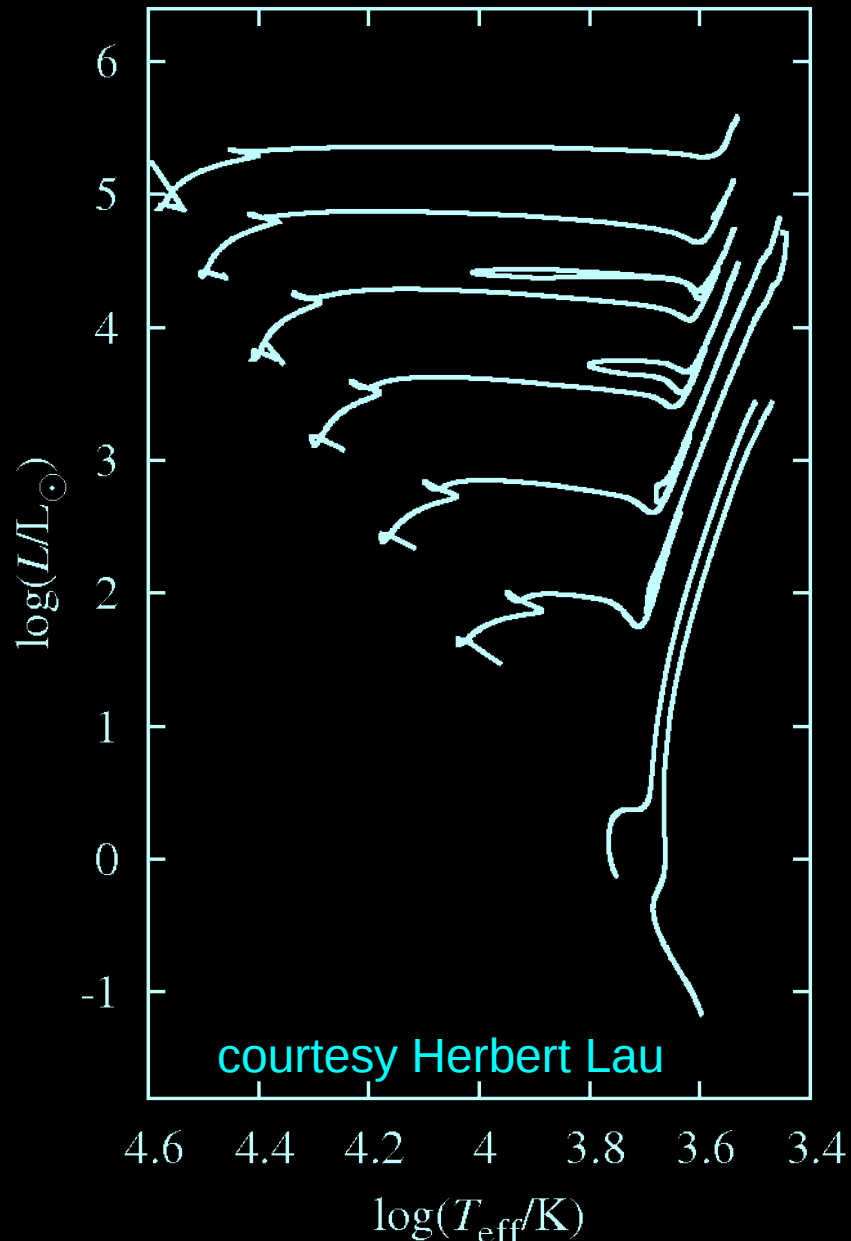
$$\alpha' = \begin{cases} 0 & M \leq 1.334 \\ 0.1509 + 0.1709 \log_{10} M & M > 1.334 \end{cases}$$

$$\beta' = \begin{cases} 0.2226 \log_{10} M & M \leq 1.334 \\ -0.4805 \log_{10} M & M > 1.334 \end{cases}$$

$$\gamma' = \begin{cases} 0.1151 & M \leq 1.334 \\ 0.5083 \log_{10} M & M > 1.334 \end{cases} .$$

Even more complicated formulae apply for later phases of evolution!  
But computers *do not care* ...

# Real vs Synthetic HRD





# Pros and Cons

## ■ Pros

- Faster to compute
- Stable

$$\log_{10} L = \log_{10} L_0 + \alpha \tau_{\text{MS}} + \beta \tau_{\text{MS}}^2$$

$$\log_{10} R = \log_{10} R_0 + \alpha' \tau_{\text{MS}} + \beta' \tau_{\text{MS}} + \gamma' \tau_{\text{MS}}^3$$

## ■ Cons

- Fixed input physics (but could use tables!)
- Discard of potentially useful information
- Off-grid treatment
- Fitting errors (<5%)

# Population Synthesis

*The process of combining stellar models into a stellar population upon which meaningful statistical analysis can be performed and compared to observations to better constrain the underlying physics.*

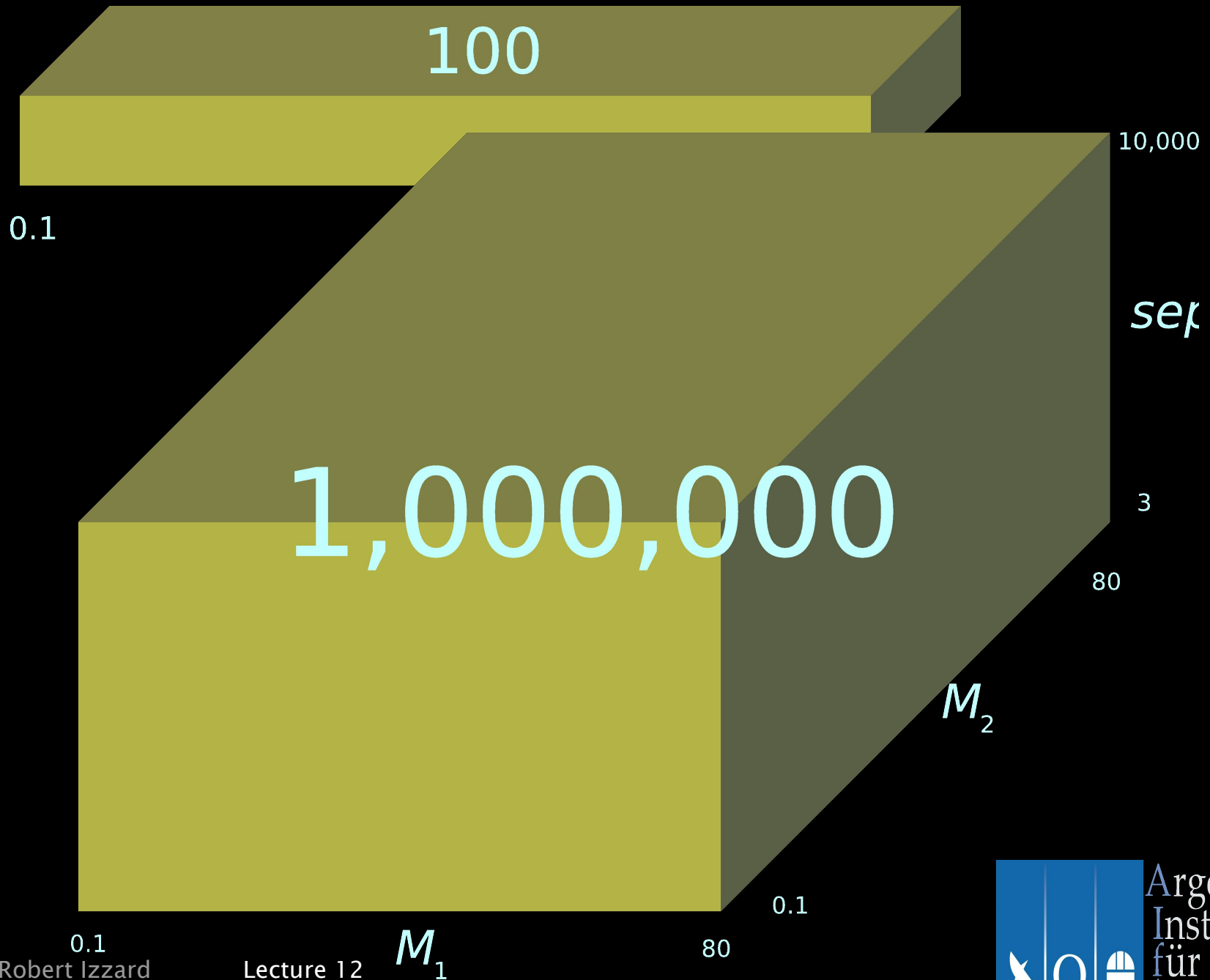
1. Make your stellar models
2. Weight these according to mass, separation, time etc.
3. Extract simulated value(s)–compare
4. Determine the “real–life” distribution from obs.
5. Compare the two, see what's wrong
6. Refine your stellar models
7. Return to step 1 until you are happy

(or funding runs out)

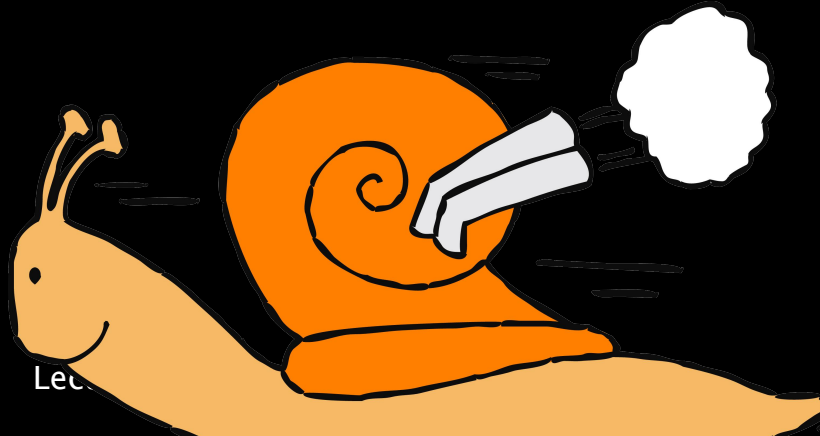
# The Parameter Space Problem

- To make a single star population, one parameter only: Mass  $M_1$
- Runtime is  $\sim N \times \Delta t$
- Binaries many parameters :
  - Primary mass  $M_1$
  - Secondary mass  $M_2$
  - Sep/Period  $a$  or  $P$
  - Maybe more e.g.  $e$
- Runtime  $\sim N^3 \times \Delta t$

# Parameter Spaces



# Popsyn + rapid code



# Discretising Parameter Space

- *Single Stars*

$$\delta \ln M = \frac{\ln M_{\max} - \ln M_{\min}}{n}$$

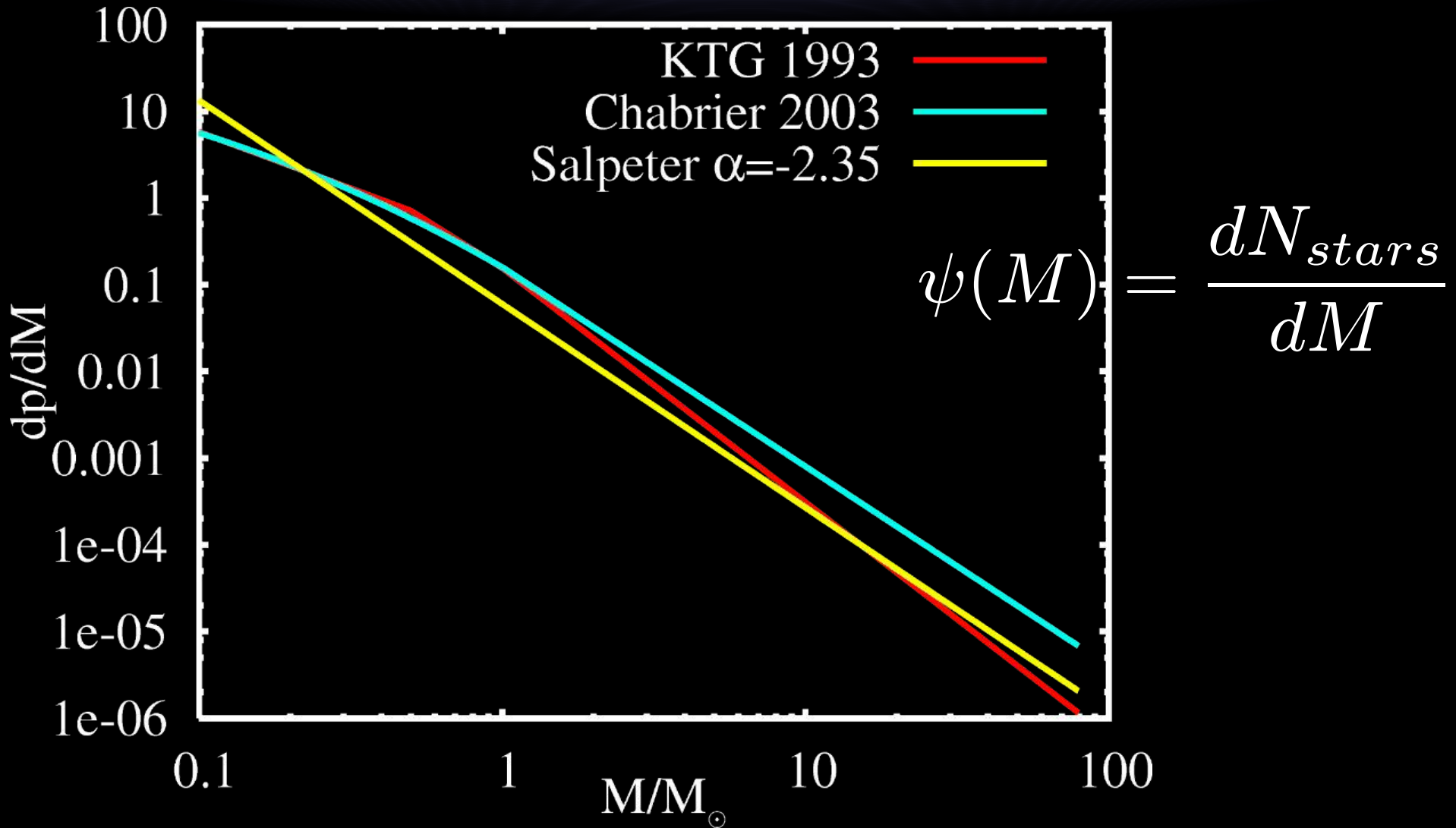
- *Each star has a probability of existence*

$$\delta p_i = \psi(M_i) \delta \ln M$$

- *Where  $\psi$  is the initial mass function*

$$\sum_i \delta p_i = 1$$

# IMF



Salpeter IMF  $\psi \propto M^{-2.35}$

# Discretising Parameter Space

- *Binary Stars*

$$\delta \ln x = \frac{\ln x_{\max} - \ln x_{\min}}{n_x}$$

where  $x$  is  $M_1, M_2, a(, P, e\dots)$

- *Each star has a probability of existence*

$$\delta p_i = \Psi_i(M_1, M_2, a) \delta V$$

- *Where  $\Psi$  is the initial distribution function*



# Initial Distribution Function

$$\Psi_i = \psi(M_{1i}) \phi(M_{2i}/M_{1i}) \chi(a_i)$$

$$\psi(M_1) = \psi(M)$$

$$\phi\left(q = \frac{M_1}{M_2}\right) = \text{constant}$$

$$\chi(a) \propto a^{-1}$$

$$\chi(\ln a) = \text{constant}.$$

$$\delta p_i = \Psi_i \delta V_i$$

$$\delta V = \delta \ln M_1 \delta \ln M_2 \delta \ln a$$
$$\sum_i \delta p_i = 1$$

# Stellar accounts

- Define

$$\begin{aligned}\delta(\text{phase}) &= 1 && \text{during the phase,} \\ &= 0 && \text{otherwise.}\end{aligned}$$

- Time a star spends in a phase of interest

$$\Delta t_i = \sum_{t=t_{\min}}^{t_{\max}} \delta(\text{phase at } t)_i \delta t$$

# Stellar accounts

- The number of stars in the phase is

$$\begin{aligned}\text{count} &= \sum_i S \delta p_i \Delta t_i \\ &= \sum_i S \delta p_i \sum_{t_{\min}}^{t_{\max}} \delta(\text{phase})_i \delta t\end{aligned}$$

where  $S$  is the star formation rate

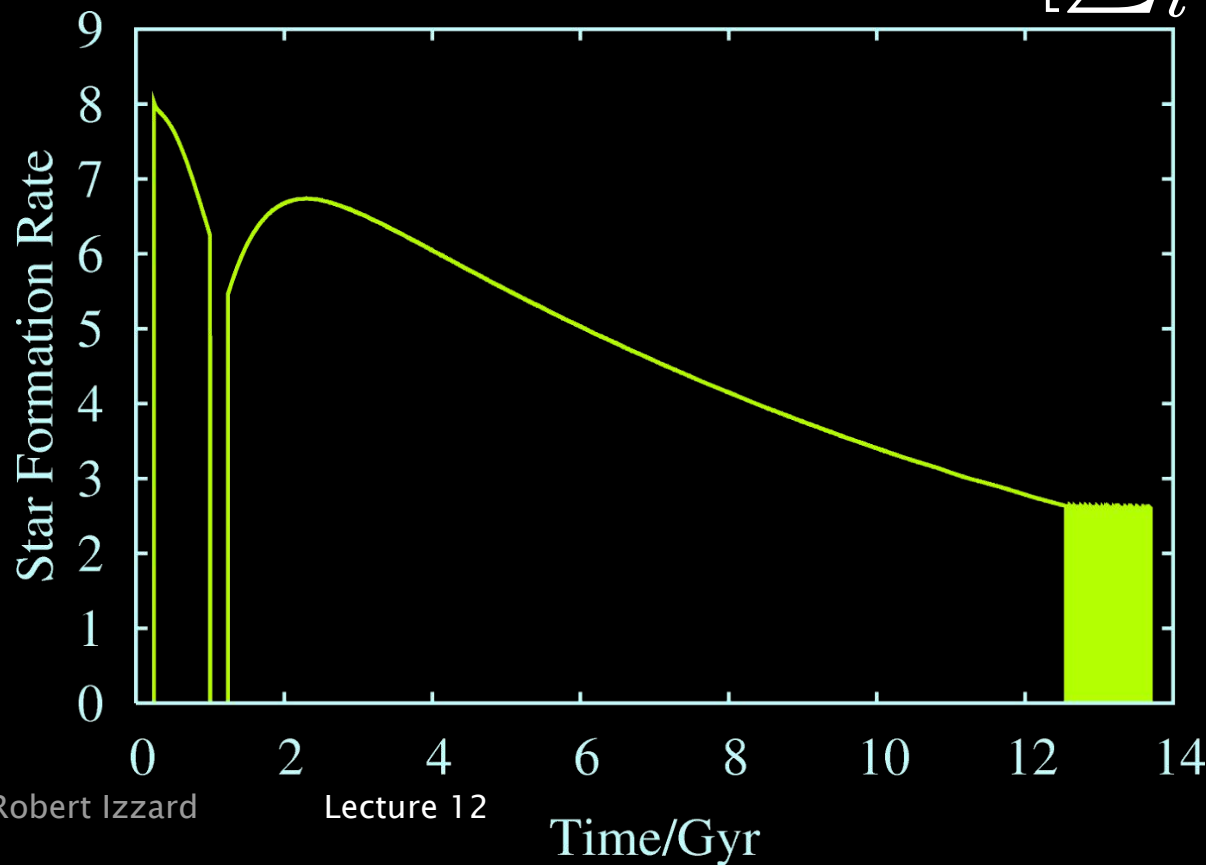
- In general we have to convolve a birth function with a star formation rate function

-

# Stellar accounts

- Simple case :  $S = \text{constant}$
- Divide counts to get ratios :  $S$  drops out

$$\text{ratio} = \frac{[\sum_i \delta p_i \Delta t_i]_1}{[\sum_i \delta p_i \Delta t_i]_2}.$$



Galactic SFR  
Chiappini et al 1997

# Stellar accounts

- The number of stars in the phase is

$$\sum_i S \delta p_i \Delta t_i$$

where  $S$  is the star formation rate

- In general we have to convolve a birth function with a star formation rate function

$$\sum_{t'_{\min}}^{t'_{\max}} \sum_i S(t) \delta p_i \delta(\text{phase at } t')_i \delta t'$$

# Compare to Observations

- Statistics!

- Boring (but not for everyone!)
- Necessary e.g.  $\chi^2$ , KS tests
- Key to good science

- Beware observational selection effects

- Often very hard to model
- Data combined from multiple surveys might be impossible to model!
- Sometimes whole papers are wrong because they neglect this!  
(not deliberately)

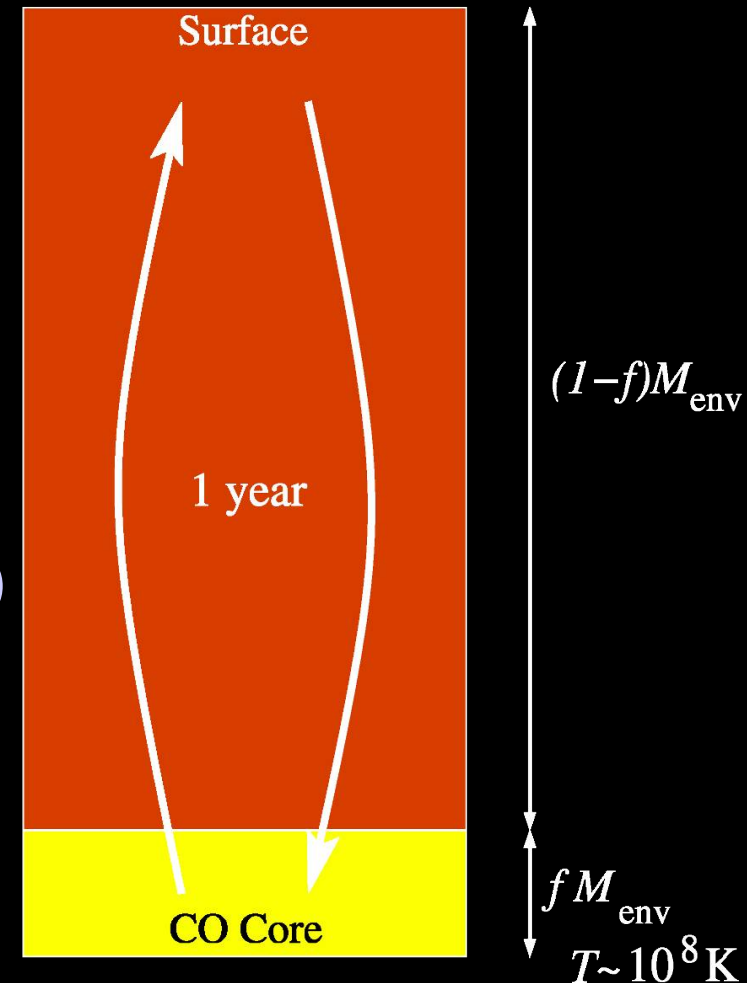


# A rapid code: *binary\_c*

- My code, my lectures, so ...
- Based on *SSE/BSE* of EFT89, Hurley et al 2000, 2002  
(e.g. see prev. eqs)
- Has fitting functions for stellar evolution
- +orbital algorithm: RLOF, Wind, Tides
- Common env., Novae, SNe Ia, Mergers etc.
- Online
- <http://www.astro.uni-bonn.de/~izzard/cgi-bin/binary3.cgi>

# *binary\_c/nucsyn*

- Added *nucleosynthesis* to *binary\_c*
- First and second dredge up
- TPAGB based on Karakas' models:
  - Third dredge up
  - Hot-bottom burning  
(CNO, NeNa, MgAl)
  - S-process (Torino group)
- SN II/Ibc yields, novae
- Thermohaline mixing
- Physics updates over last few years



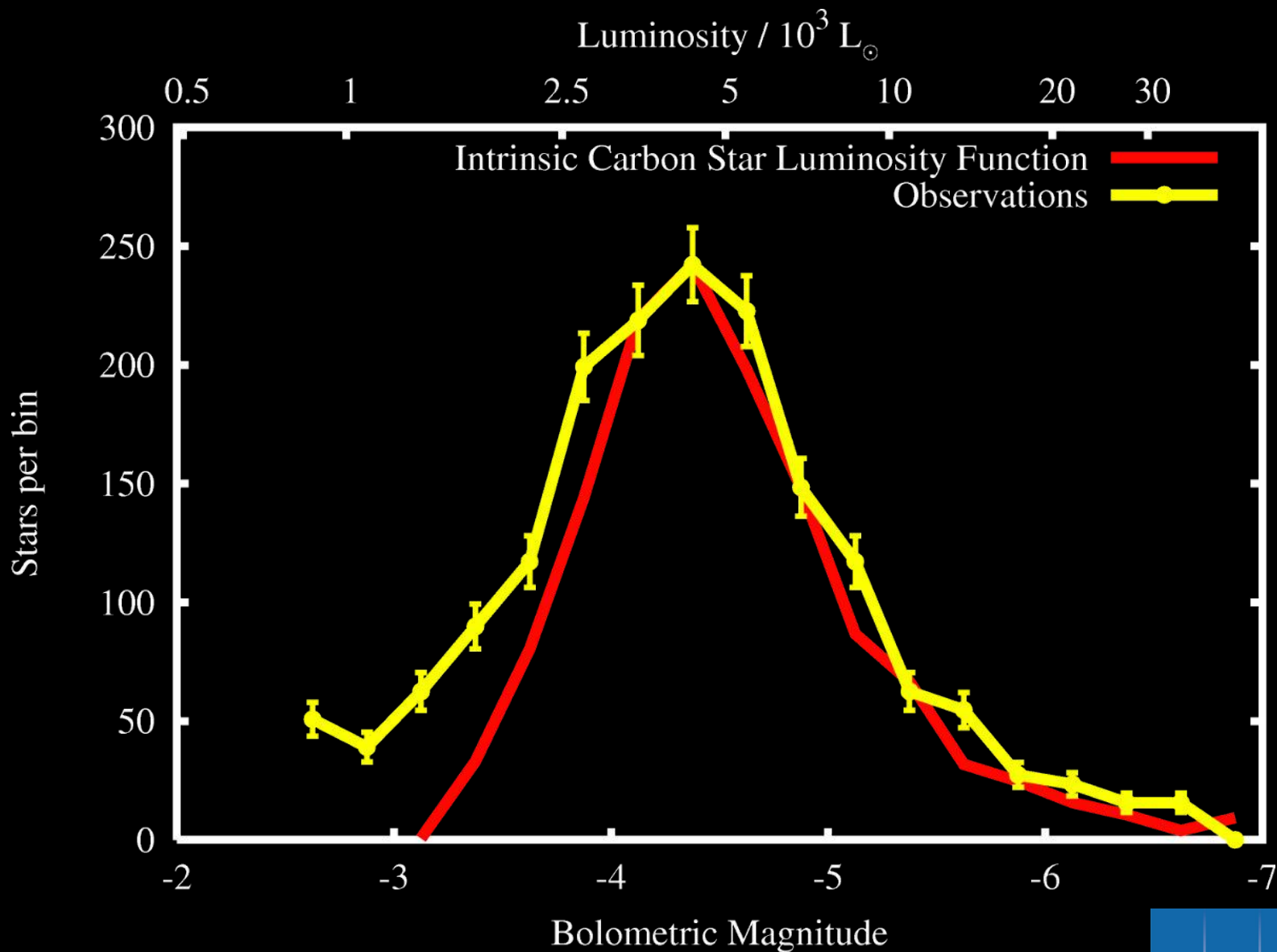


# Some examples of binary\_c

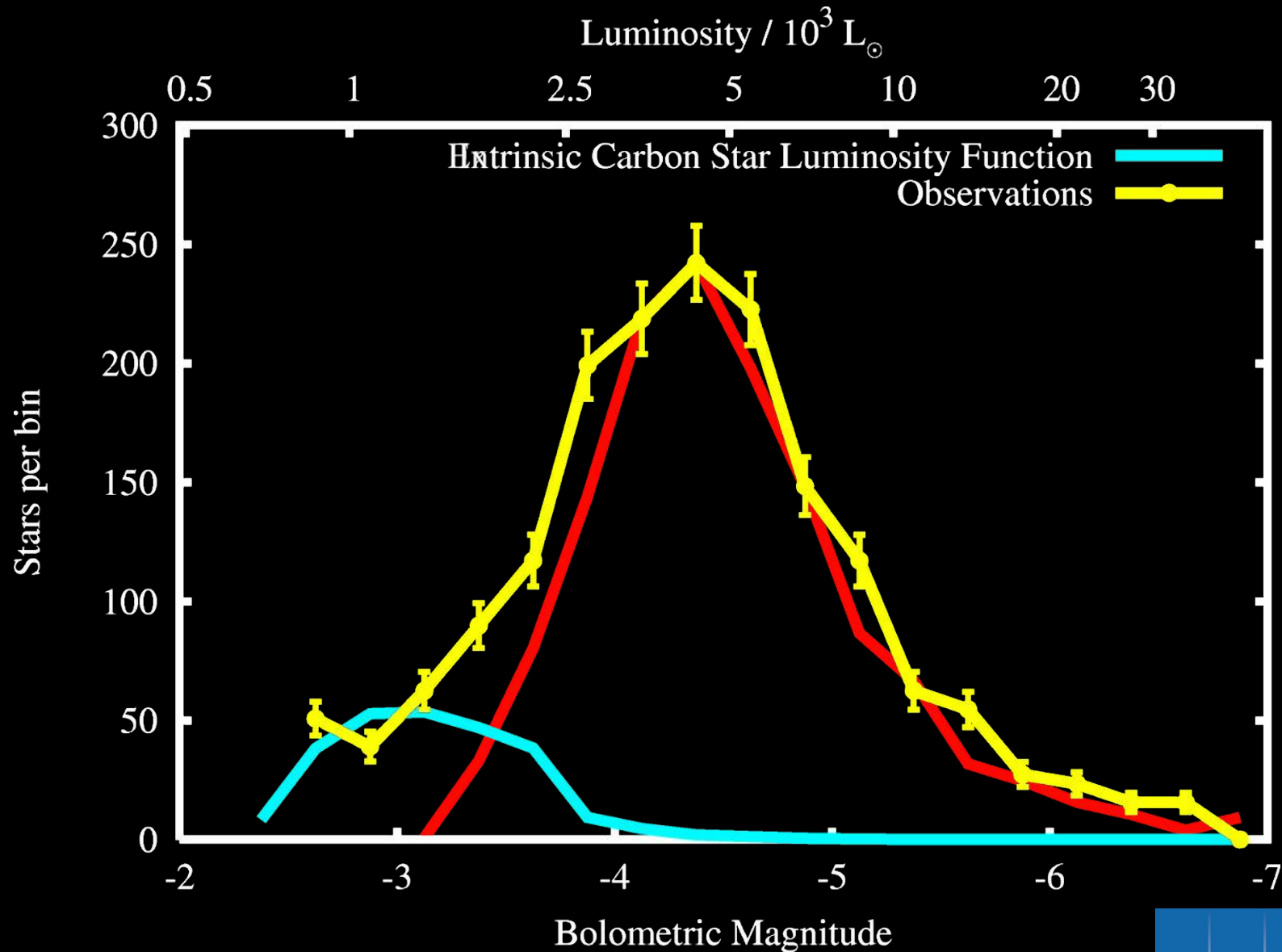
- Remember to try it yourself!
- <http://www.astro.uni-bonn.de/~izzard/cgi-bin/binary3.cgi>

binary_c/nucsyn results											
A frontend to the <a href="#">binary_c/nucsyn</a> code											
Evolution Time (MYr)	Star 1 mass ( $M_{\odot}$ )	Star 2 mass ( $M_{\odot}$ )	Star 1 type	Star 2 type	Separation ( $R_{\odot}$ )	Period	Eccentricity	Star 1 R/ROL	Star 2 R/ROL	What's happening?	
0.0000	14.000	6.000	Main Sequence	Main Sequence	100.000	25.92	0.00	0.106	0.095	In the beginning there was a star...	
14.0936	13.718	6.002	Hertzsprung Gap	Main Sequence	101.340	26.63	0.00	0.256	0.103	Stellar Type Change	
14.1165	13.715	6.003	Hertzsprung Gap	Main Sequence	101.384	26.64	0.00	1.000	0.103	Begin Roche Lobe Overflow	
14.1165	13.715	6.003	Hertzsprung Gap	Main Sequence	101.384	26.64	0.00	1.000	0.103	Common Envelope Evolution in	
14.1165	3.349	6.003	Main Sequence Naked Helium star	Main Sequence	12.748	1.72	0.00	1.000	0.103	Common Envelope Evolution	
14.1165	3.349	6.003	Main Sequence Naked Helium star	Main Sequence	12.748	1.72	0.00	0.112	0.591	End of Roche Lobe Overflow	
16.1738	3.042	6.014	Hertzsprung Gap Naked Helium star	Main Sequence	13.359	1.88	0.00	0.103	0.562	Stellar Type Change	
16.3312	2.978	6.023	Hertzsprung Gap Naked Helium star	Main Sequence	13.397	1.89	0.00	1.003	0.559	Begin Roche Lobe Overflow	

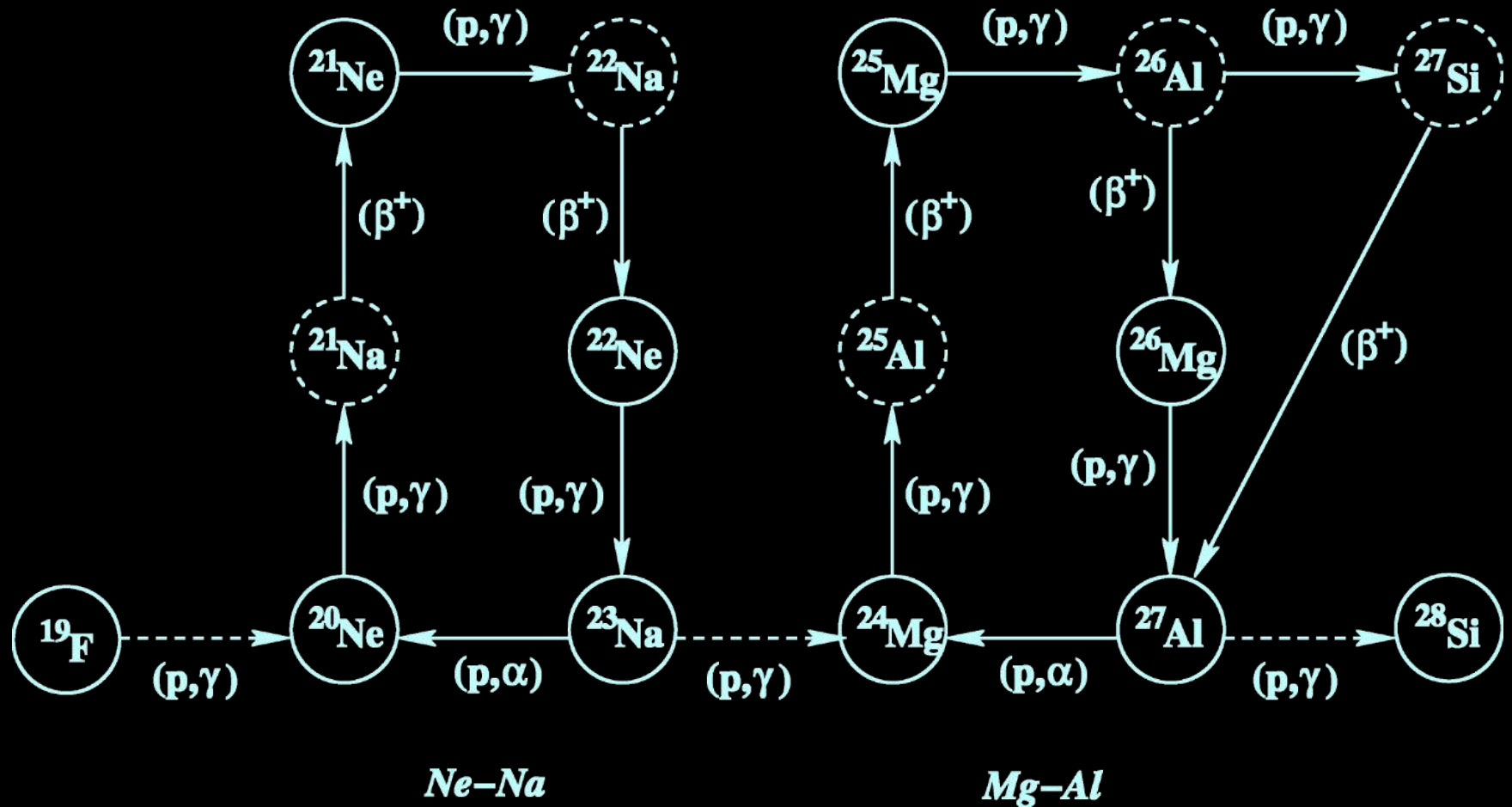
# Low-L Carbon Stars



# Low-L Carbon Stars



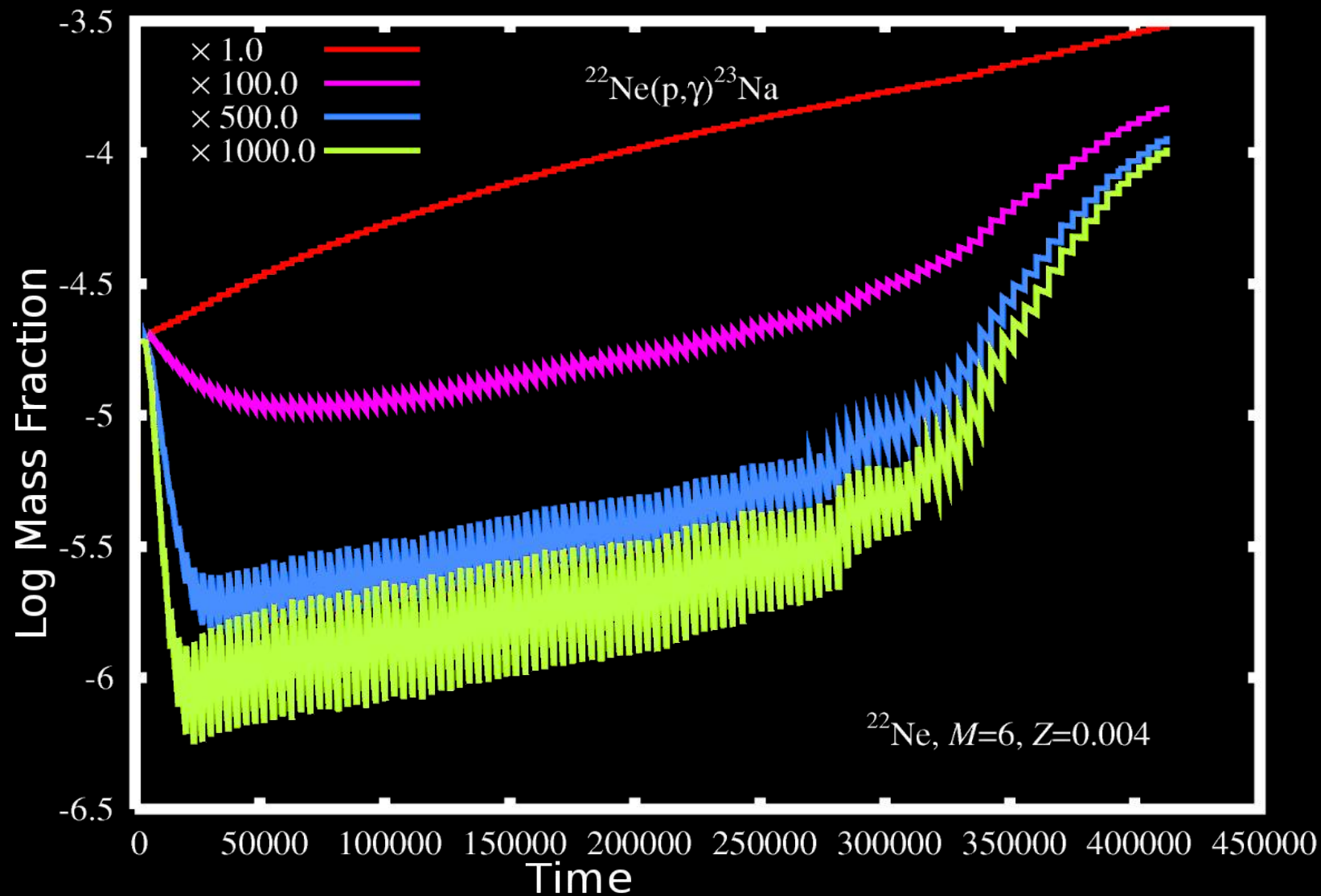
# Nuclear Burning Rates



# Nuclear Burning Rates

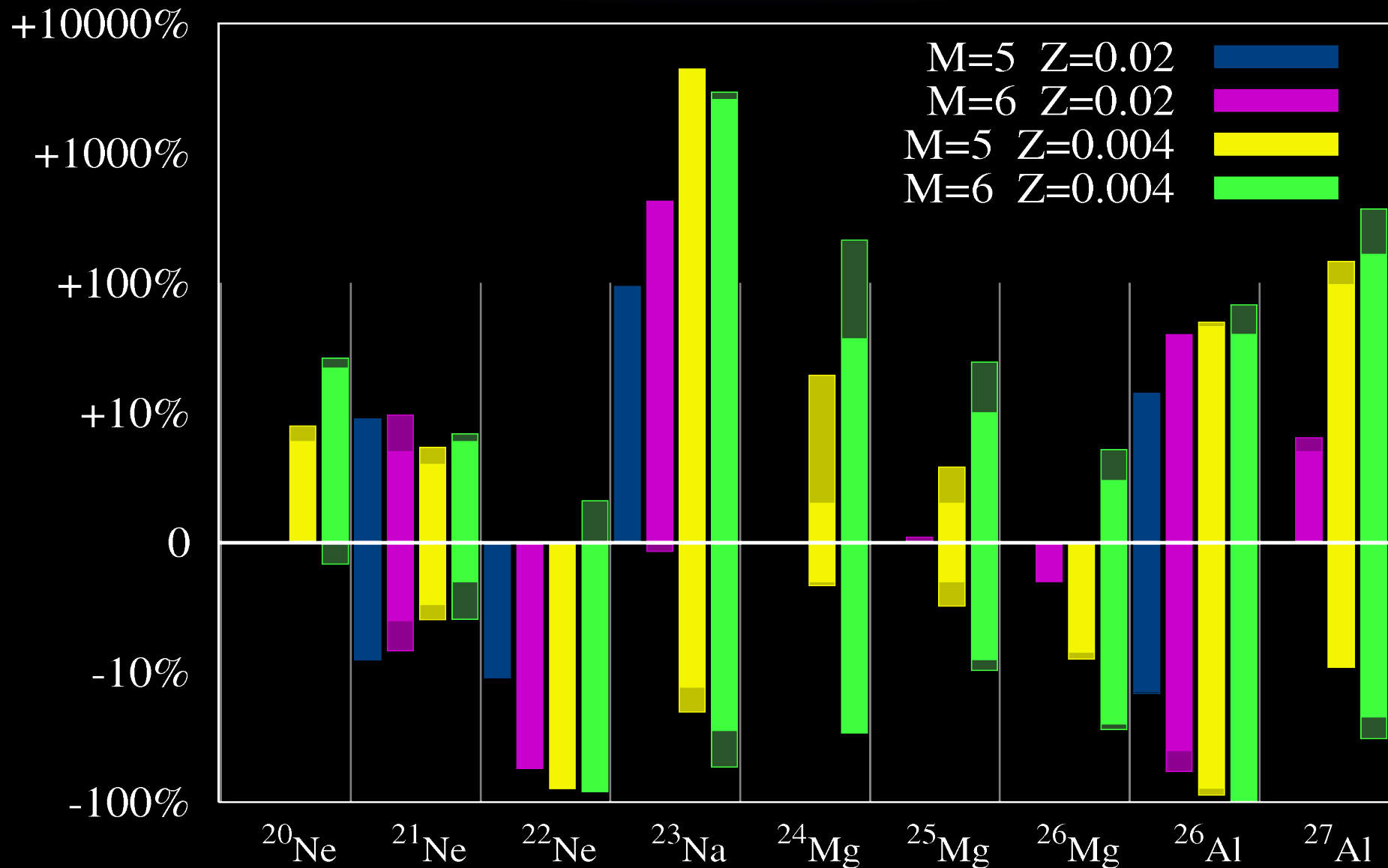
Rate			Source
$^{20}\text{Ne}(p, \gamma)^{21}\text{Na}(\beta^+)^{21}\text{Ne}$	-50%	+50%	NACRE
$^{21}\text{Ne}(p, \gamma)^{22}\text{Na}(\beta^+)^{22}\text{Ne}$	-20%	+20%	Iliadis et al. 2001
$^{22}\text{Ne}(p, \gamma)^{23}\text{Na}$	-50%	$\times 2000$	Hale et al. 2001
$^{23}\text{Na}(p, \alpha)^{20}\text{Ne}$	-30%	+30%	Rowland et al. 2004
$^{23}\text{Na}(p, \gamma)^{24}\text{Mg}$	/40	$\times 10$	Rowland et al. 2004
$^{24}\text{Mg}(p, \gamma)^{25}\text{Al}(\beta^+)^{25}\text{Mg}$	-17%	+20%	Powell et al. 1999
$^{25}\text{Mg}(p, \gamma)^{26}\text{Al}(\beta^+)^{26}\text{Mg}$	-50%	$\times 1.5$	Iliadis et al. 2001
$^{26}\text{Mg}(p, \gamma)^{27}\text{Al}$	/4	$\times 10$	Iliadis et al. 2001
$^{26}\text{Mg}(p, \gamma)^{27}\text{Al}$	-25%	$\times 3$	Iliadis et al. 2001
$^{26}\text{Al}(p, \gamma)^{27}\text{Si}$	/2	$\times 600$	Iliadis et al. 2001

# Nuclear Burning Rates



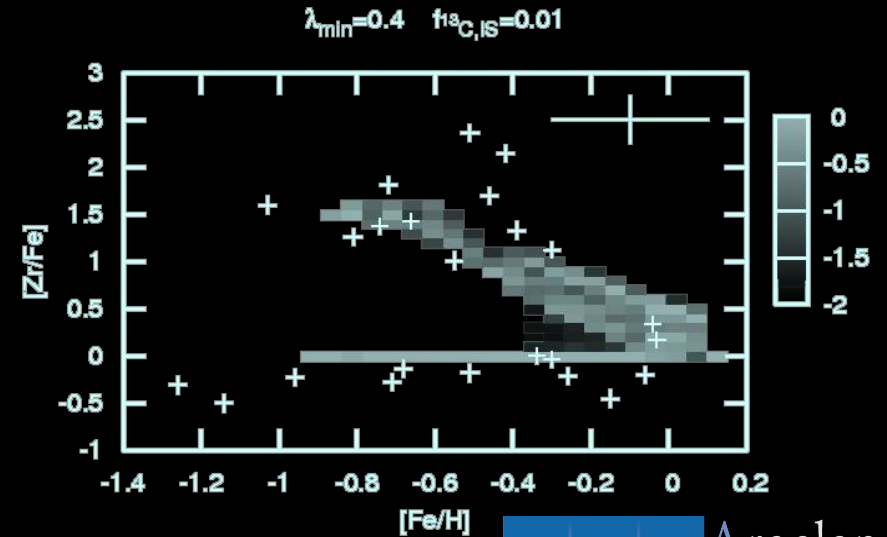
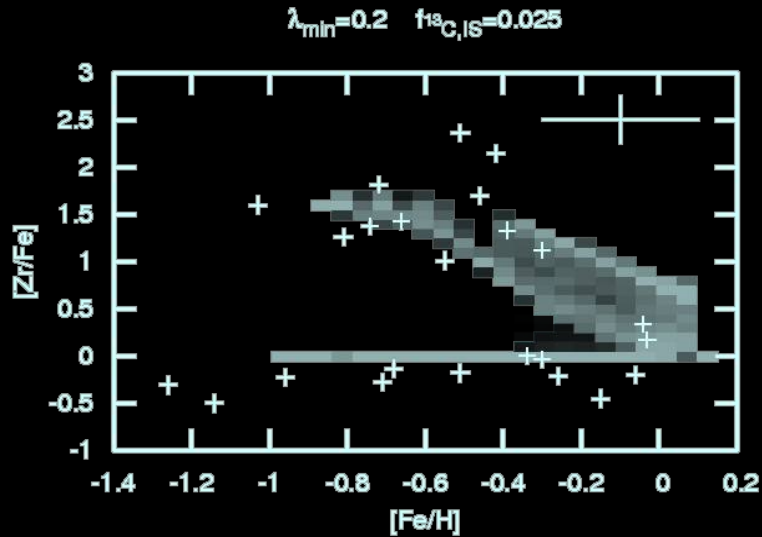
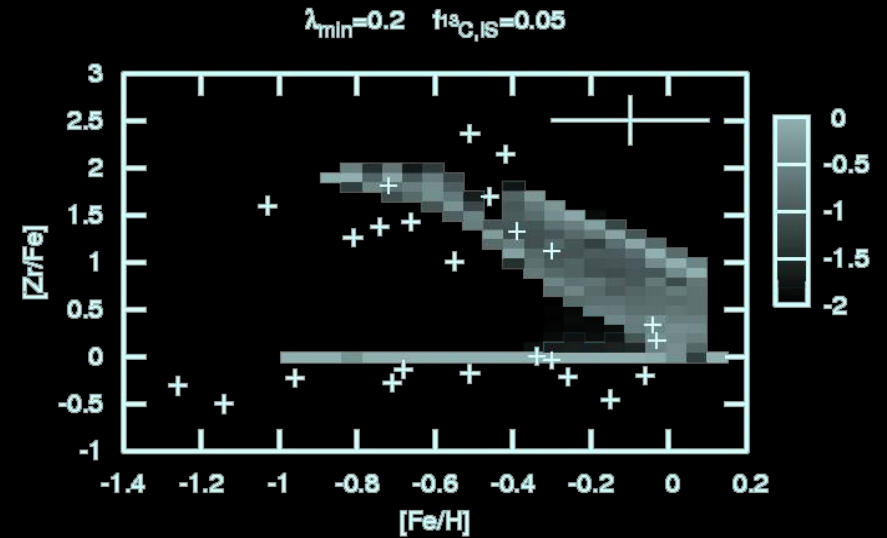
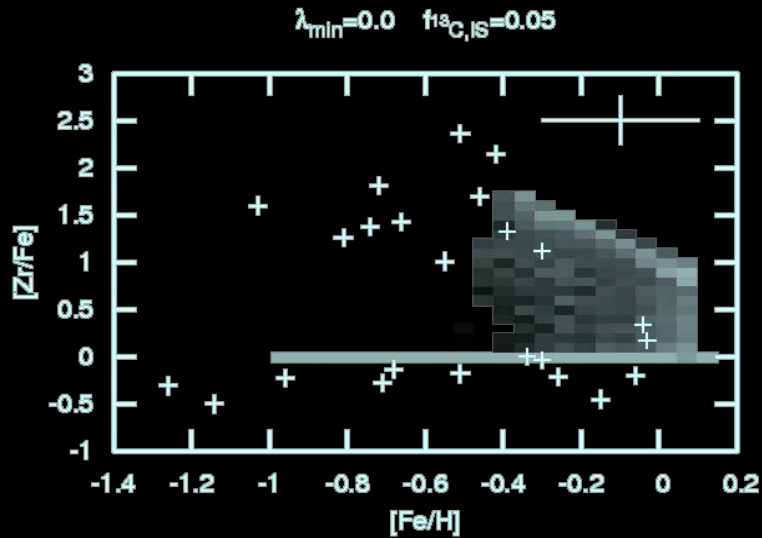
Izzard et al. 2007

# Nuclear Burning Rates



Izzard et al. 2007

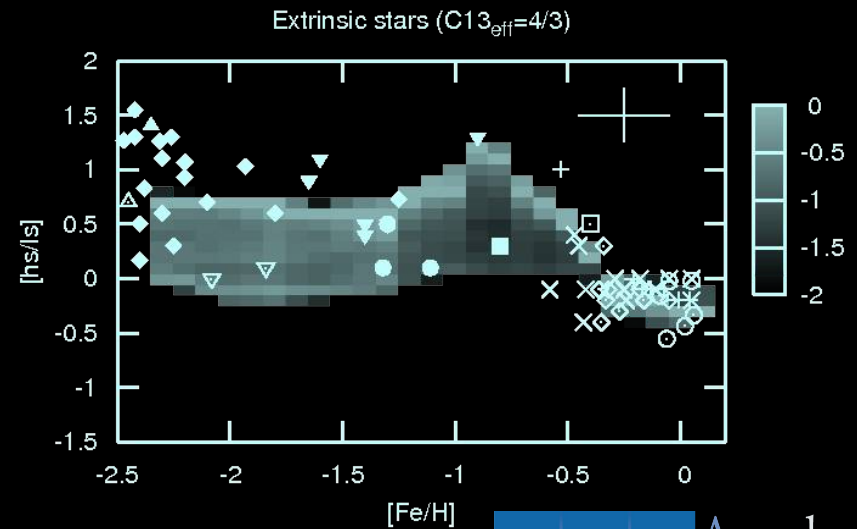
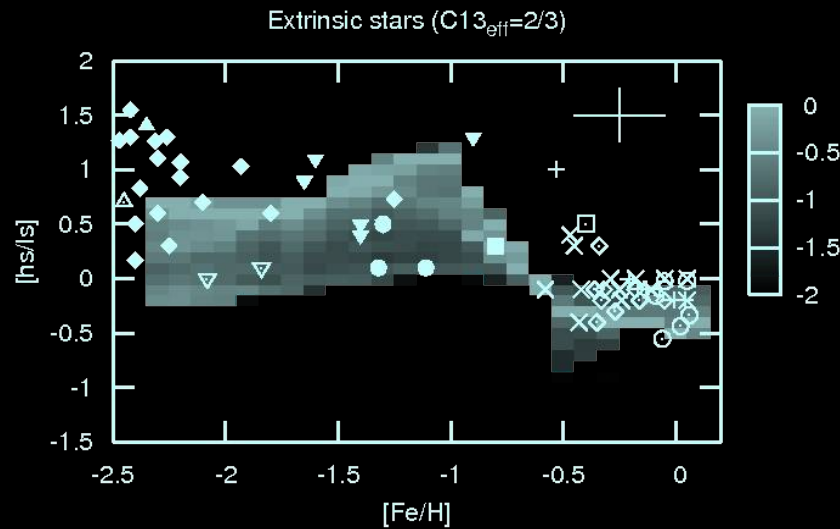
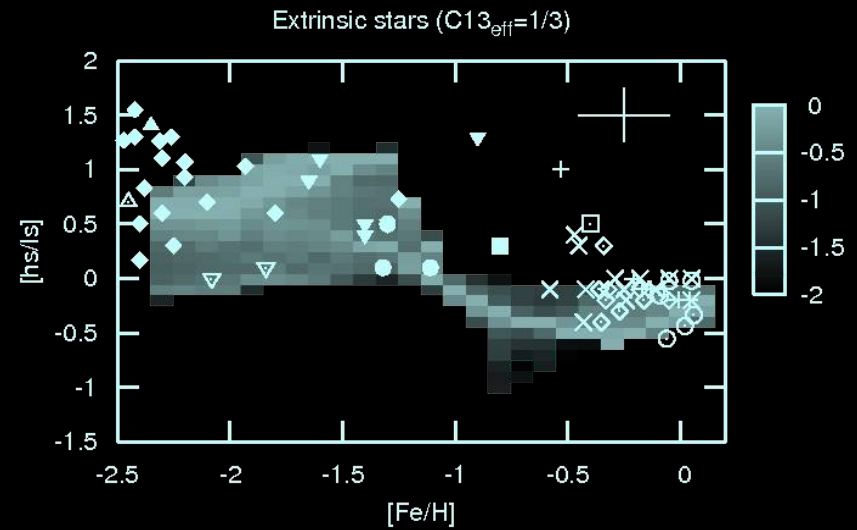
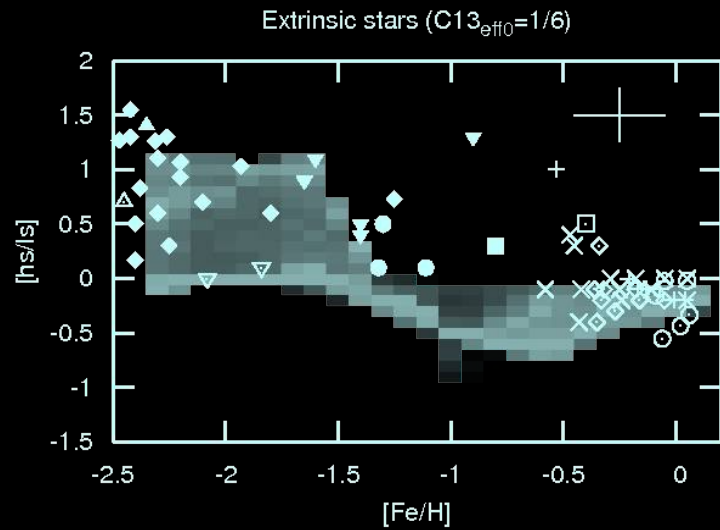
# s-process in post-AGB



Bonacic et al. 2007

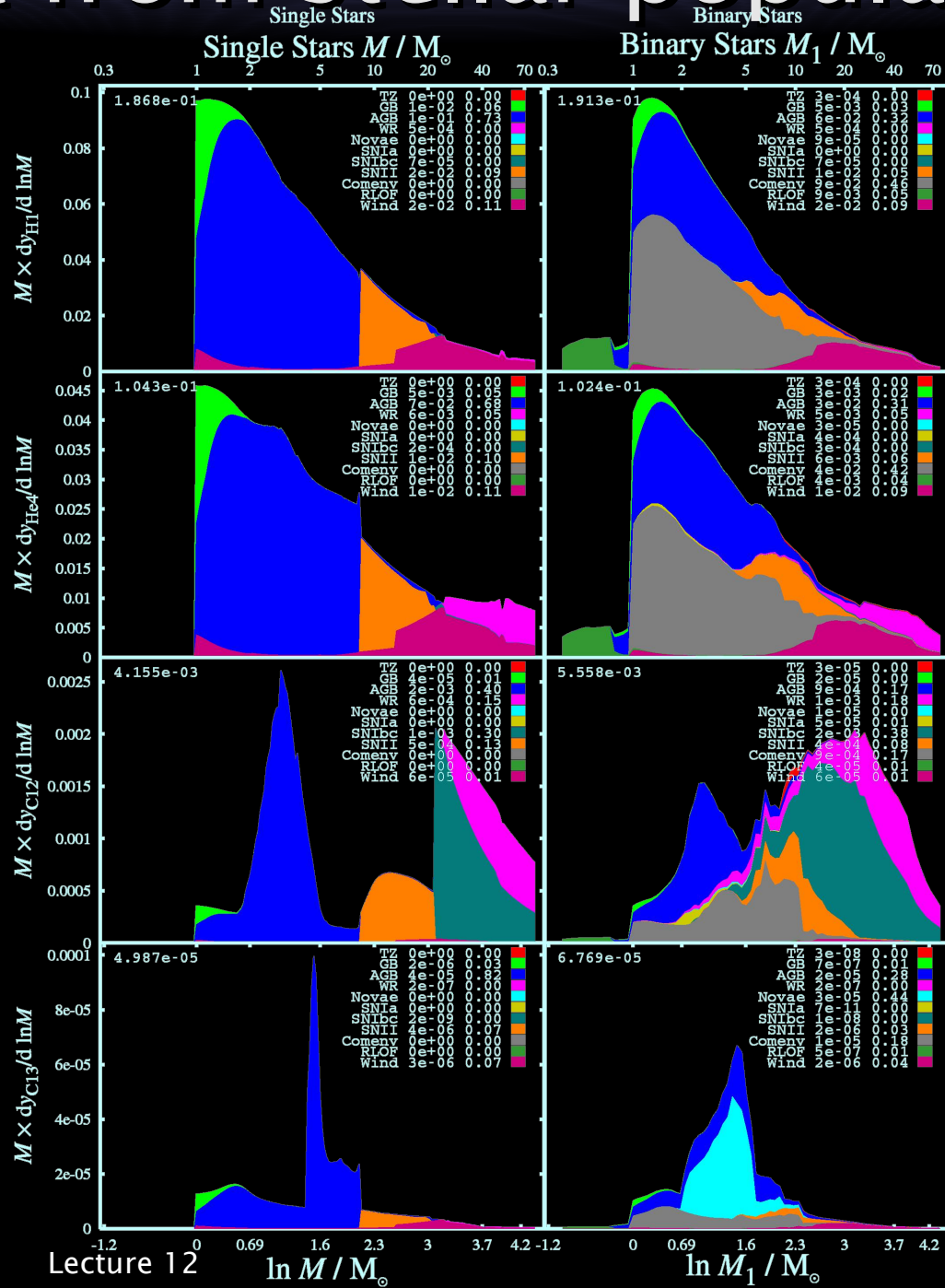


# s-process in post-AGB



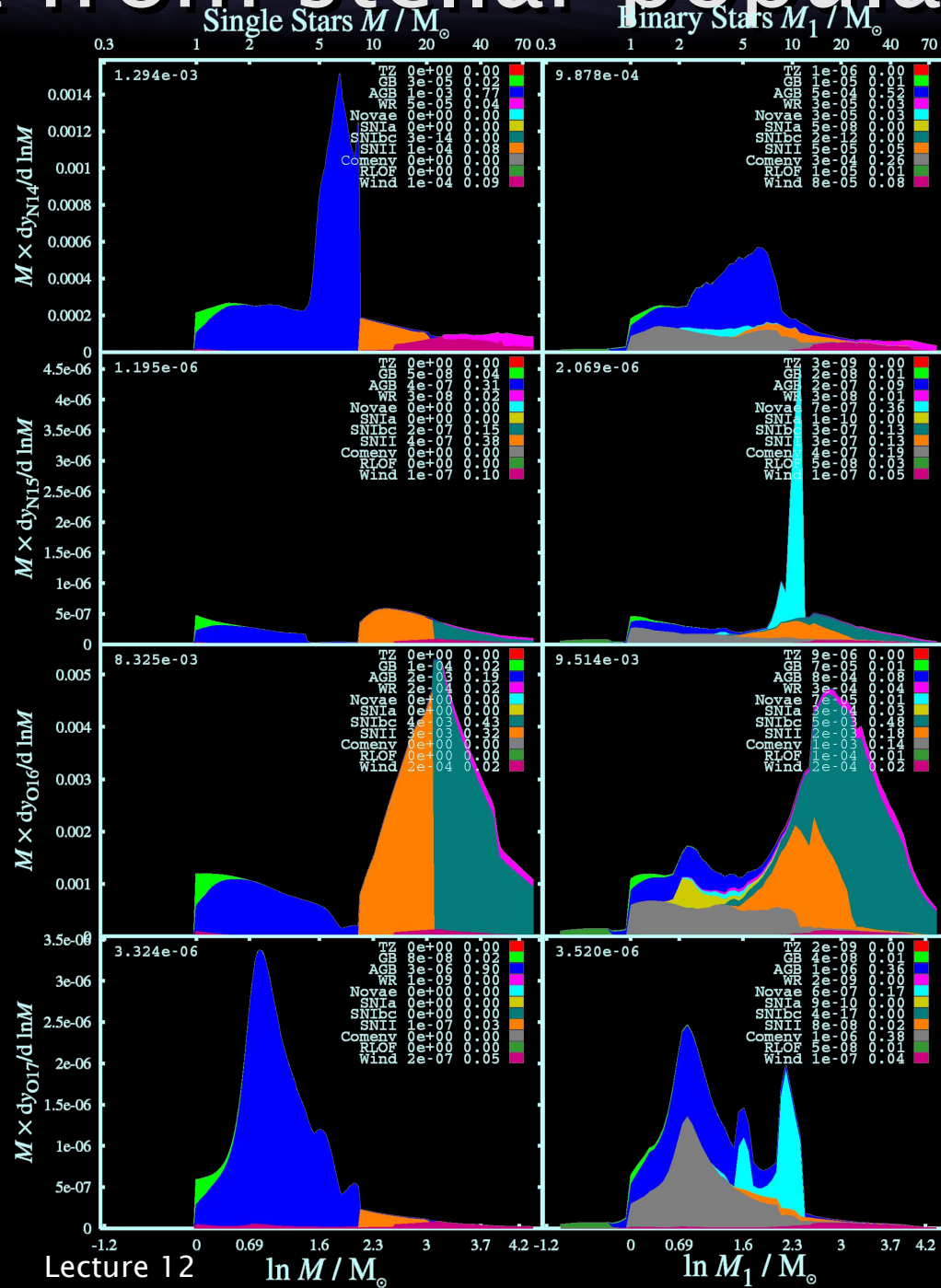
Bonacic et al. 2007

# Ejecta from stellar populations



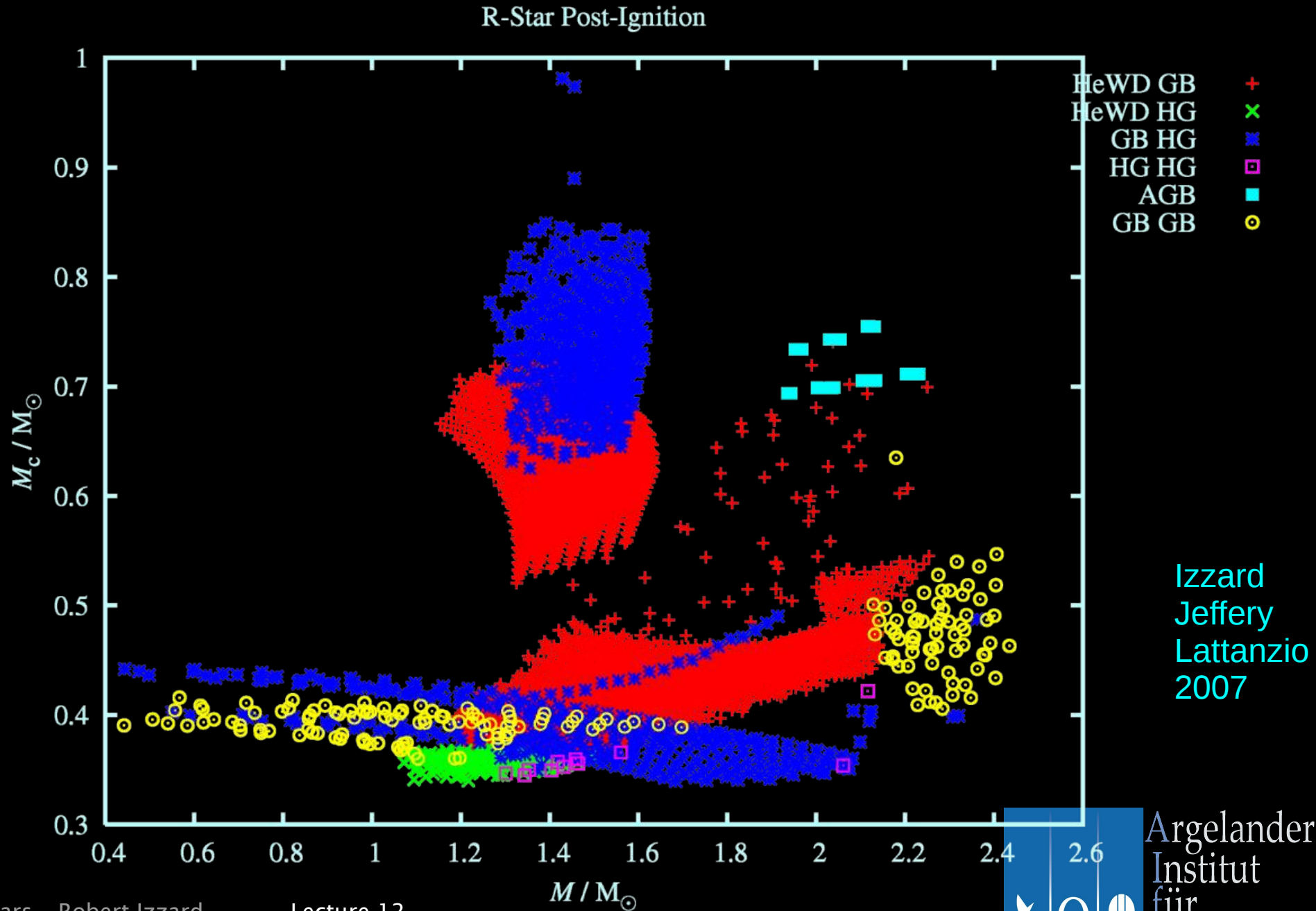
Izzard PhD!

# Ejecta from stellar populations

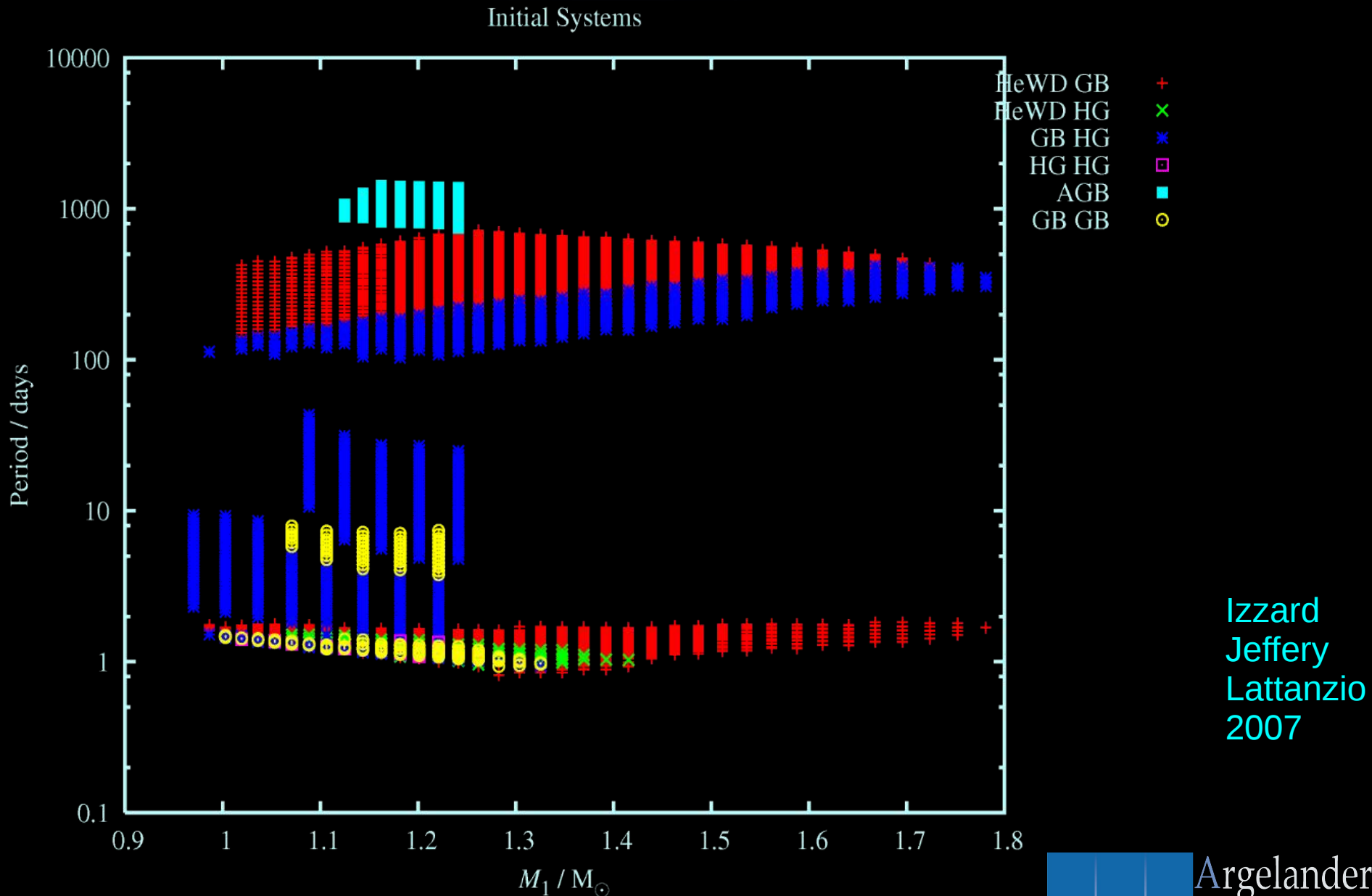


Izzard PhD!

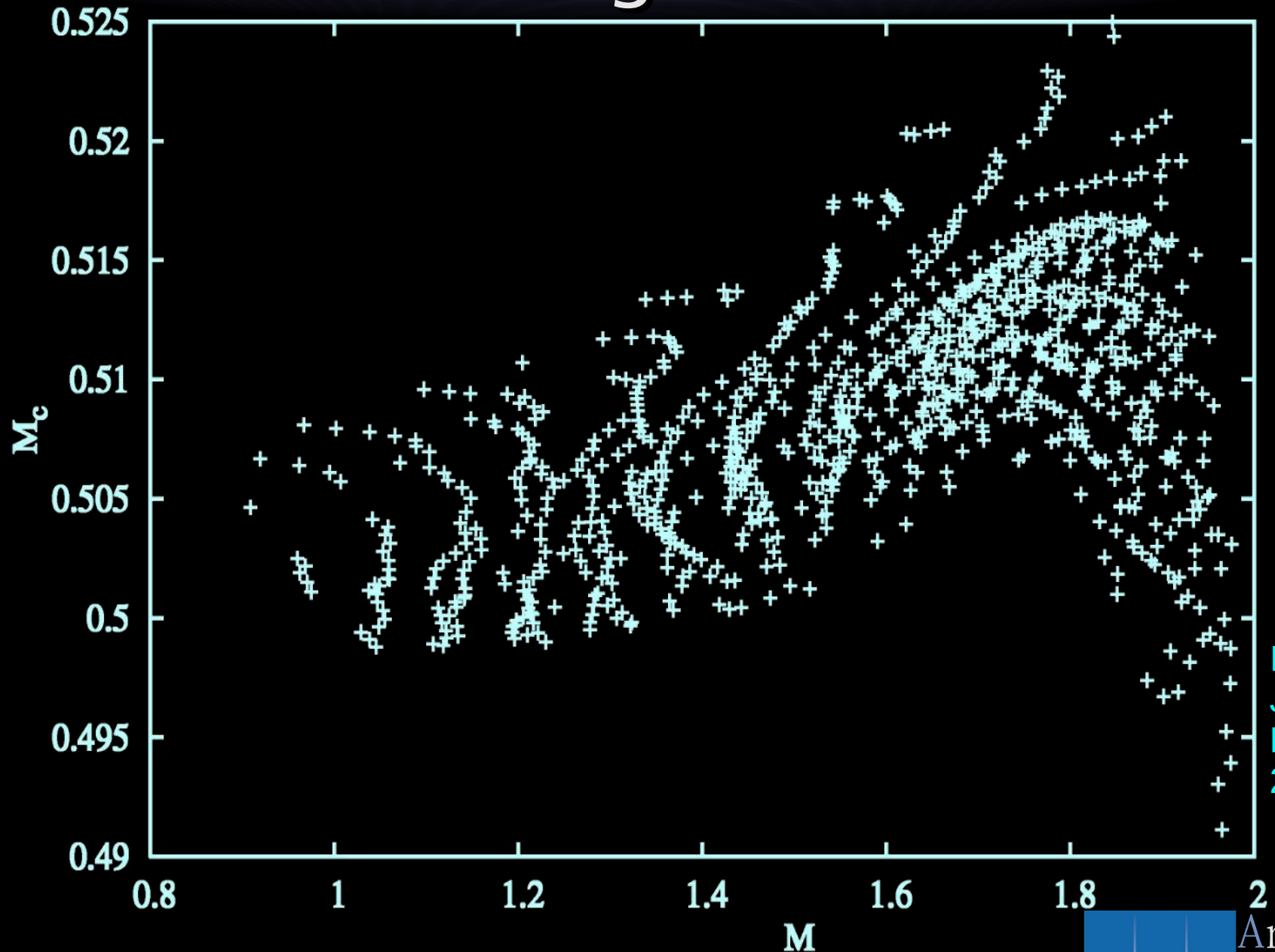
# Stellar Mergers: R Stars



# Stellar Mergers: R Stars

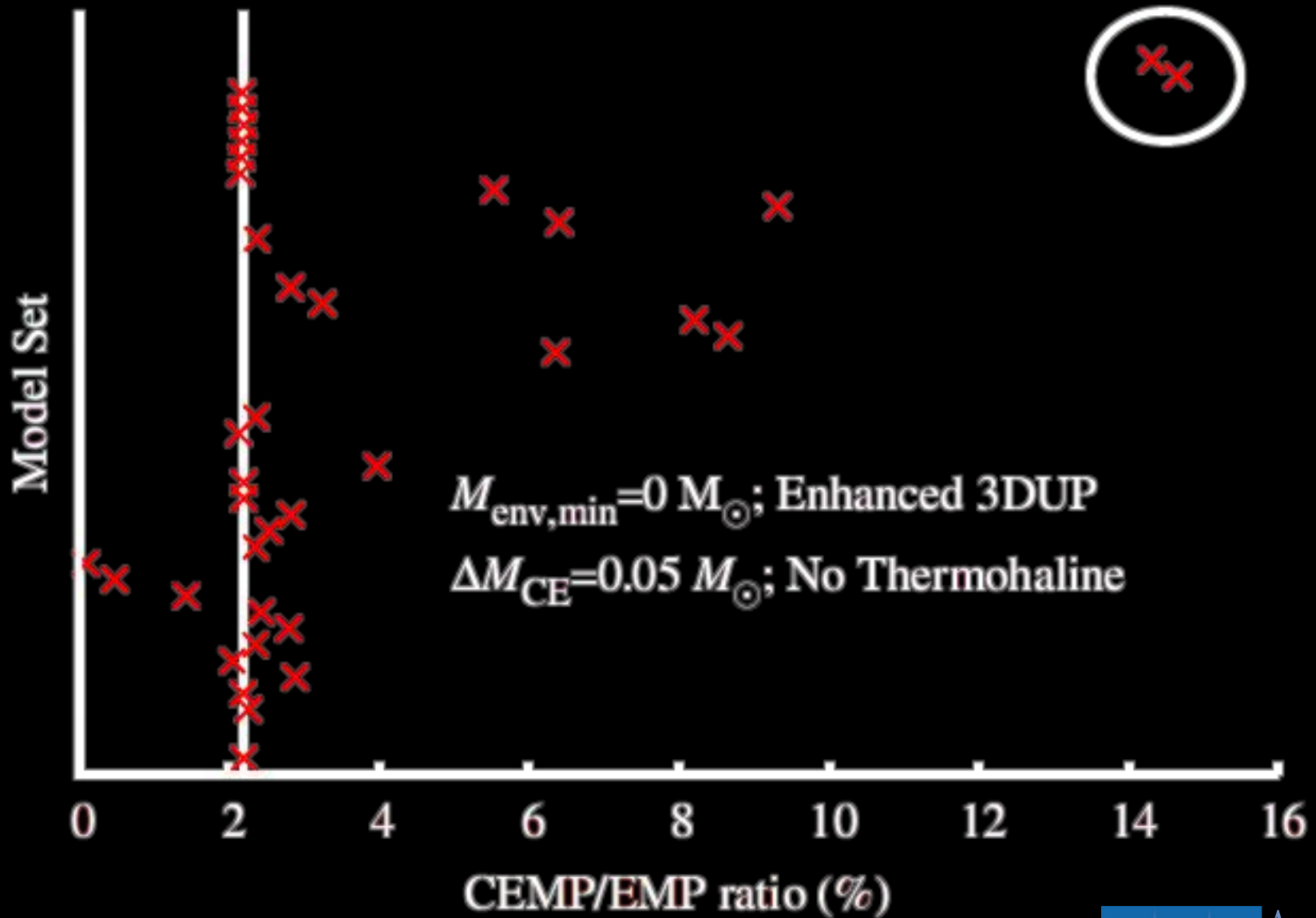


# Stellar Mergers: R Stars

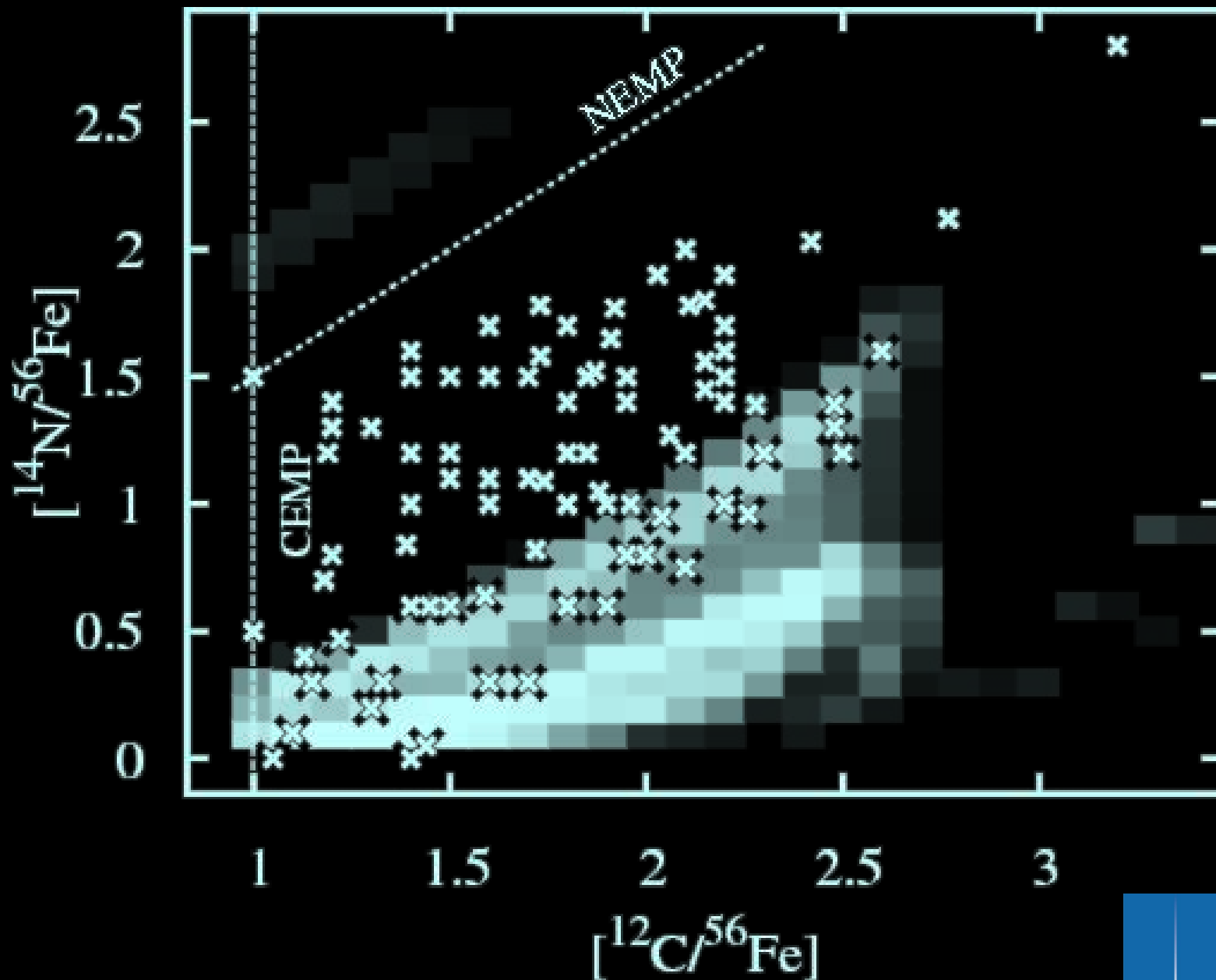


Izzard  
Jeffery  
Lattanzio  
2007

# CEMP stars

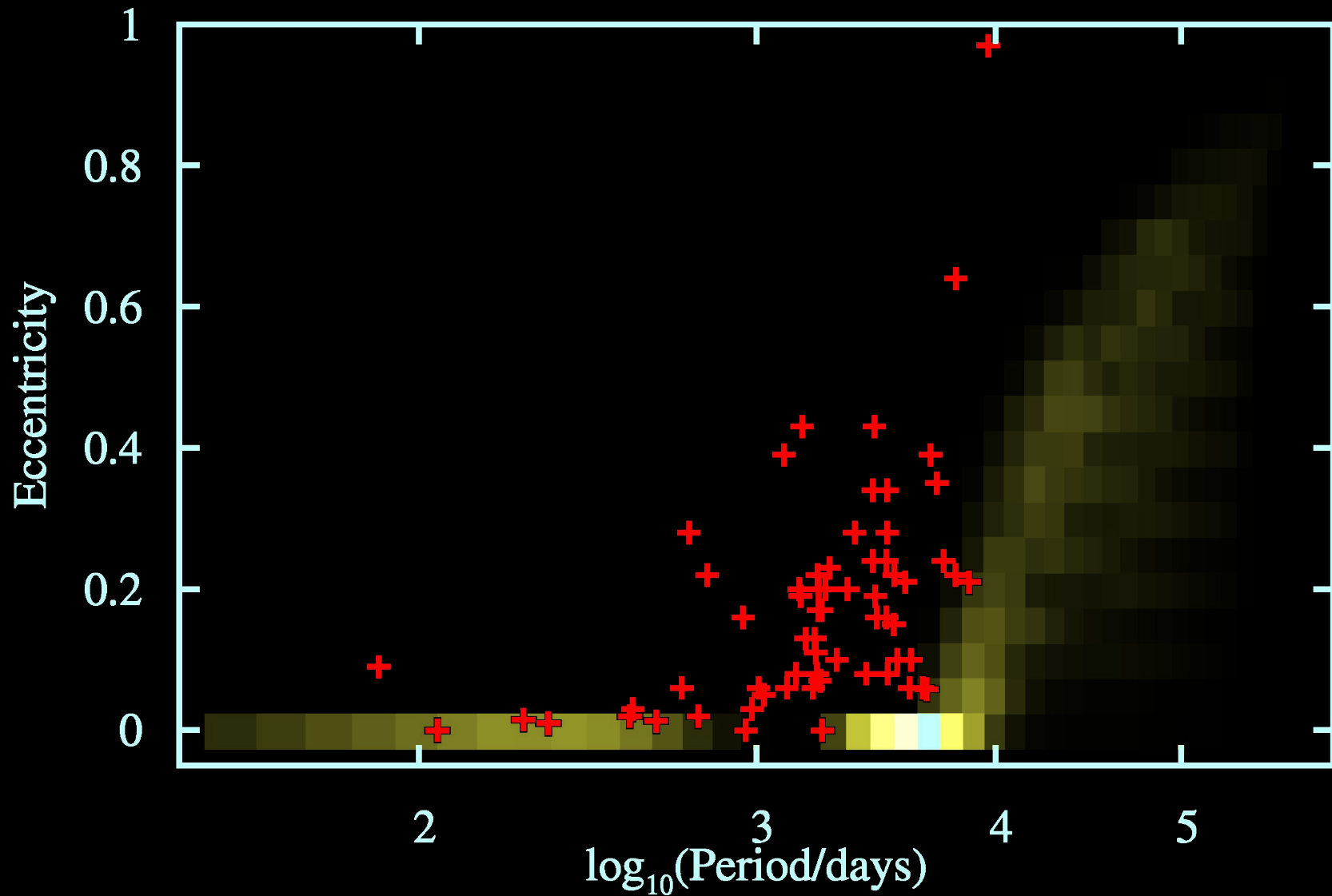


# CEMP stars

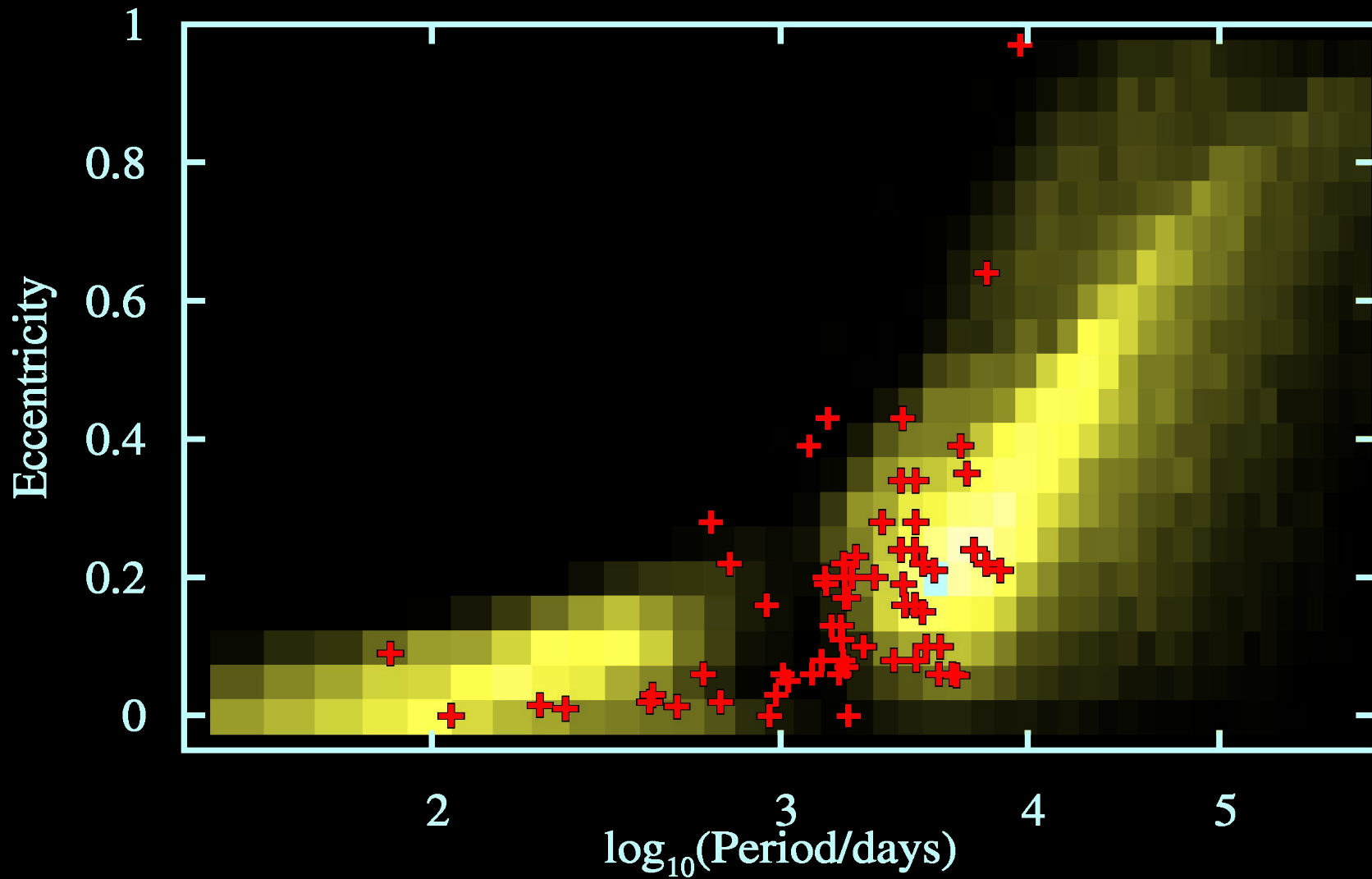




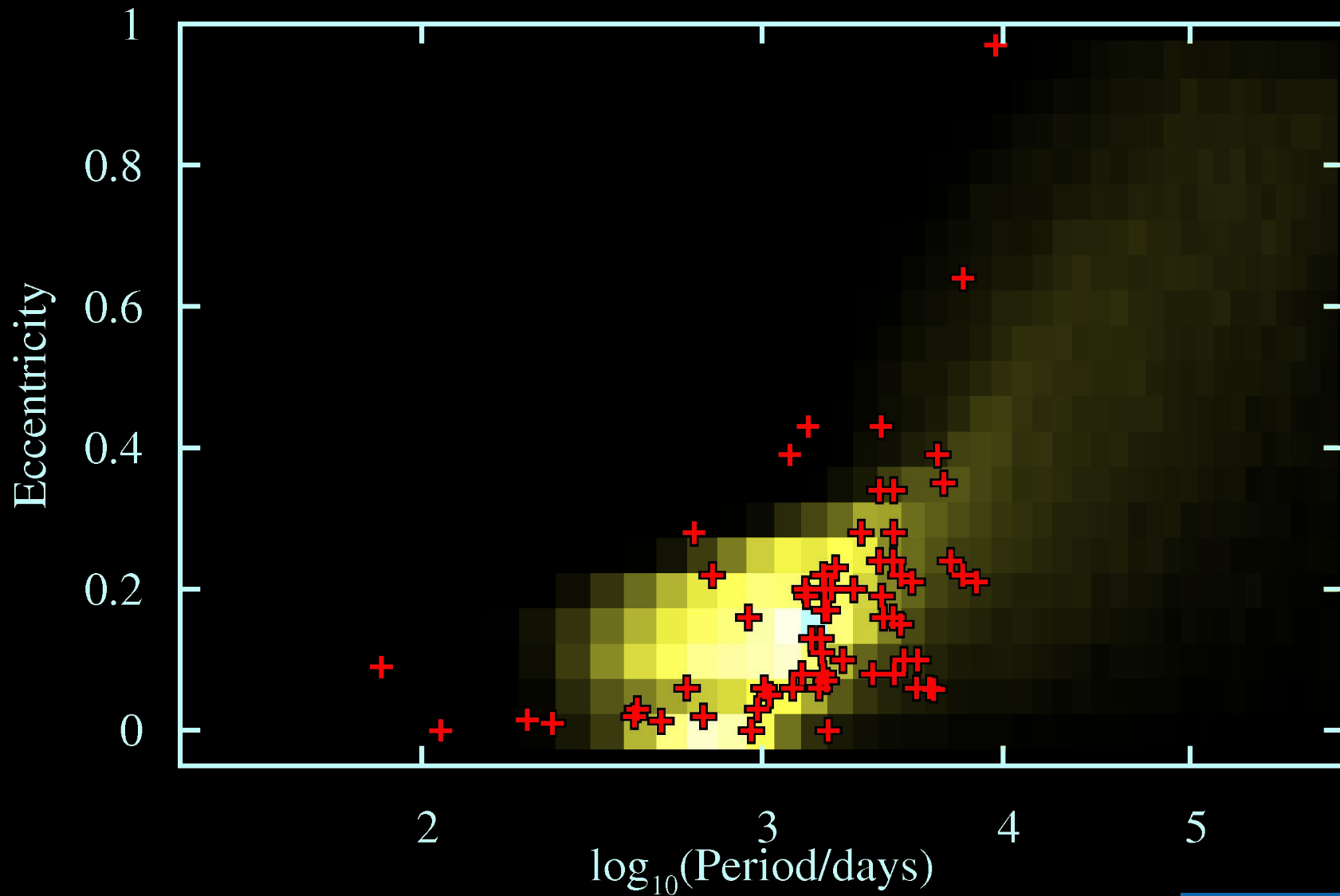
# Barium Stars



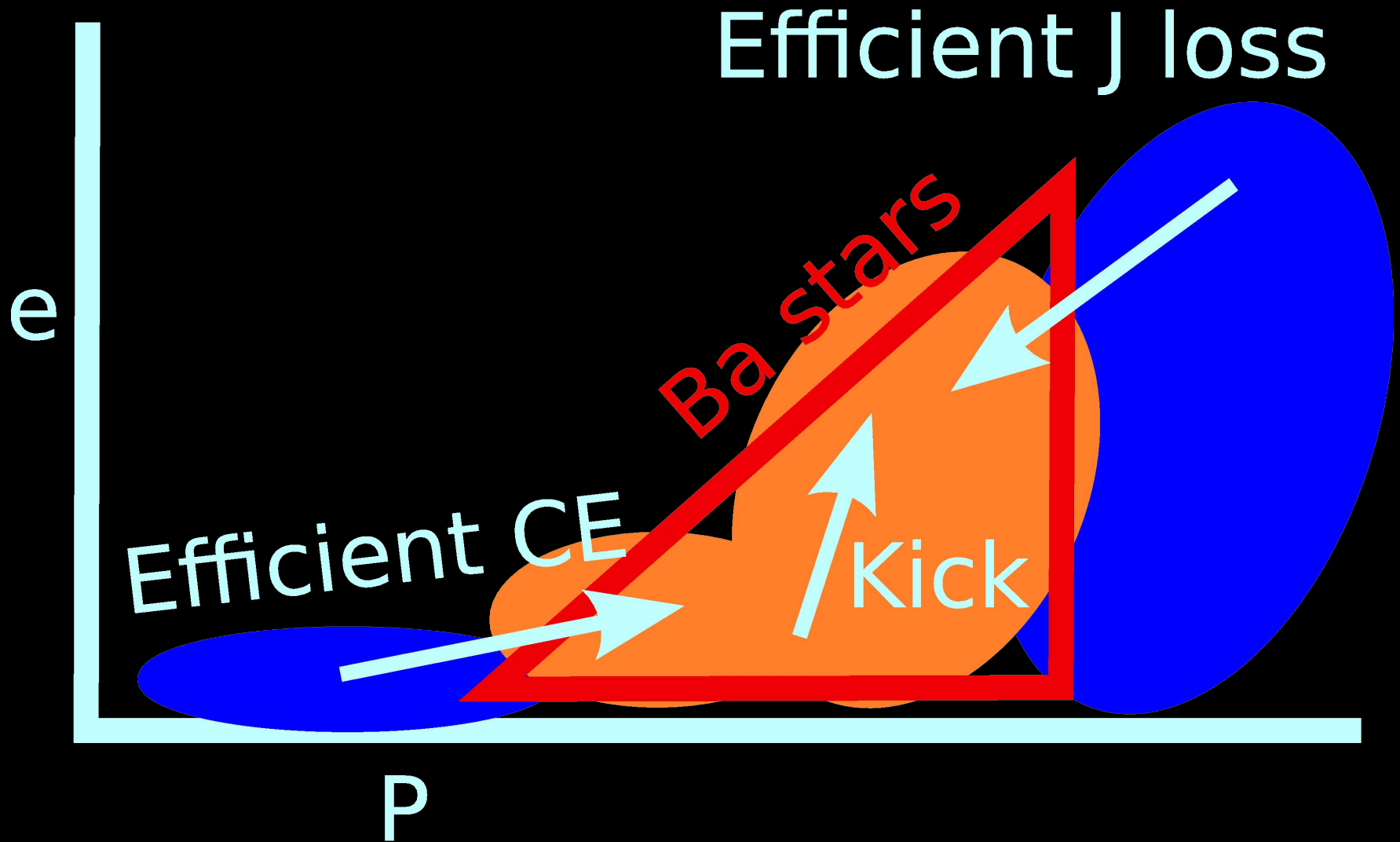
# Barium Stars



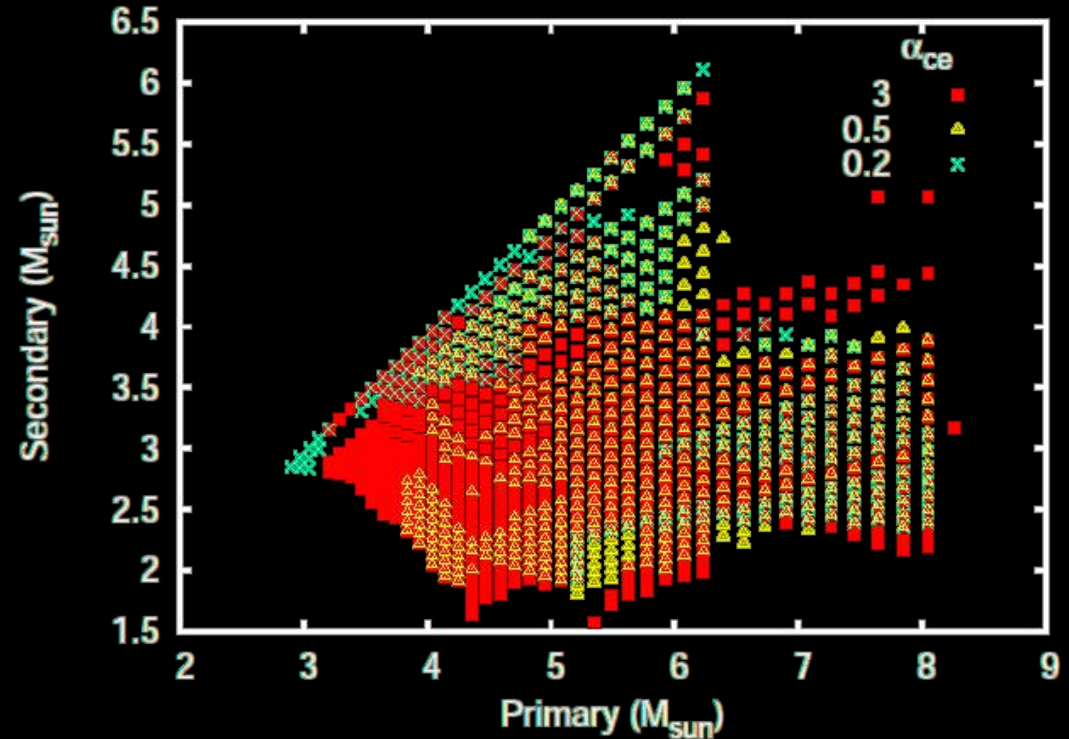
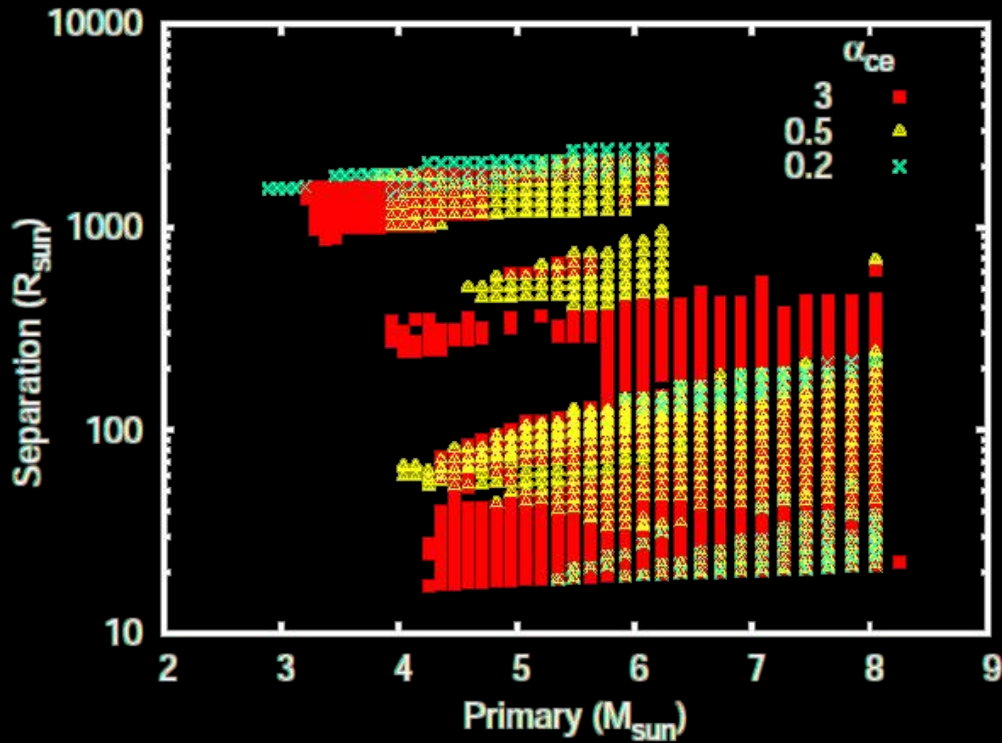
# Barium Stars



# Barium Stars



# Ia Supernovae

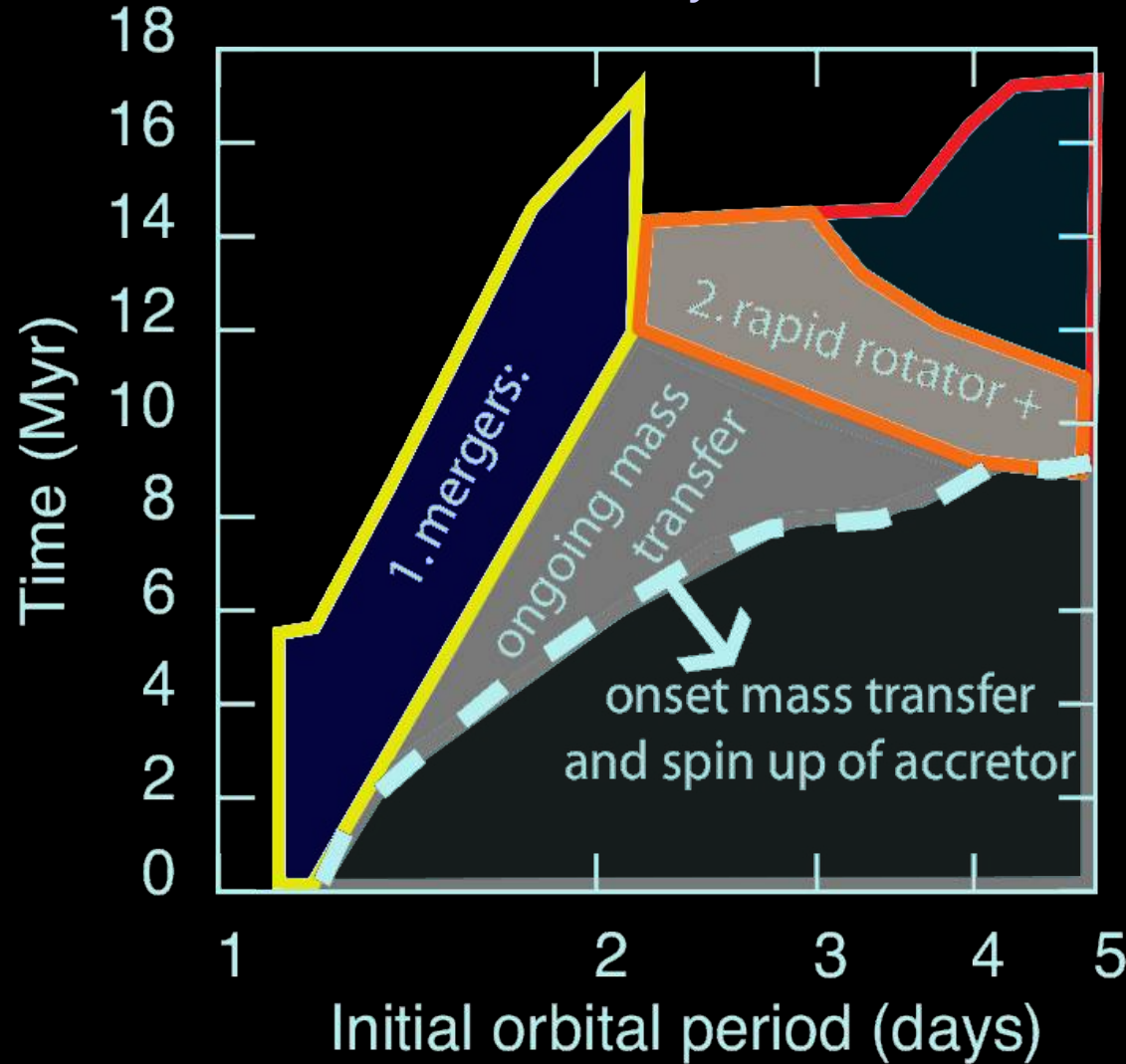


Initial systems that evolve towards a type Ia SN according to the DD channel.  
Different colors indicate different  $\alpha_{\text{ce}}$ .  $\lambda_{\text{ce}}$  is 1.

Joke Claeys (work in progress!)

# Massive Stars

The fate of a 20+15  $M_{\odot}$  close binary as a function of initial period.



De Mink et al. 2010/11

# The end!

- Exam:

Tuesday 17<sup>th</sup> July

10.00–11.30am

Herbert Lau will be supervising you.

- Good luck! Thanks for coming :)